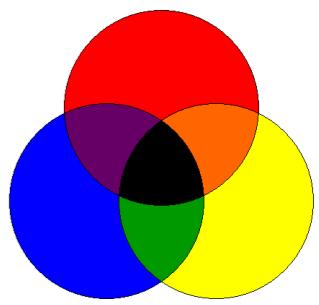


This is what you should know after this lecture + own work:

1. How does an x-ray tube works: physical principles and technological solutions
2. Energy spectrum emitted from x-ray tube, characteristics and origin.
3. How a radiation detector (photon counting and energy integrating) works in principles.
4. Detection efficiency (geometric, intrinsic and total) definition and how to evaluate it in simple cases
5. Difference between emitted and detected spectrum
6. Difference and relationship among activity, emitted photons, detected photons, count rate

X-ray tube Detectors

Physics



- Beer's law
 - attenuation factor, linear and mass attenuation coefficient, primary photons . . .
- Object contrast
 - depends on photon E (given the object!)

Technology

Not much

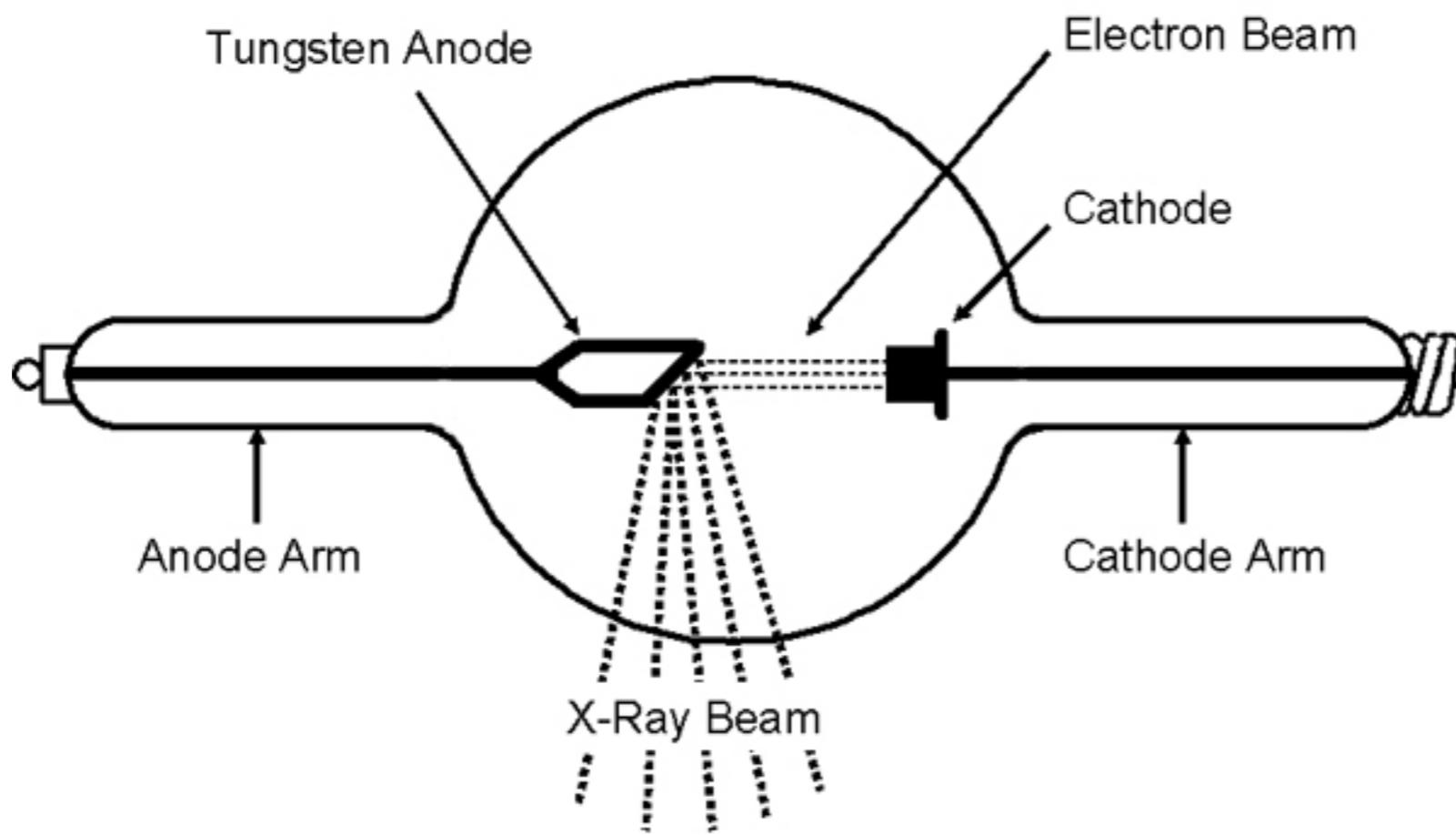
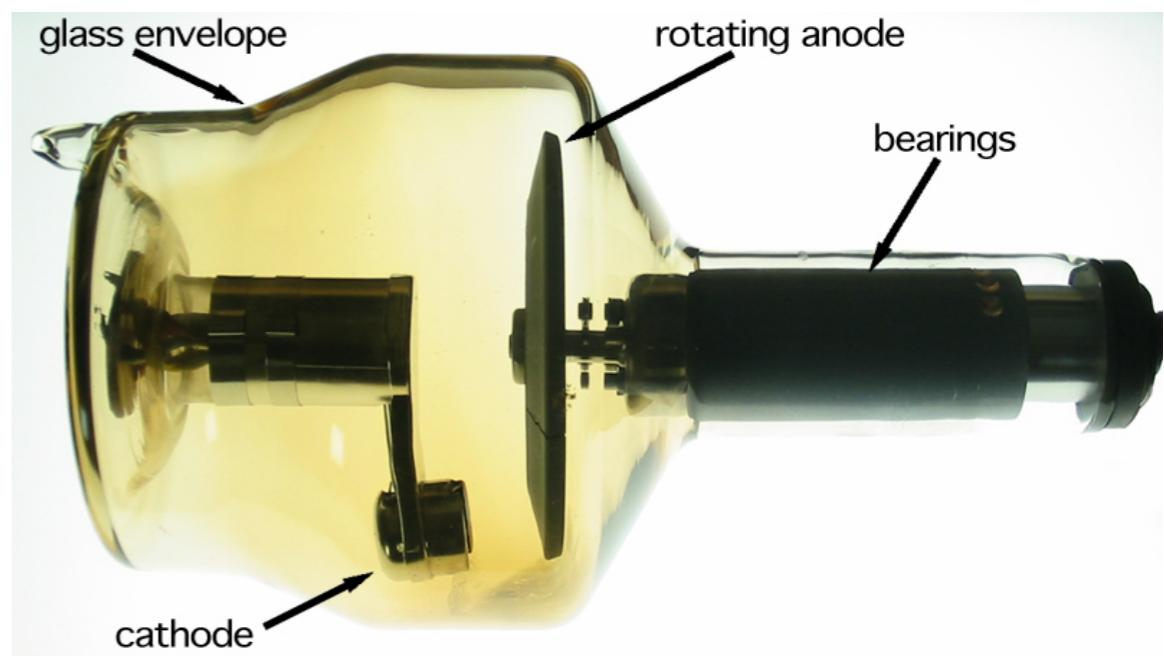
object contrast
vs
image contrast

Clinical need/application

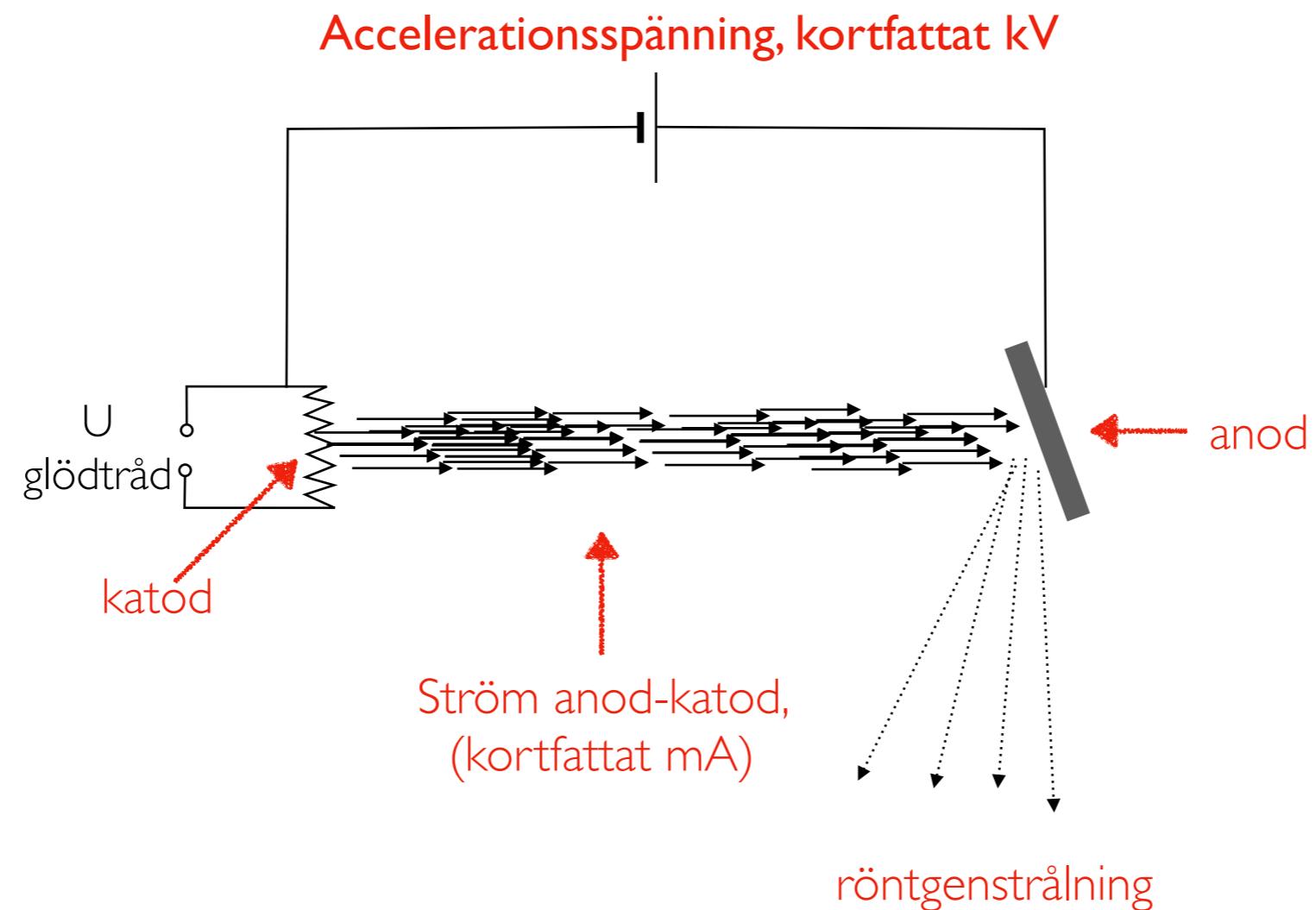
Some “hints”. Started discussing, for example, that Compton is not accounted for

X-ray sources

Röntgenrör



Röntgentrör enkel schema:

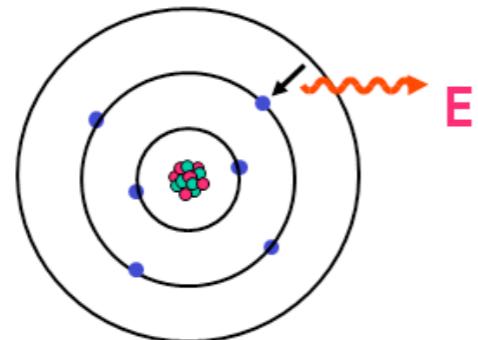


Vad händer i anoden?

