Department of Mathematics



SF1624/SF1684 Algebra and Geometry Year 2018/2019

Problems for Seminar 1

Check the canvas page of the course for information on how seminars are run and what you are expected to do before and during the seminars.

The seminar starts with a test. The problem will be about finding an equation for a line or a plane in \mathbb{R}^3 with certain properties.

In the seminar, the following problems will be discussed.

Problem 1. The points P, Q, and R have coordinates

$$P = \begin{bmatrix} 1\\2\\0 \end{bmatrix}, \quad Q = \begin{bmatrix} -1\\0\\1 \end{bmatrix}, \quad R = \begin{bmatrix} 4\\6\\-1 \end{bmatrix},$$

and the plane Π is given by the equation

$$2x - y + 2z = 3$$

- (a) Compute a parameter form for the line L through P and Q.
- (b) Does the line L contain the point R?
- (c) Determine the intersection of Π and L.
- (d) Compute an equation for the plane which is orthogonal to L and contains P.

Problem 2. For each number t, we are given a triangle T with vertices

$$A = \begin{bmatrix} 1\\2\\3 \end{bmatrix}, \quad B = \begin{bmatrix} 1\\0\\-2 \end{bmatrix} \quad \text{and} \quad C = \begin{bmatrix} t\\t\\1 \end{bmatrix}.$$

- (a) For which value of t is T right-angled at A?
- (b) Compute the other two angles for this value of t (use a calculator).
- (c) Find a value for t such that the point C is closest to A.

Problem 3. Find an equation for the plane consisting of all points with equal distance to the point A = (-1, 1, 2) and to the point B = (1, 5, -4). (*Hint*: The mid point of the line segment between A and B lies in the plane.)

MISCELLANEOUS

Here are some other topics that are important and interesting to discuss.

- How many equations does one need to define an *m*-dimensional subspace of \mathbb{R}^n ? How many free variables are needed in a parametric form?
- What is the expected intersection between two planes in \mathbb{R}^3 , in \mathbb{R}^4 , and in \mathbb{R}^5 ?
- What might the angle between a line and a plane or between two planes in \mathbb{R}^3 mean? How can one compute this angle?