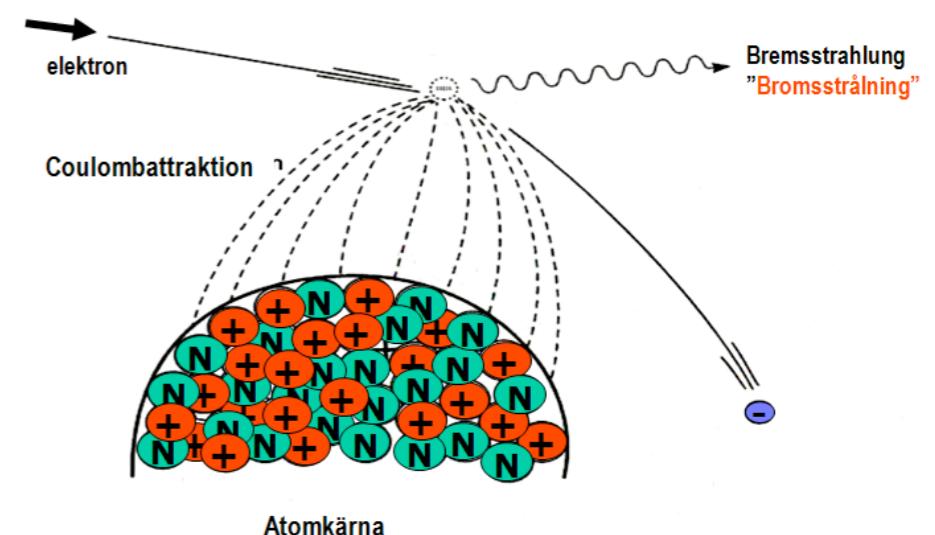
laddade partiklar

$e^- - e^-$

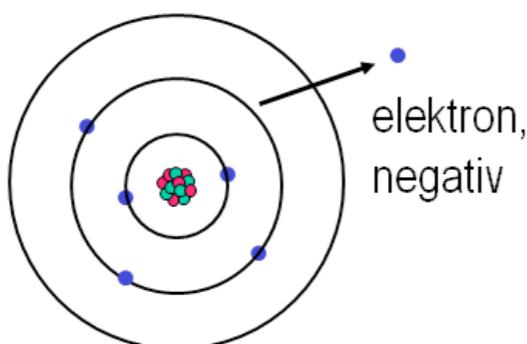
- Elektromagnetisk strålning, t.ex vid deexcitation



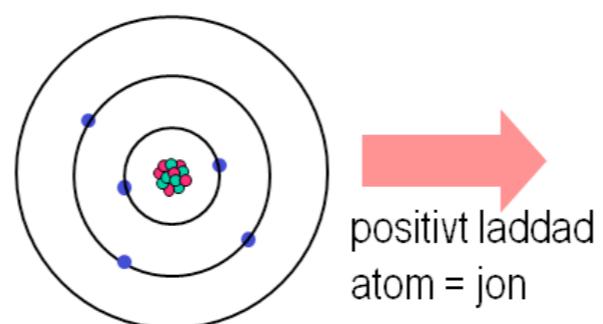
$e^- - \text{kärna}$



- Partikelstrålning vid ionisation

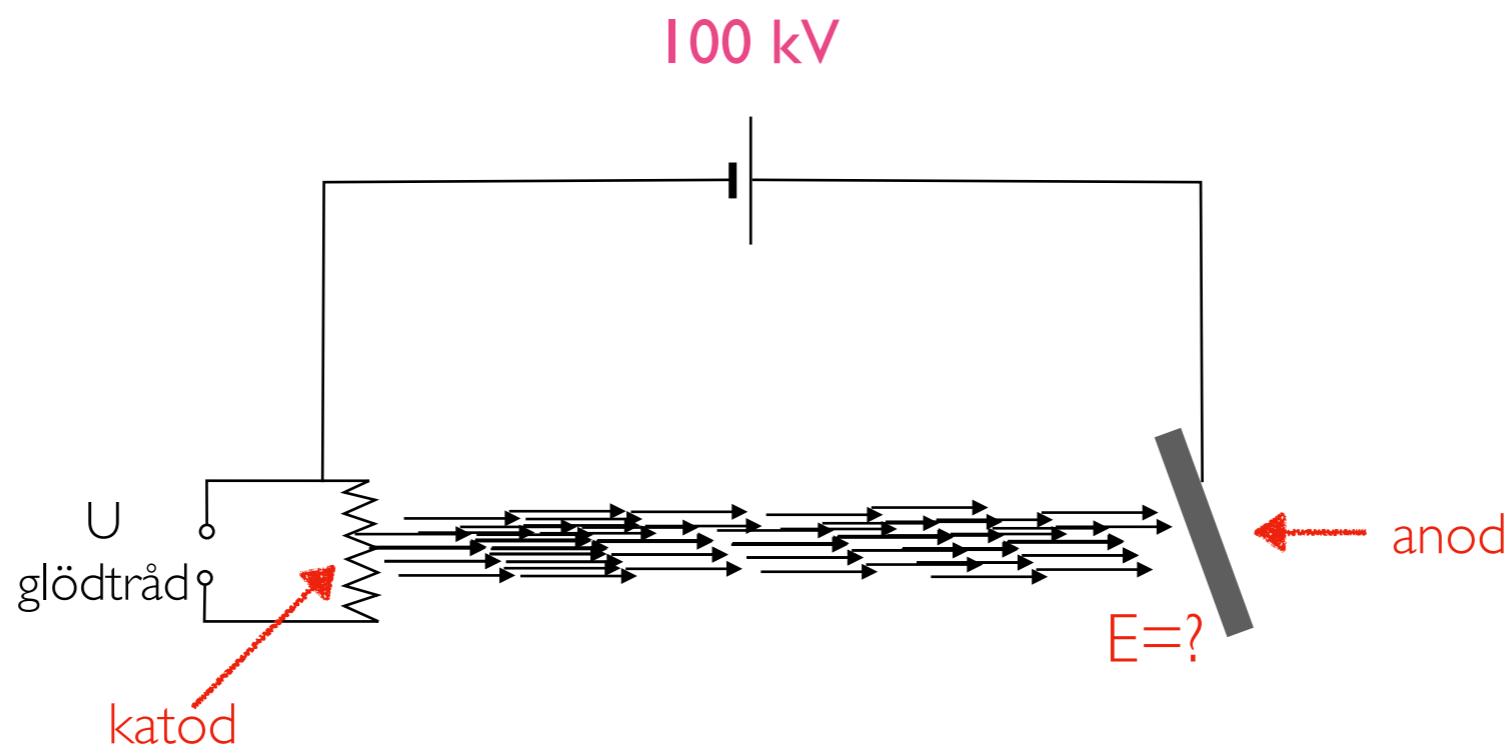


eller jonstrålning



Which of the following claims are true?

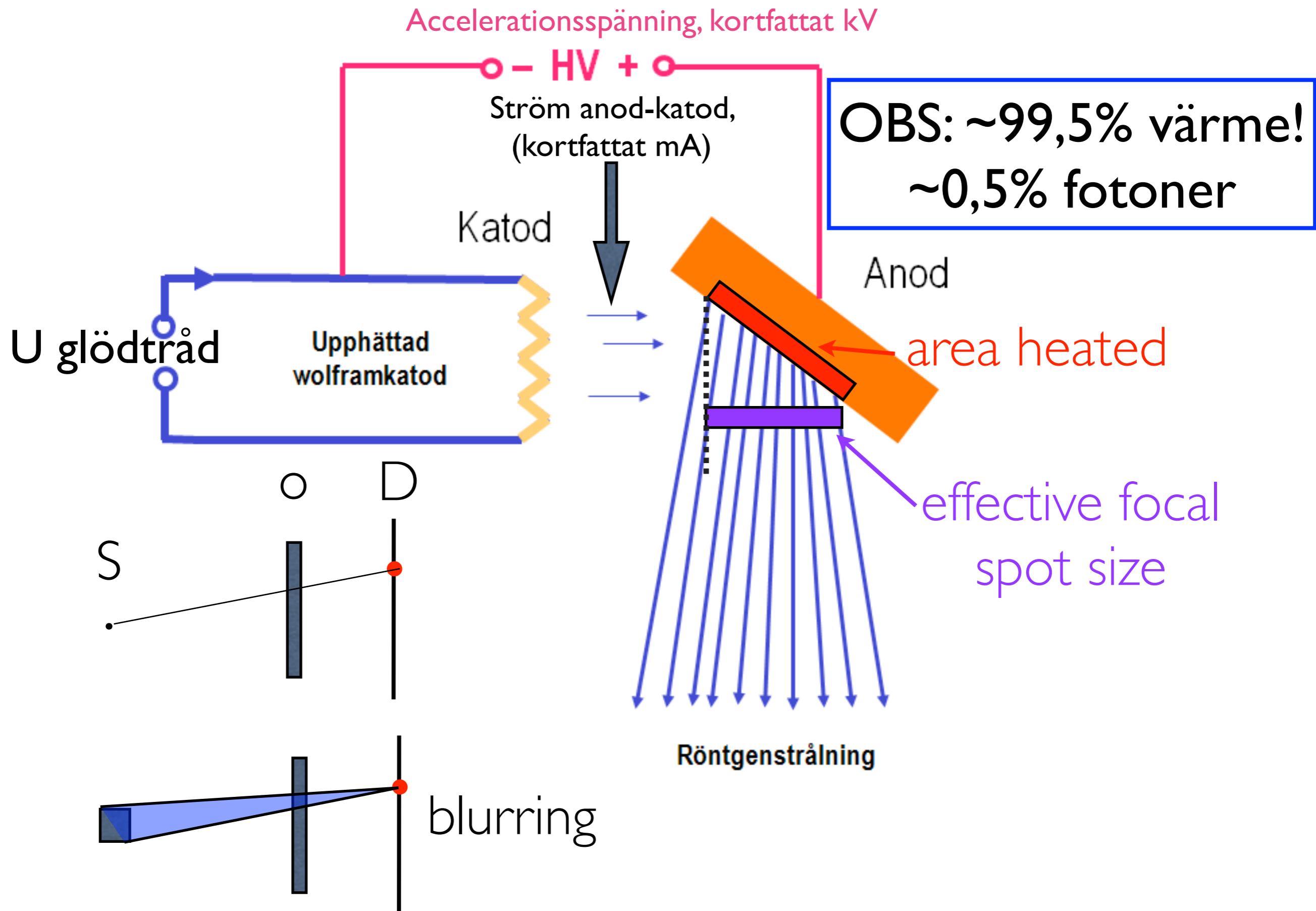
1. bremsstrahlung is an interaction between electrons
2. bremsstrahlung is an interaction between electrons and nuclei
3. Röntgen radiation (characteristic radiation) is a result of the interaction between 2 electrons, one bound to an atom
4. Röntgen radiation (characteristic radiation) is a result of the interaction between an electron and an atomic nucleus

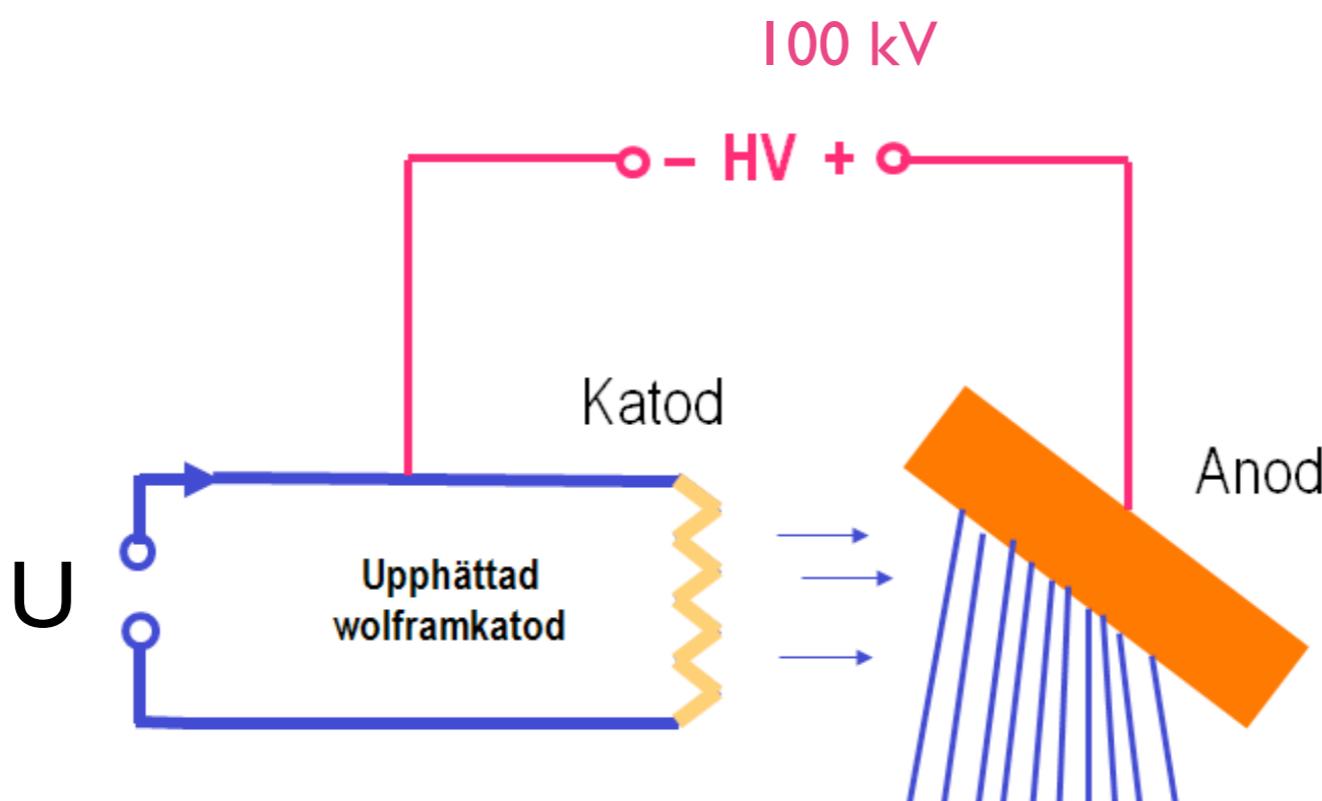


Suppose that the accelerating potential is 100 kV. Just before they hit the anode, the energy of the electrons emitted at the cathode is:

1. very high
2. anything between 0 and 100 keV
3. 100 keV
4. impossible to say, more information is needed

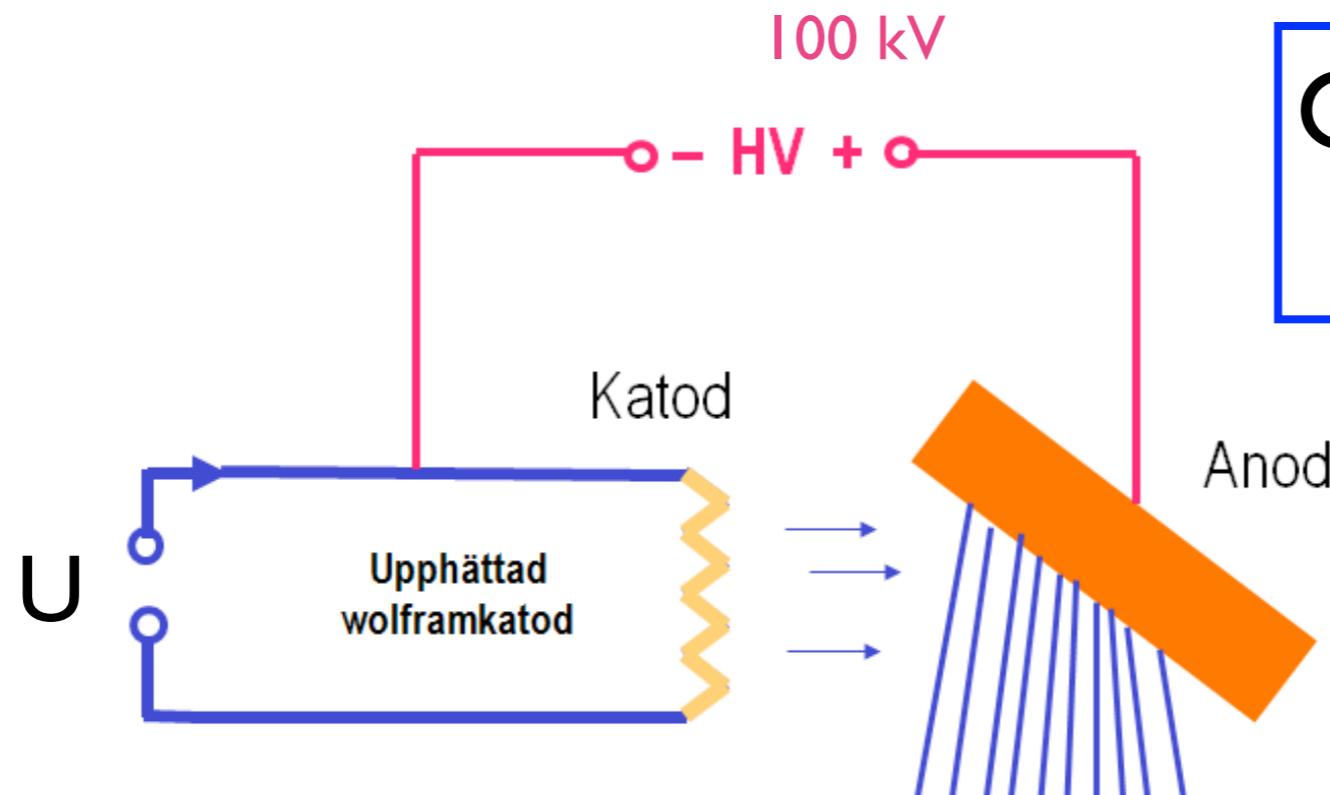
Röntgentränsförför focal spot size vs output:





Suppose that the tube is operated at 100 kV and 100 mA, while the filament voltage is 10V. The power dissipated in the anode is then:

1. ~9,95 kW
2. 10 kW
3. ~9,95 W
4. 10W
5. impossible to determine

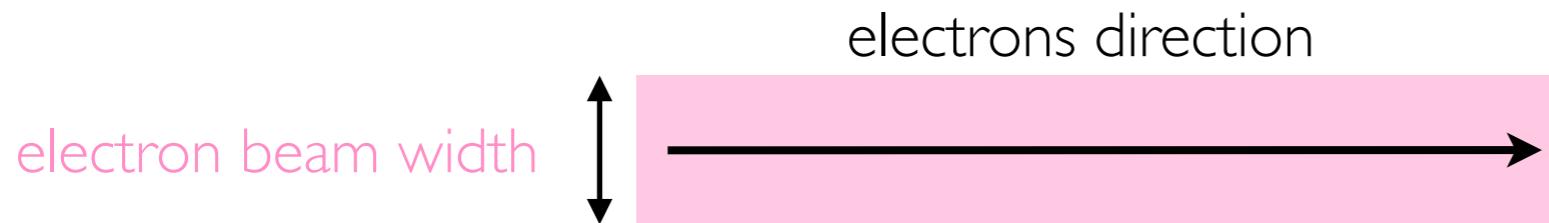


OBS: ~99,5% värme!
~0,5% fotoner

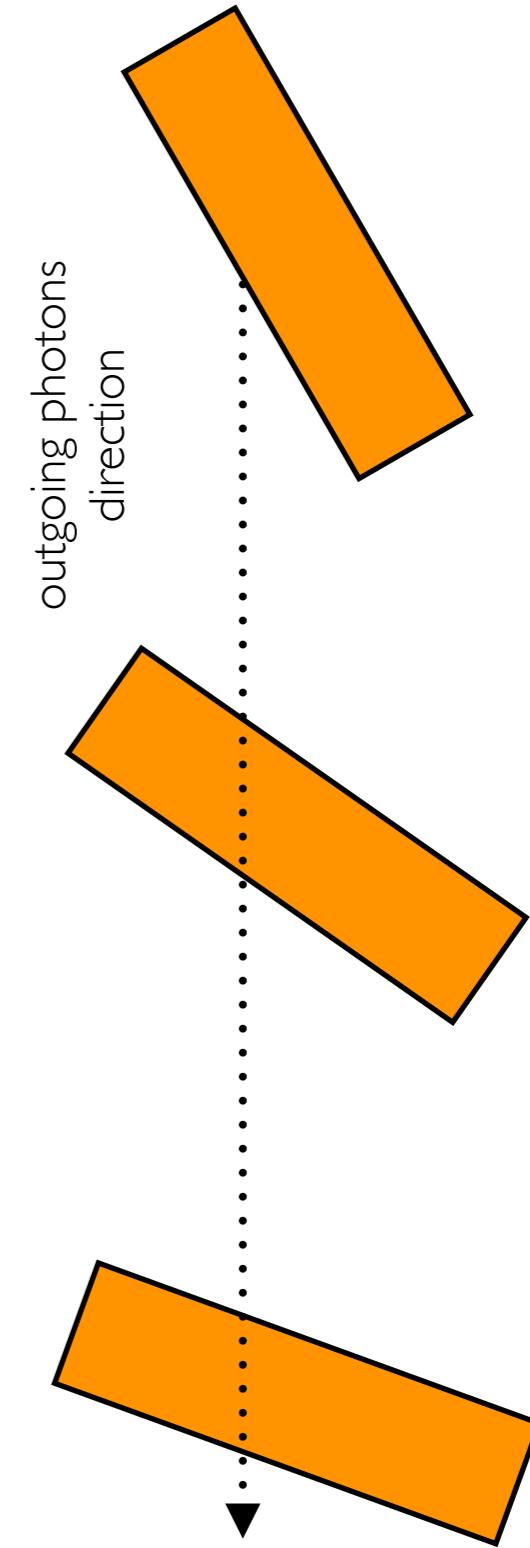
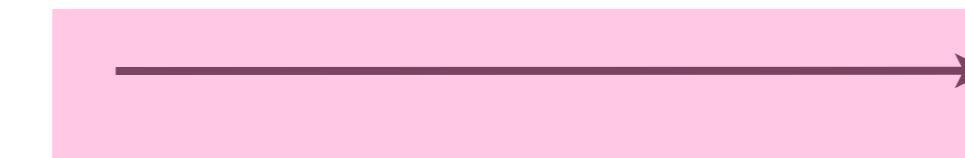
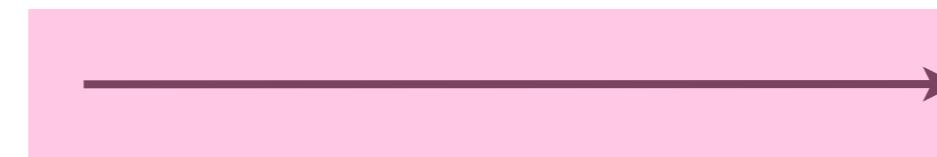
Suppose that the tube is operated at 100 kV and 100 mA, while the filament voltage is 10V. The power dissipated in the anode is then:

1. ~9,95 kW
2. 10 kW
3. ~9,95 W
4. 10W
5. impossible to determine

Which positioning of the anode will minimise the effective focal spot area while increasing the area over which heat is delivered?



cathode side

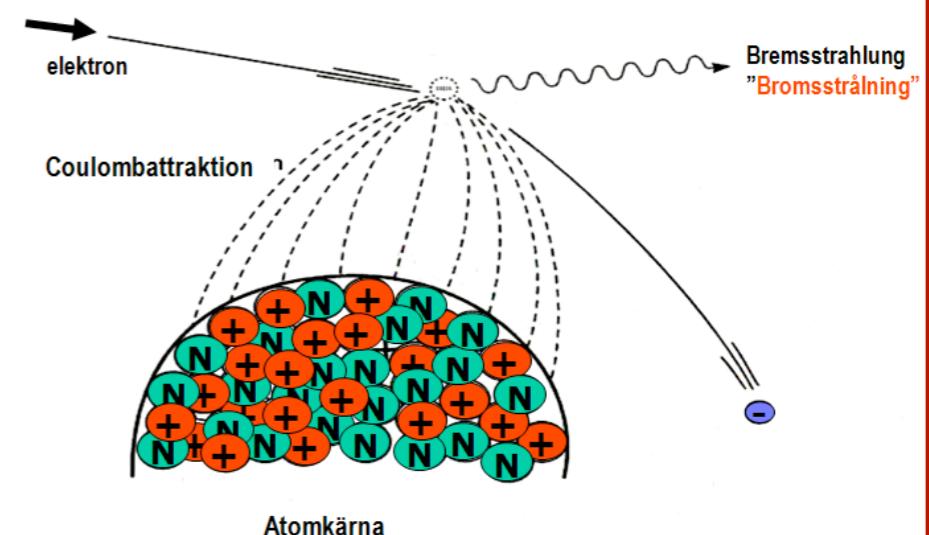
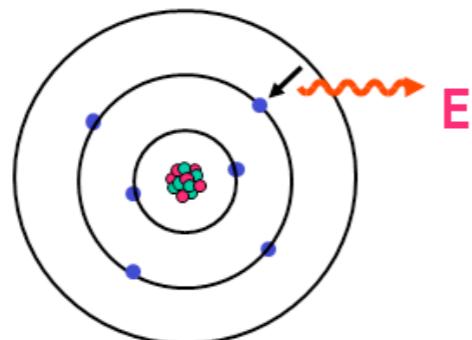


Vad händer i anoden?

$e^- - e^-$

$e^- - \text{kärna}$

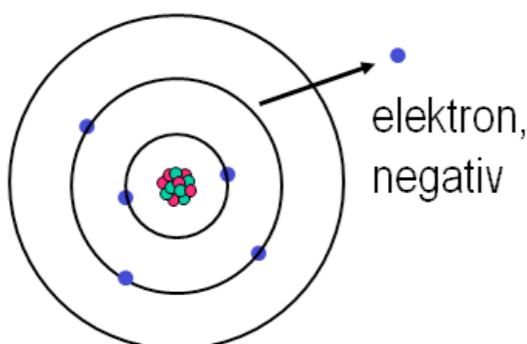
- Elektromagnetisk strålning, t.ex vid deexcitation



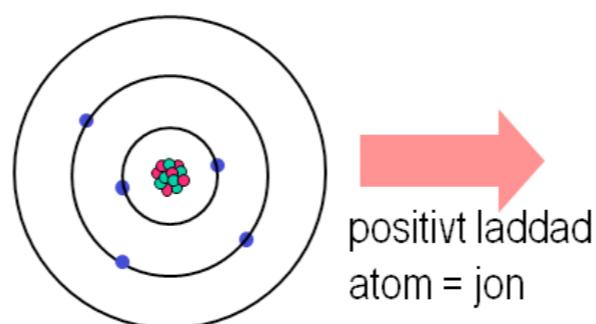
fotoner

2 mekanismer bidrar till röntgenspektrum

- Partikelstrålning vid ionisation



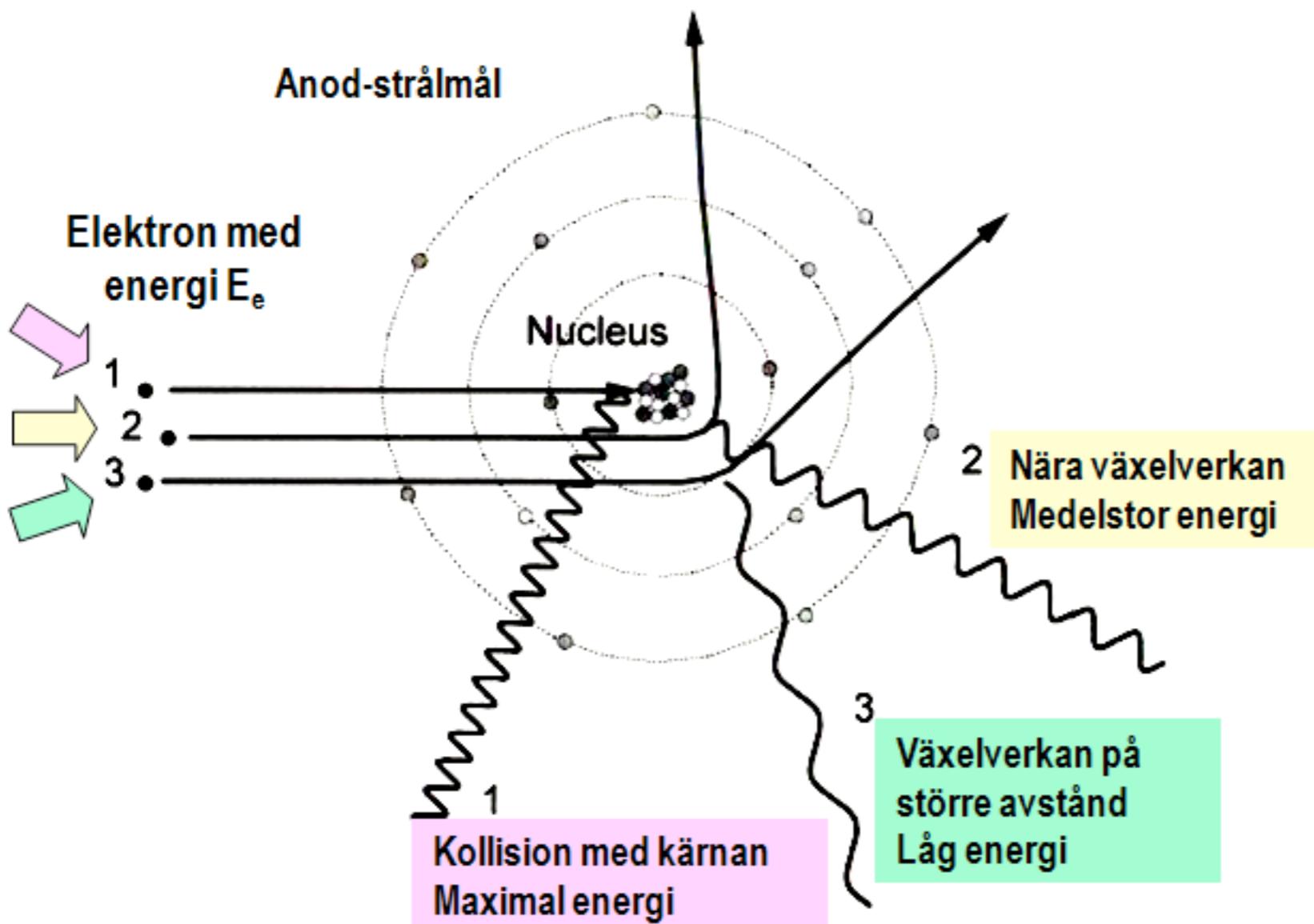
eller jonstrålning



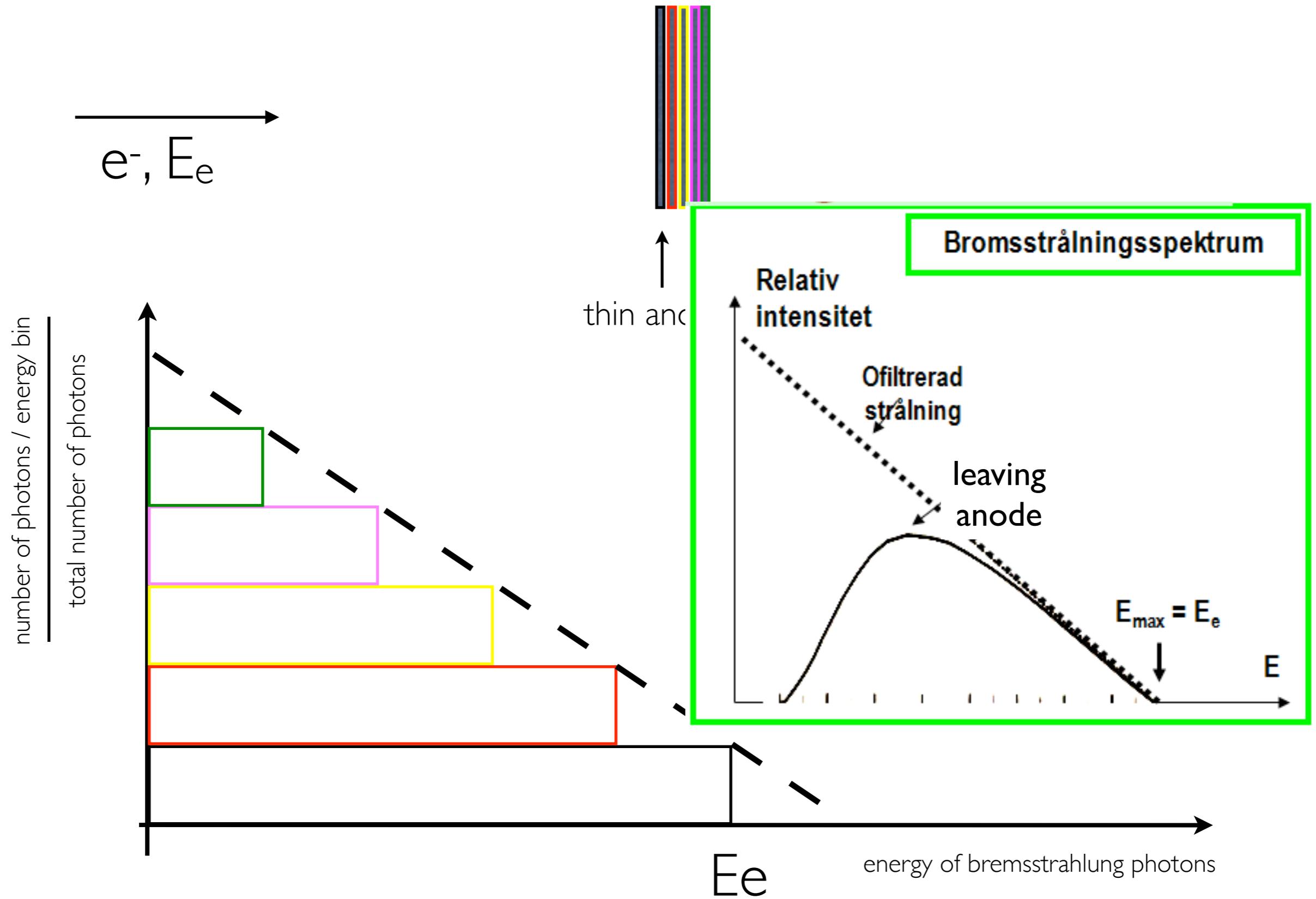
laddade partiklar

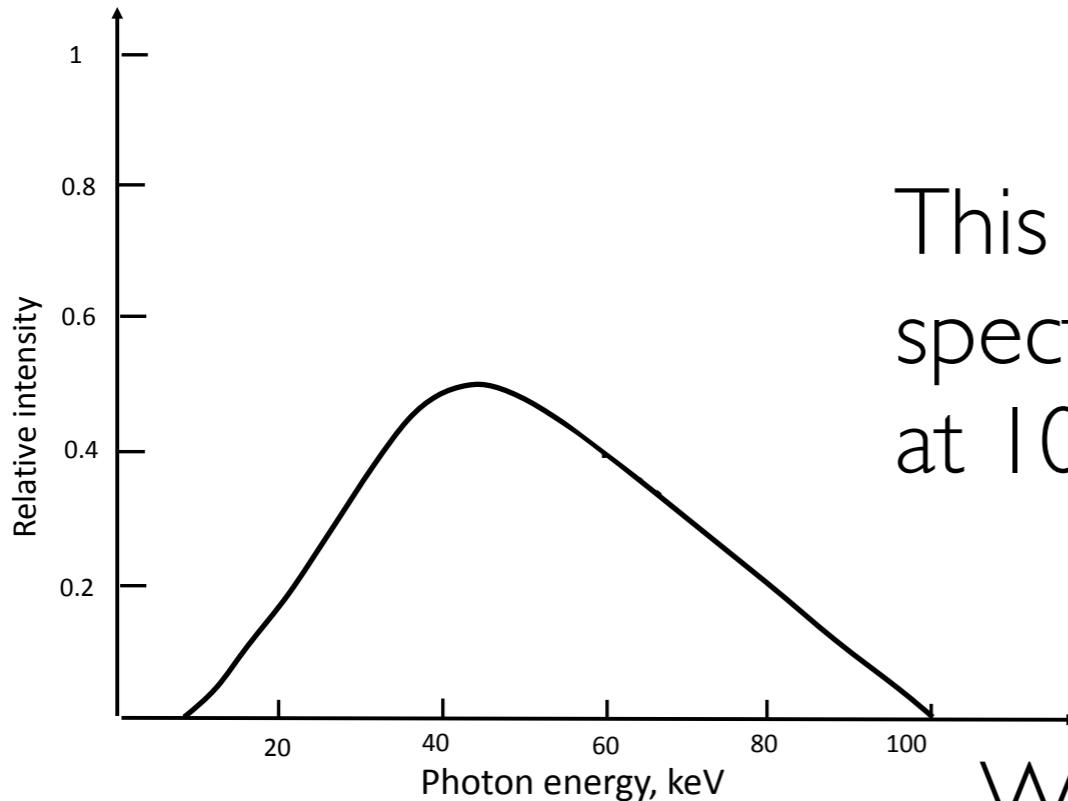
Bromsstrålning

- Bromsstrålningens energifördelning är kontinuerlig
- Maxenergin är lika med elektronens energi
- Den är samma som accelerationsspänningen ggr e-laddning

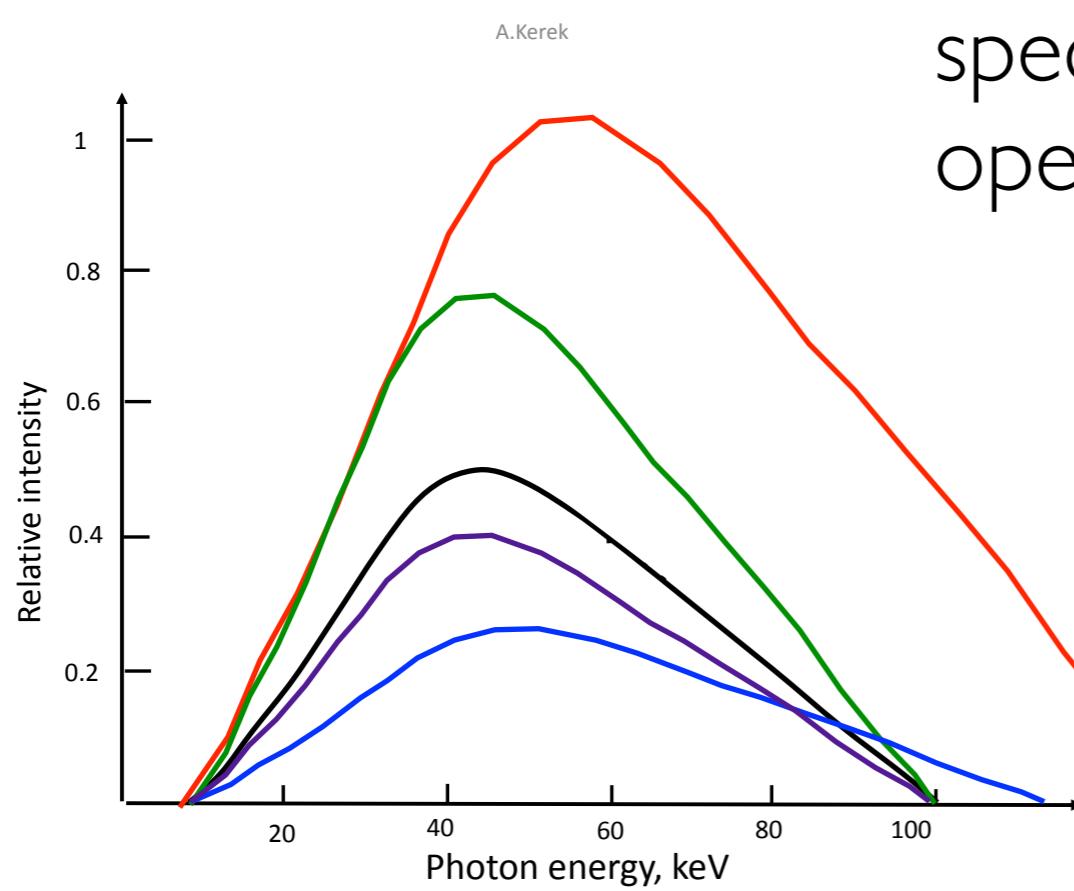


Unfiltered spectrum:





This is the continuous part of the spectrum from an x-ray tube operated at 100 kV and 100 mA



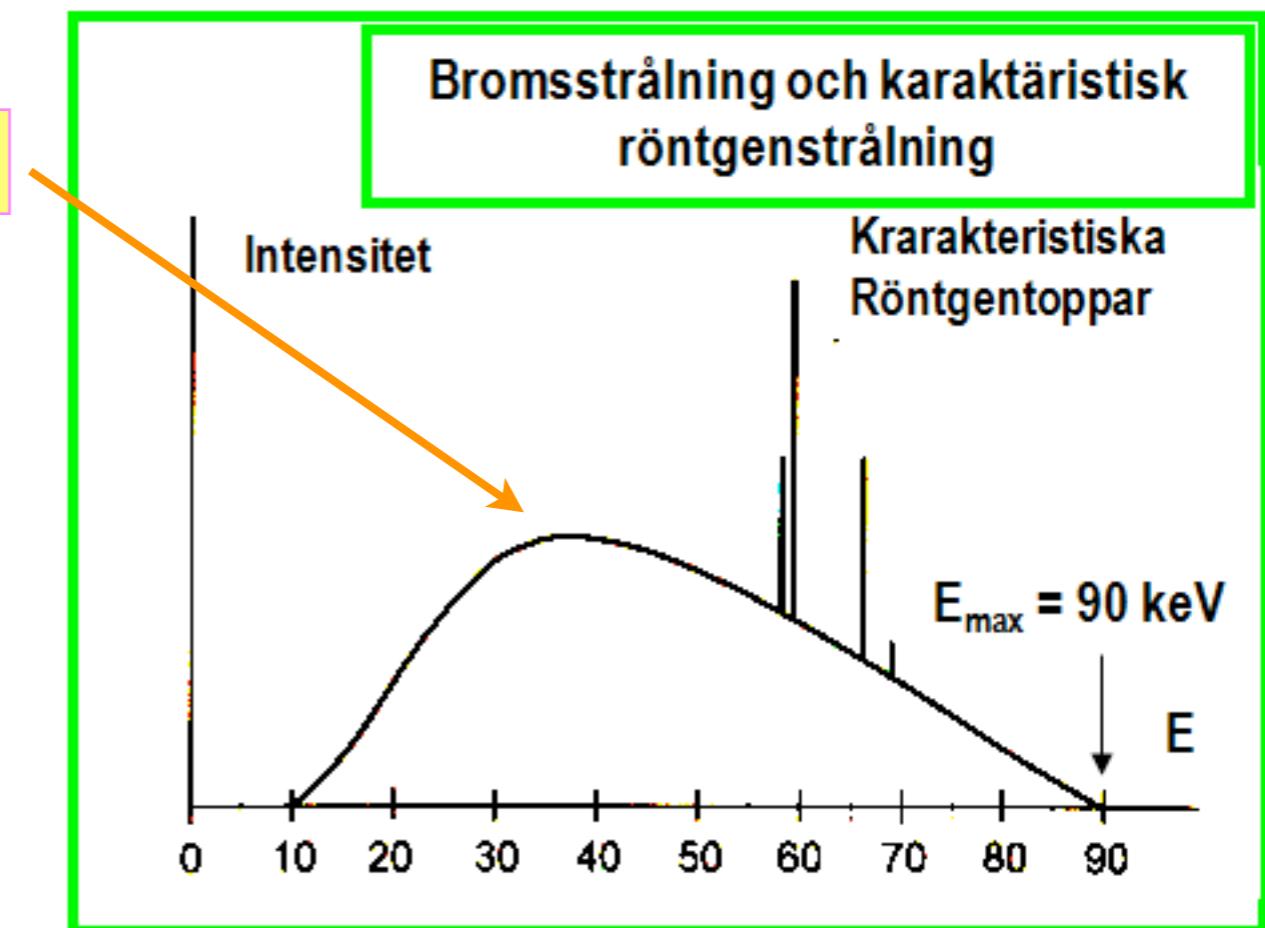
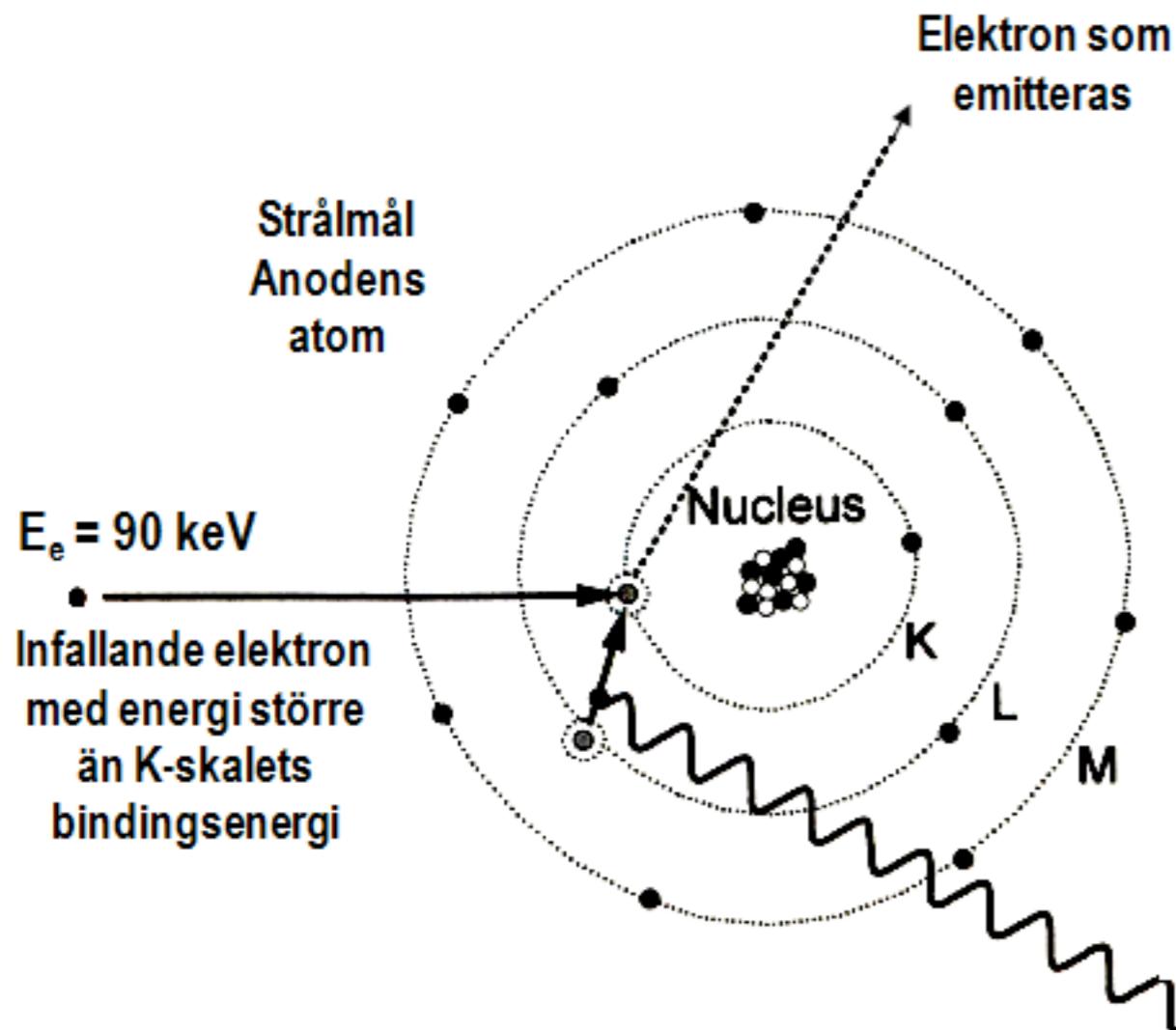
Which line represent the continuous spectrum from the same tube operated at 100 kV and 150 mA?

-
-
-
-

Röntgenstrålning och bromsstrålning

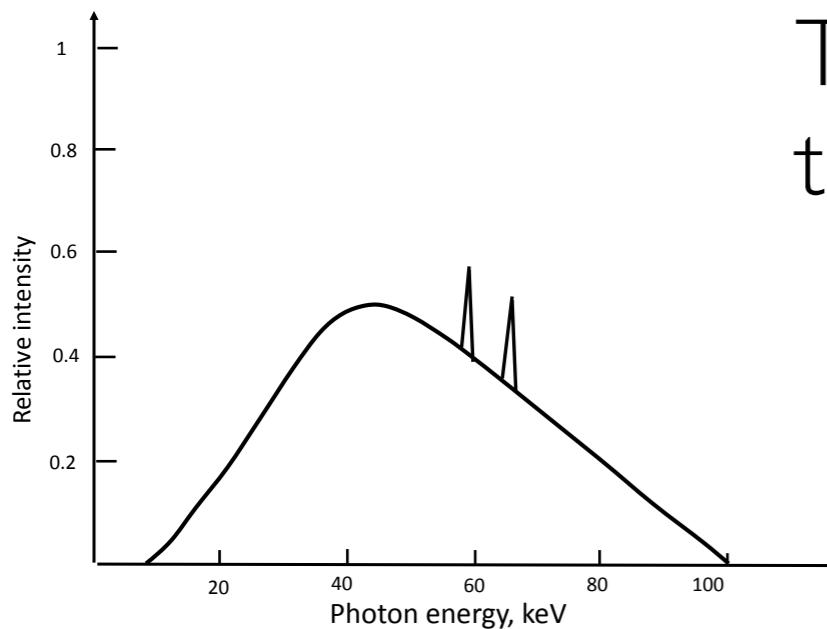
- Om elektronernas energi är tillräcklig kan de slå ut elektroner från anodens atomer. En foton med karakteristisk Röntgenenergi emitteras.
- Dessa kan observeras överlagrade bromsstrålsspektrat

OBS: max intensitet @ 1/3-1/2 av E_{max}

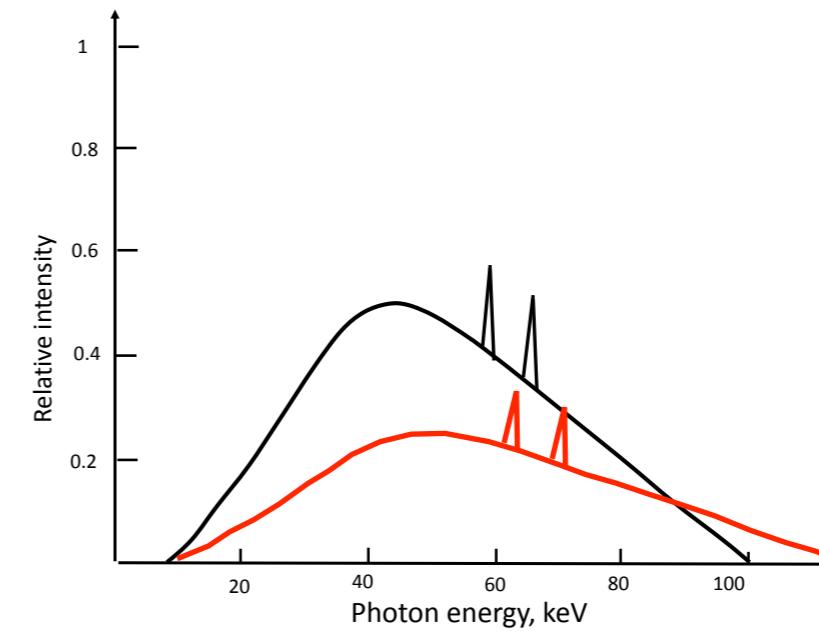
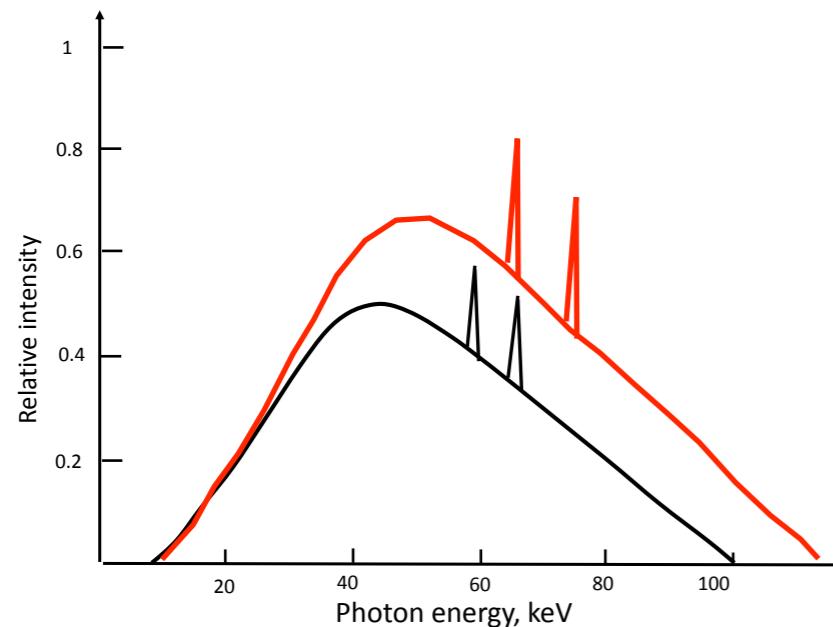
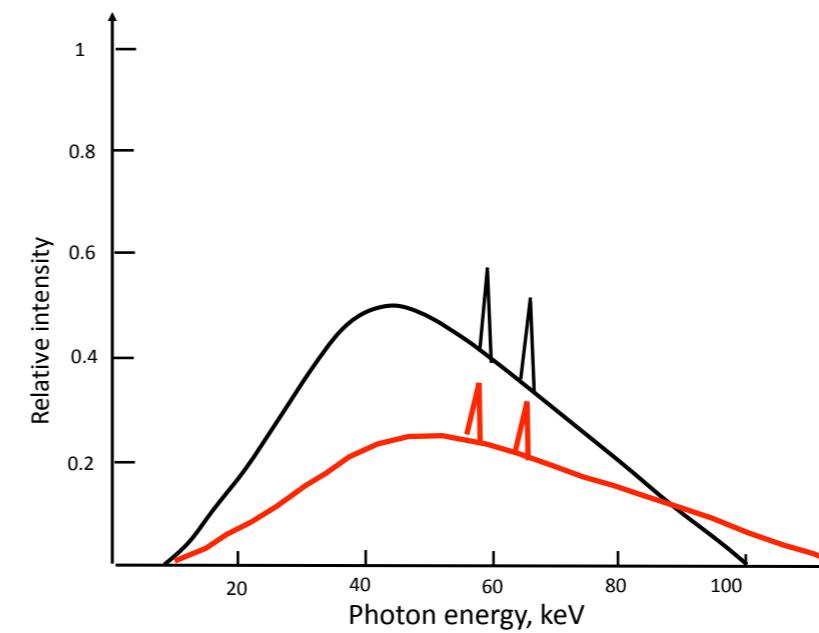
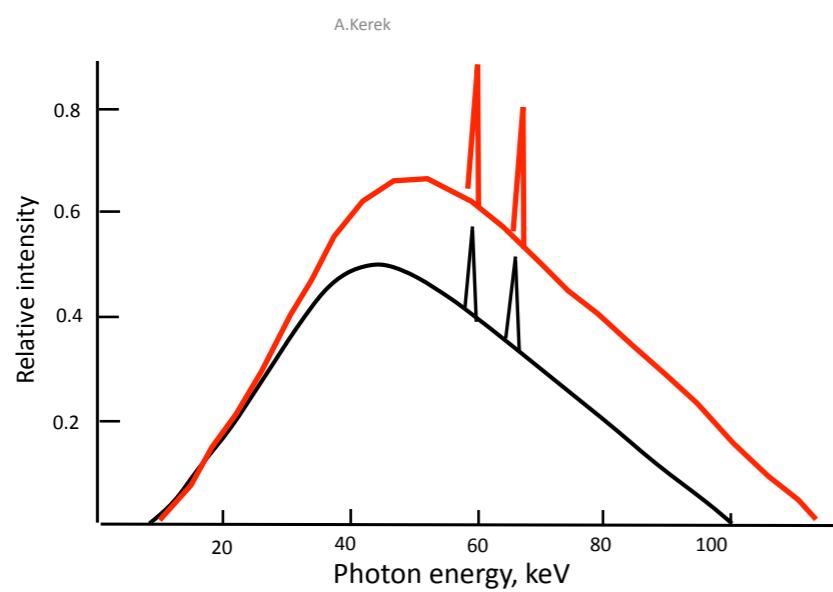


Karakteristisk
Röntgen övergång
från K → L skal

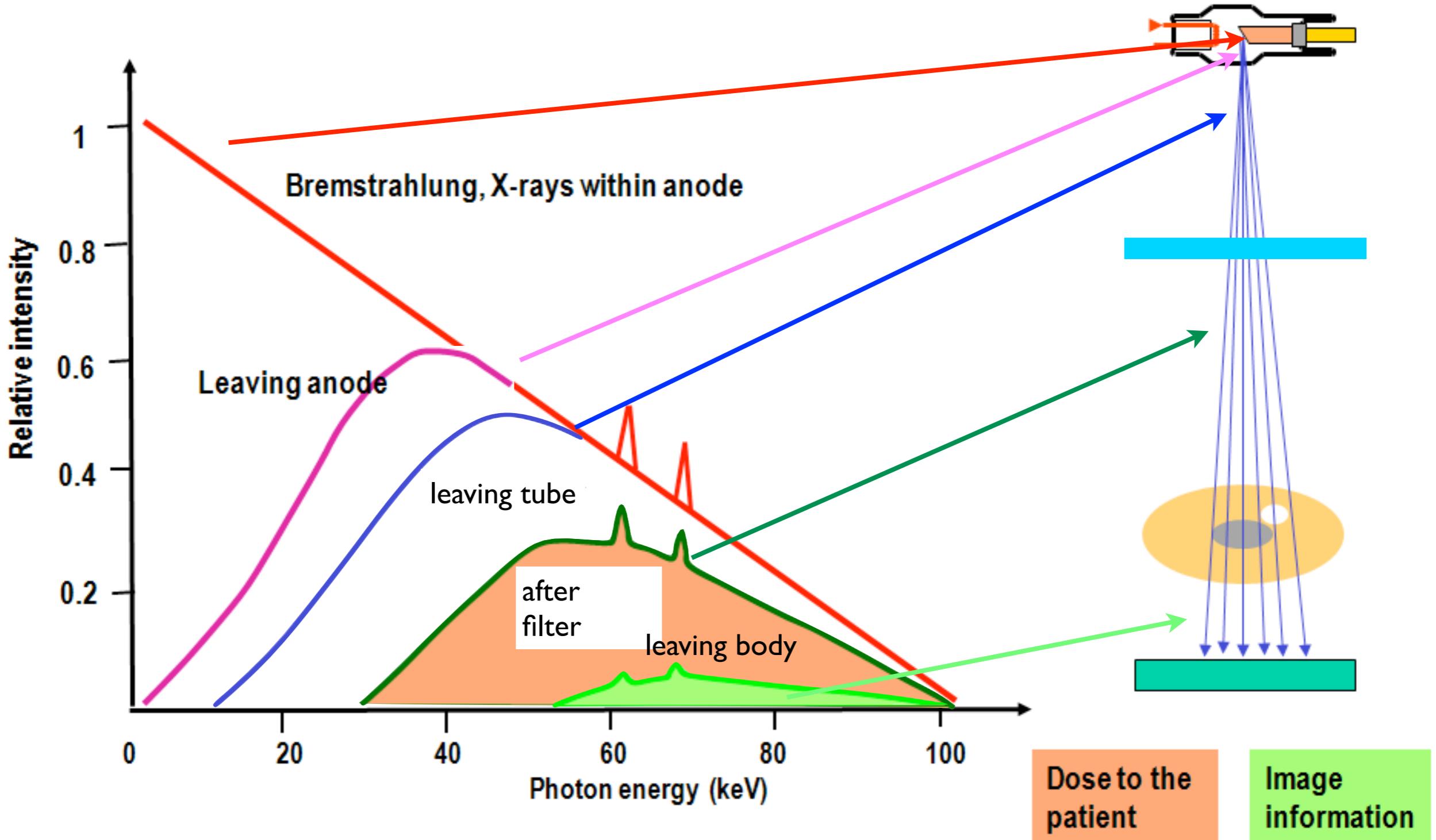
This is the spectrum from an x-ray tube operated at 100 kV and 100 mA

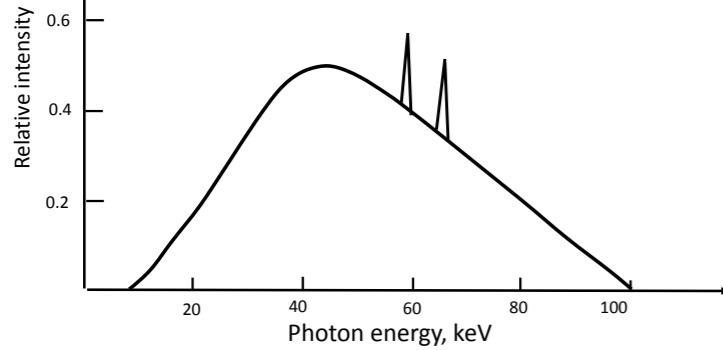


The tube voltage is increased while the current is kept constant. Which of the following spectra will be obtained?

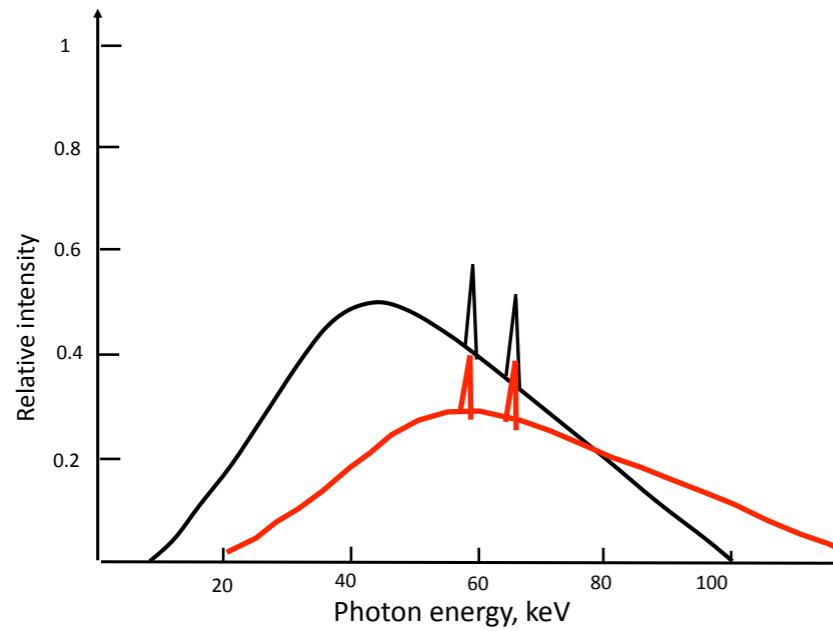
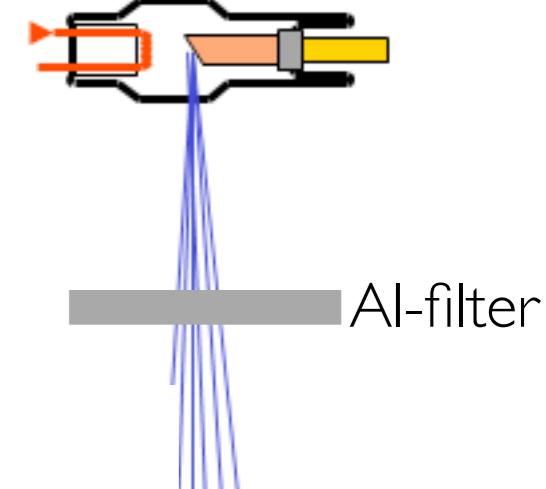


Beam hardening - filters

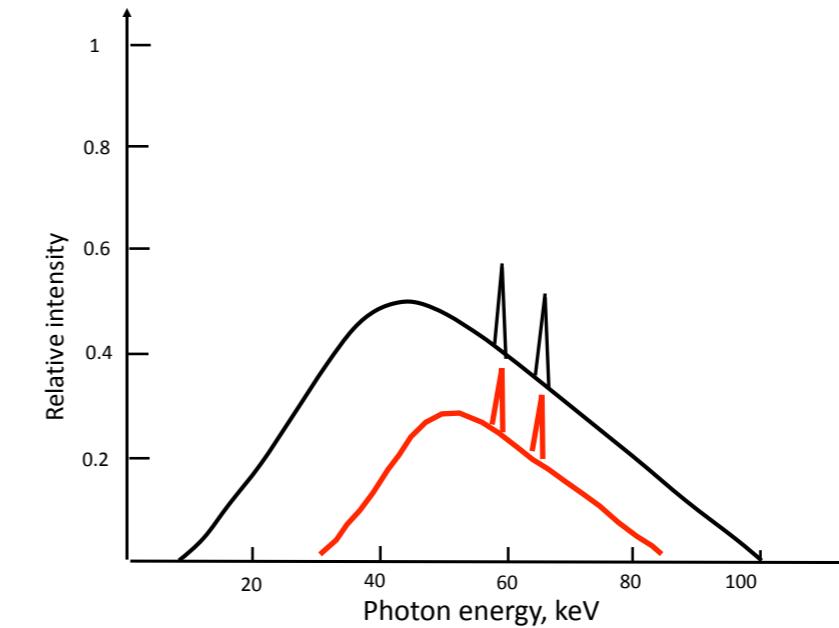




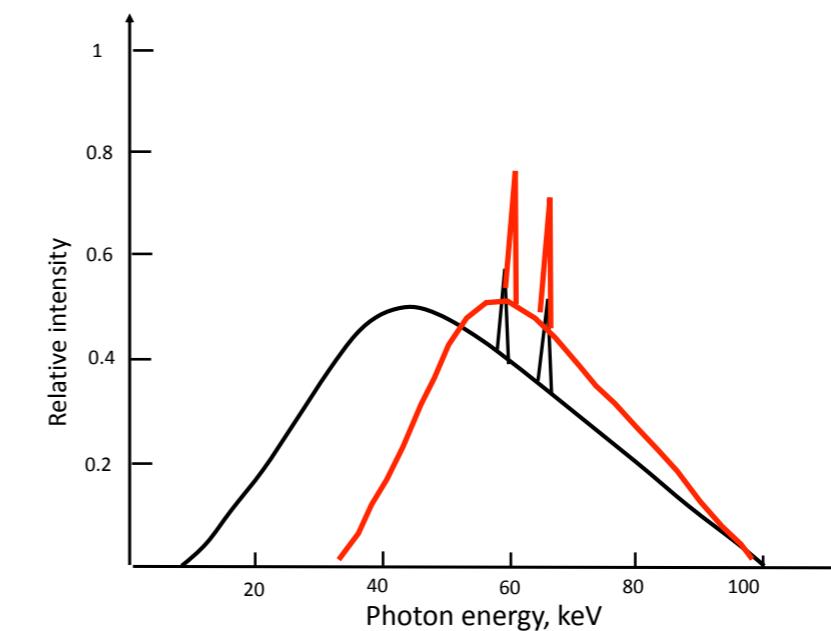
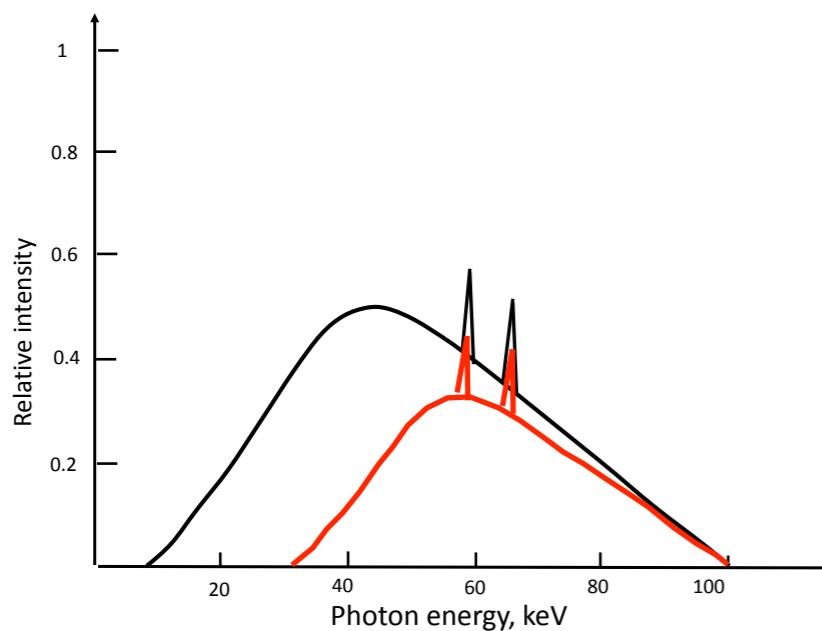
On the left you see the spectrum of x-rays leaving an x-ray tube. Which of the red spectra would possibly represent the spectrum after an Al-filter? The original spectrum is reported in black in all plots.

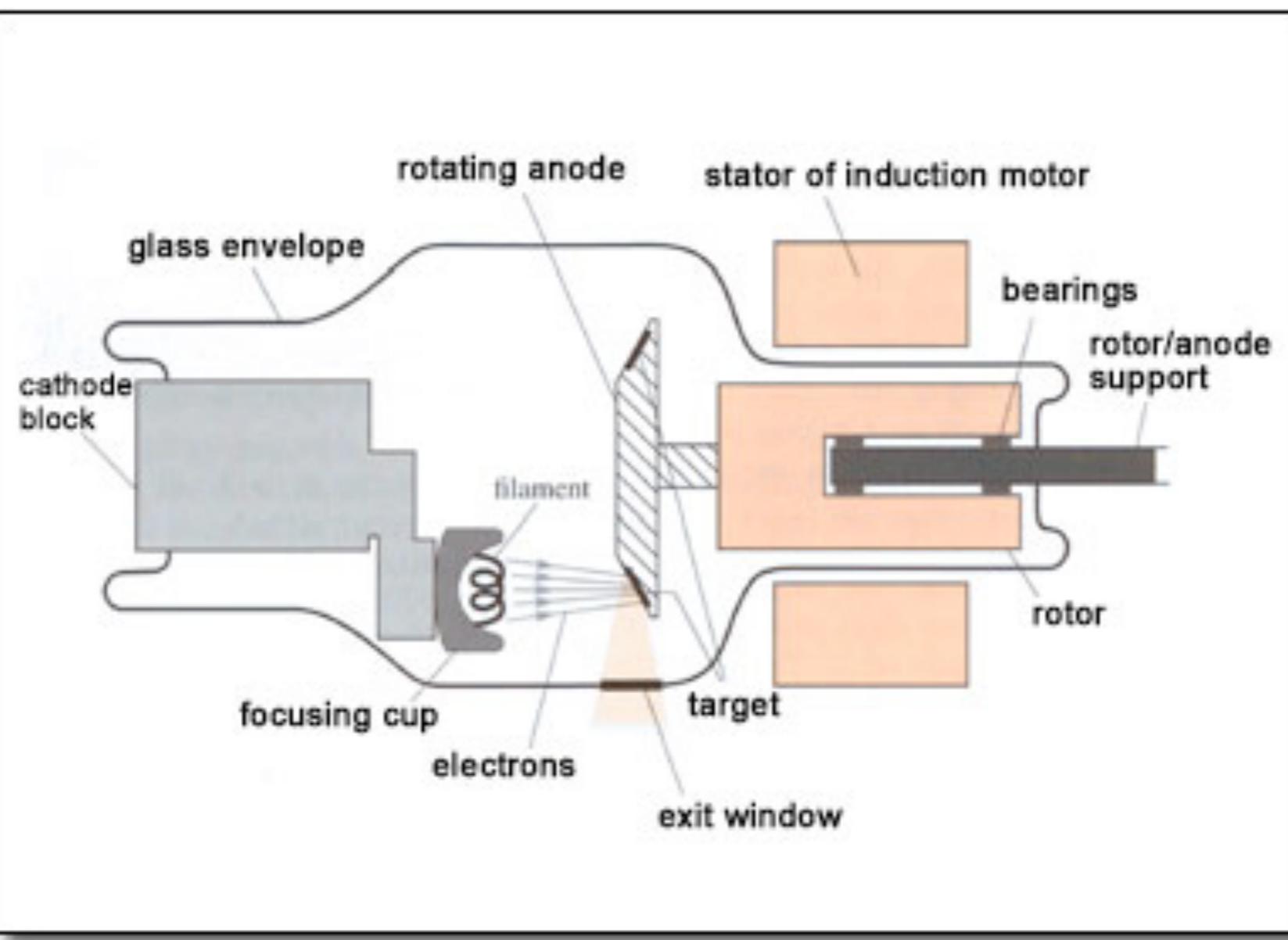


A.Karak



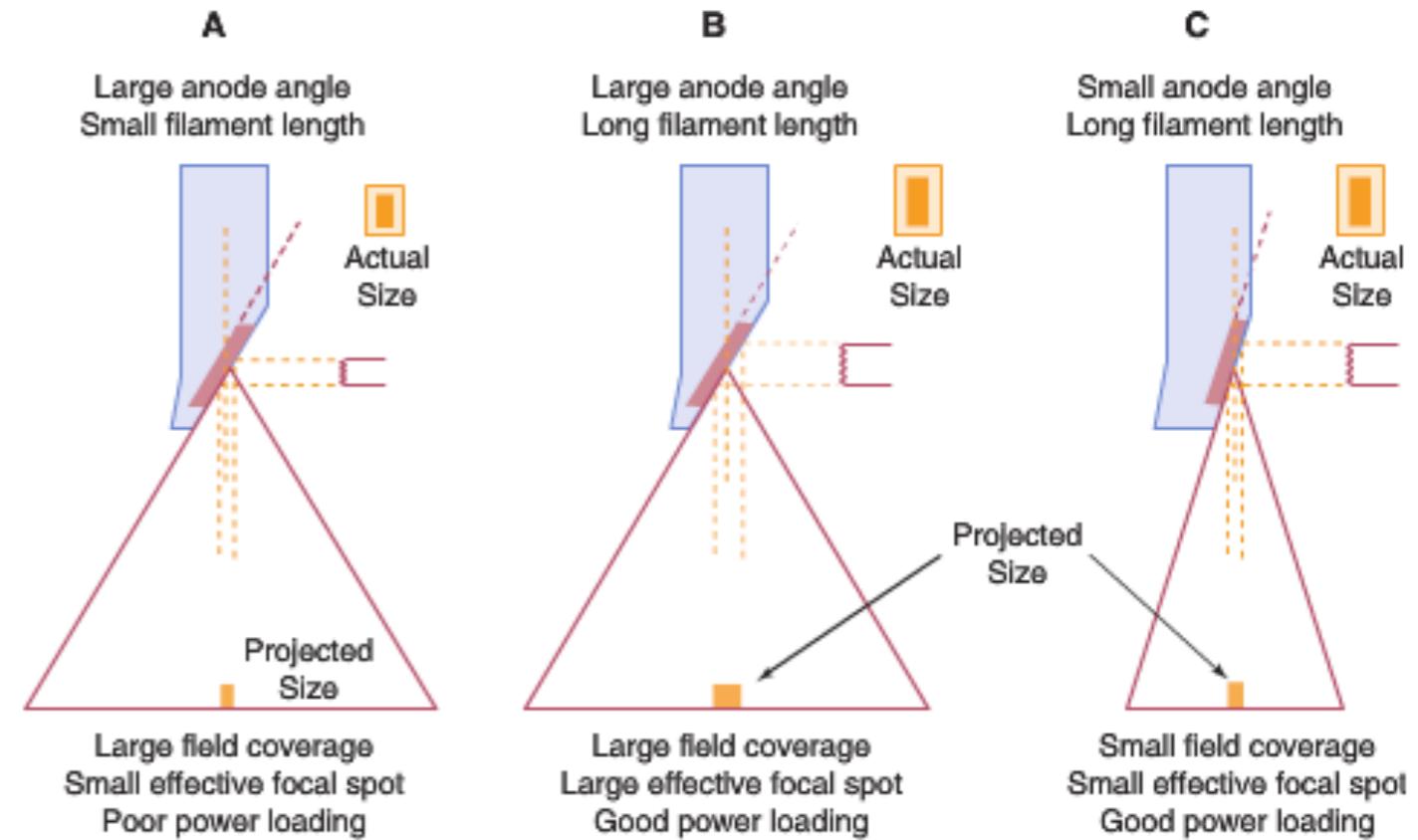
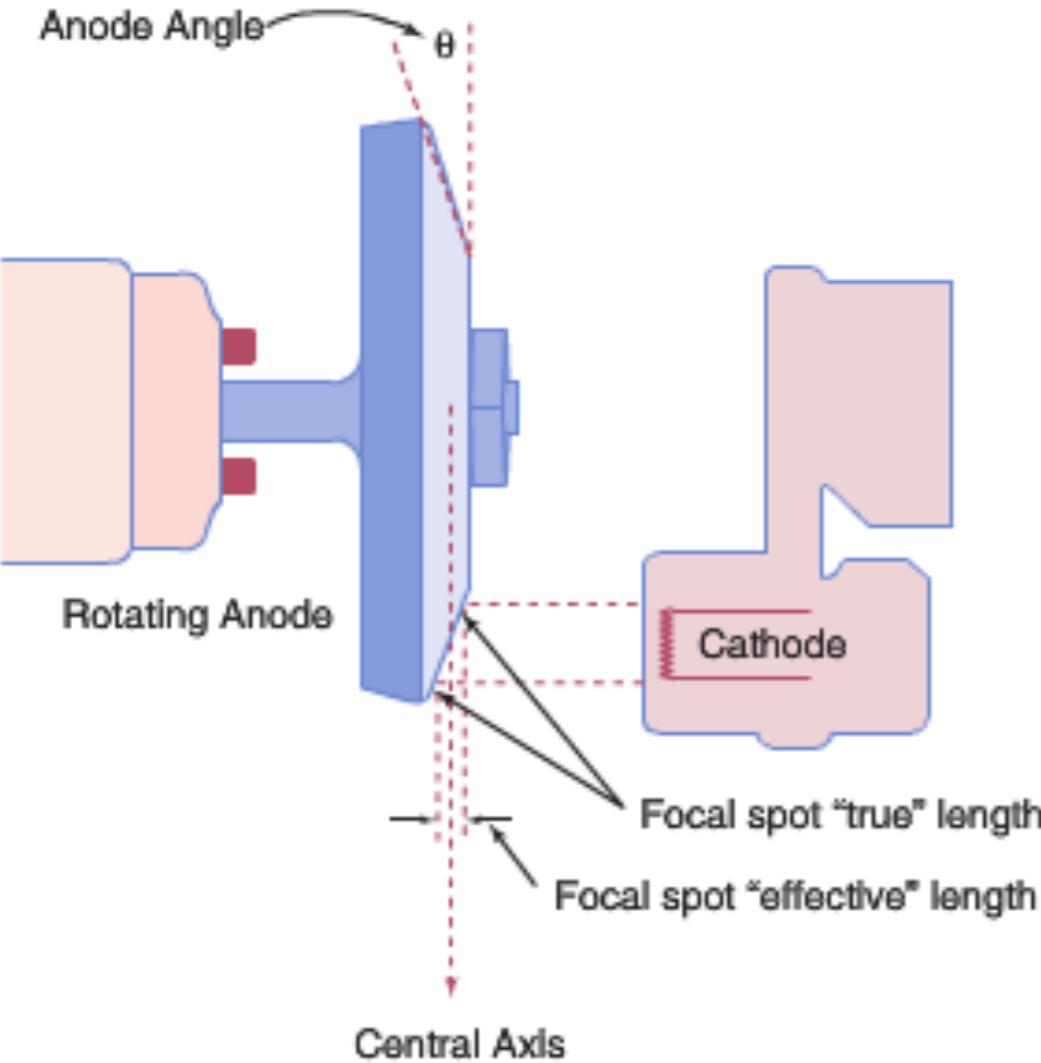
A.Kerek





focal spot

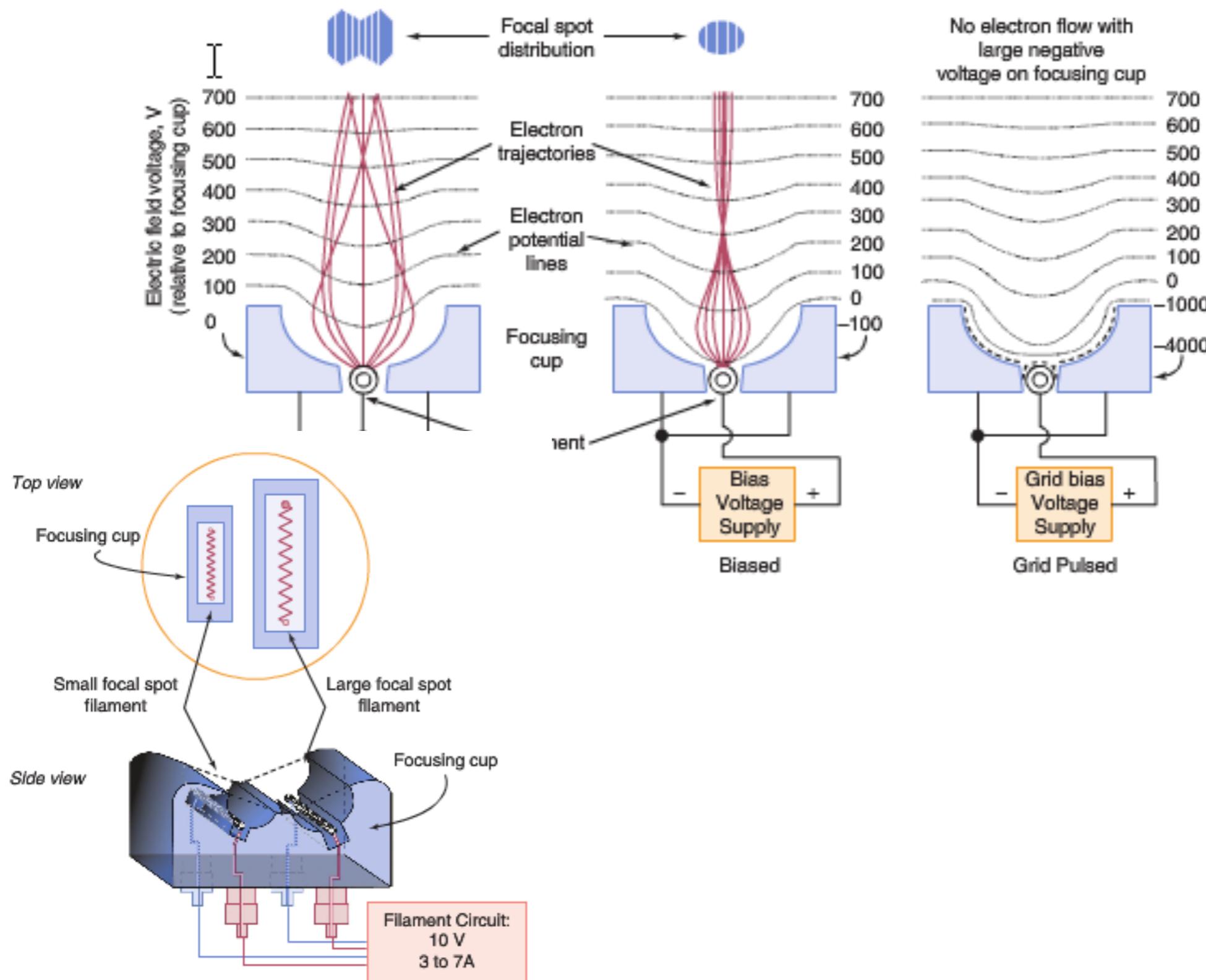
Side view of anode and cathode



anode angle

filament length

focusing cup



Snabb diskussion (grupper 2-3):

1. Vad beror den kontinuerliga bromssstrålnings spektrum på?

2. Vad beror de karaktäristiska röntgentoppar på?

Snabb diskussion (grupper 2-3):

1. Vad beror den kontinuerliga bromsstrålnings spektrum på?

accel. spänning (kortfatatt kV) och
glödtrådsspänning => mA!

2. Vad beror de karakteristiska röntgentoppar på?

material i anoden => Z

Detectors for radiography

X-ray detectors

1. basic principles of radiation detection, classification of detectors
2. sensitivity of a detector: detected photons, emitted photons, activity and count rate
3. sensitivity of a detector: geometric and intrinsic efficiency
4. common kinds of x-ray detectors



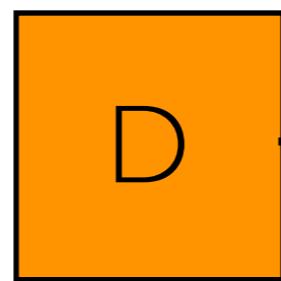
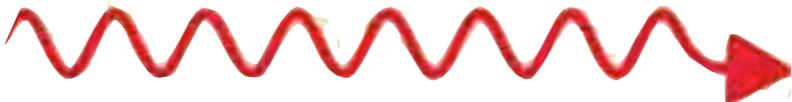
20 - 150 keV

Lessons to learn:

1. avoid Compton in patient and detector!
2. detector should absorb ~100% x-rays going through patient

Detector for ionising radiation: basic principles

photon $E > 100$ eV



“visible” output
(usually electric signal)

x- or gamma-rays

photon counting

to

current,
voltage

each photon is counted independently

sum all photons in time interval

current mode

transmission today!

Barn kastar pappersflygplan i klassrummet under en viss tid. Jag hittar 3 i min “detektorkorg”.



Hur många pappersflygplan har kastats under tiden?

- 1. ≤ 3
- 2. 3
- 3. ≥ 3

Om du i framtiden ville uppskatta antal kastade från de som hamnar i korgen, vad skulle du göra?

Detector efficiency (effektivitet):

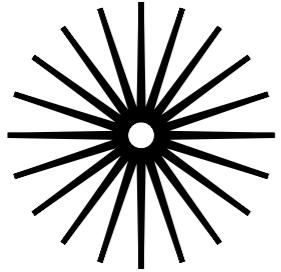
geometry (solid angle) & “intrinsic” efficiency

before that:

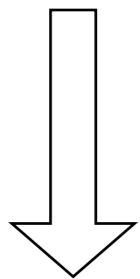
difference between activity (decay/s),
emitted photons and
detected photons
count rate

detection efficiency

S



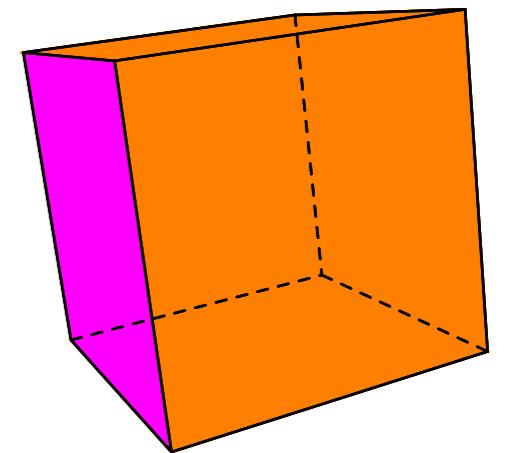
$$A = 1 \text{ kBq}$$

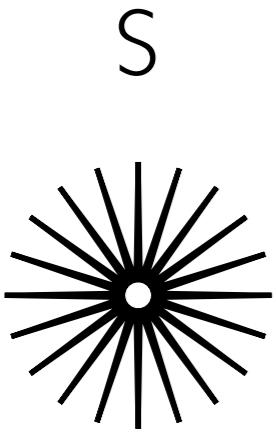


1000 decays/s

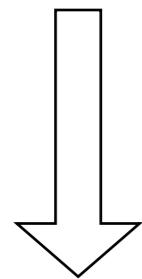
does this imply
that 1000
photons/s are
emitted?

D



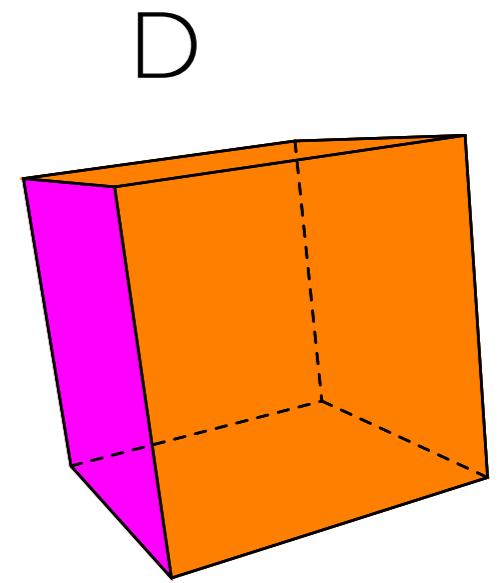


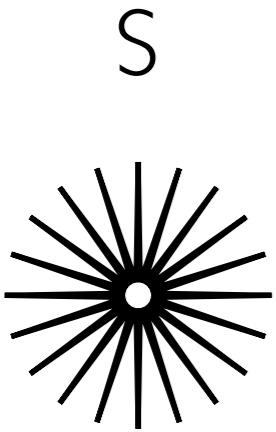
$$A = 1 \text{ kBq}$$



1000 decays/s

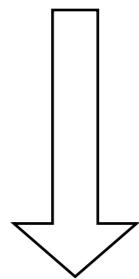
of emitted
photons depends
on decay
scheme!





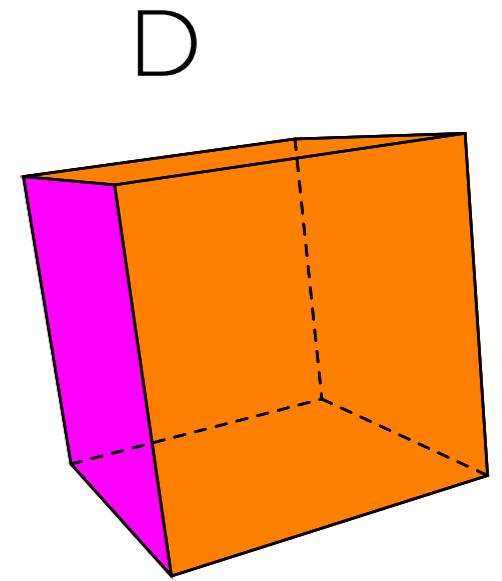
S

$$A = 1 \text{ kBq}$$

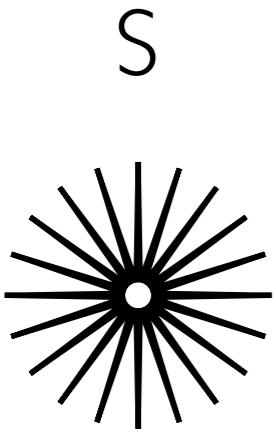


1000 decays/s

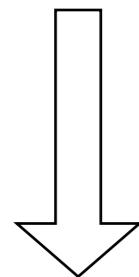
of emitted
photons depends
on decay
scheme!



of detected
photons?

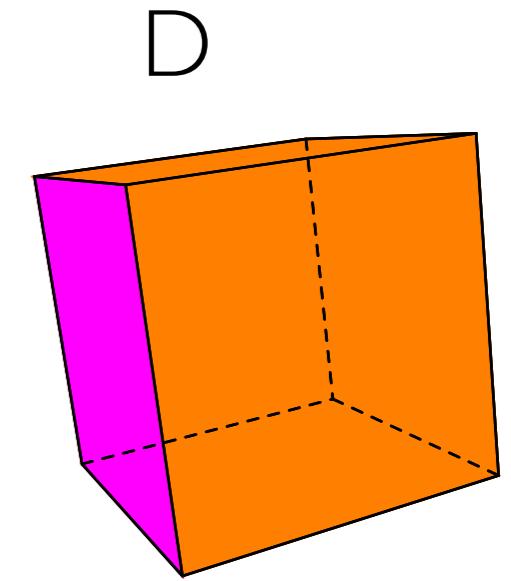


$A = 1 \text{ kBq}$



1000 decays/s

of emitted
photons depends
on decay
scheme!

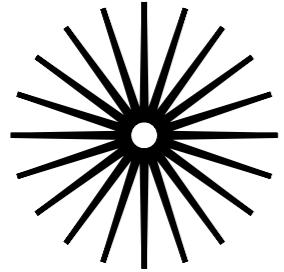


of detected
photons?

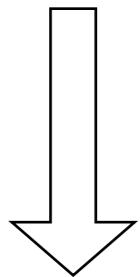
efficiency:

$$\frac{\text{\# detected photons}}{\text{\# emitted photons}}$$

S

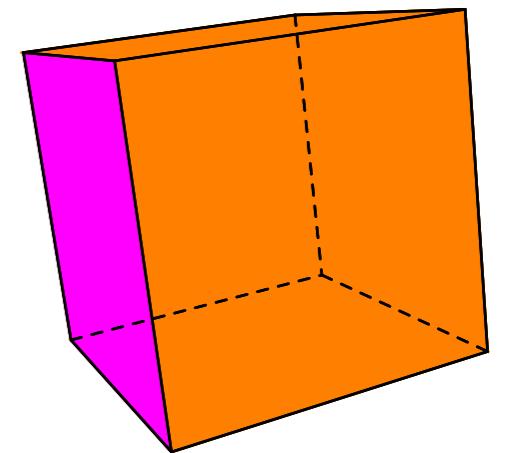


$$A = 1 \text{ kBq}$$

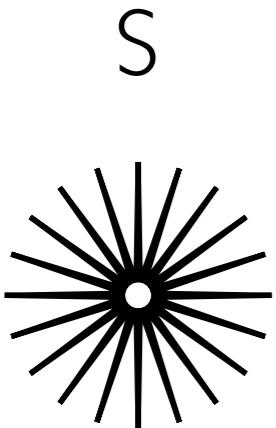


does this imply
that 1000
photons/s are
emitted?

D

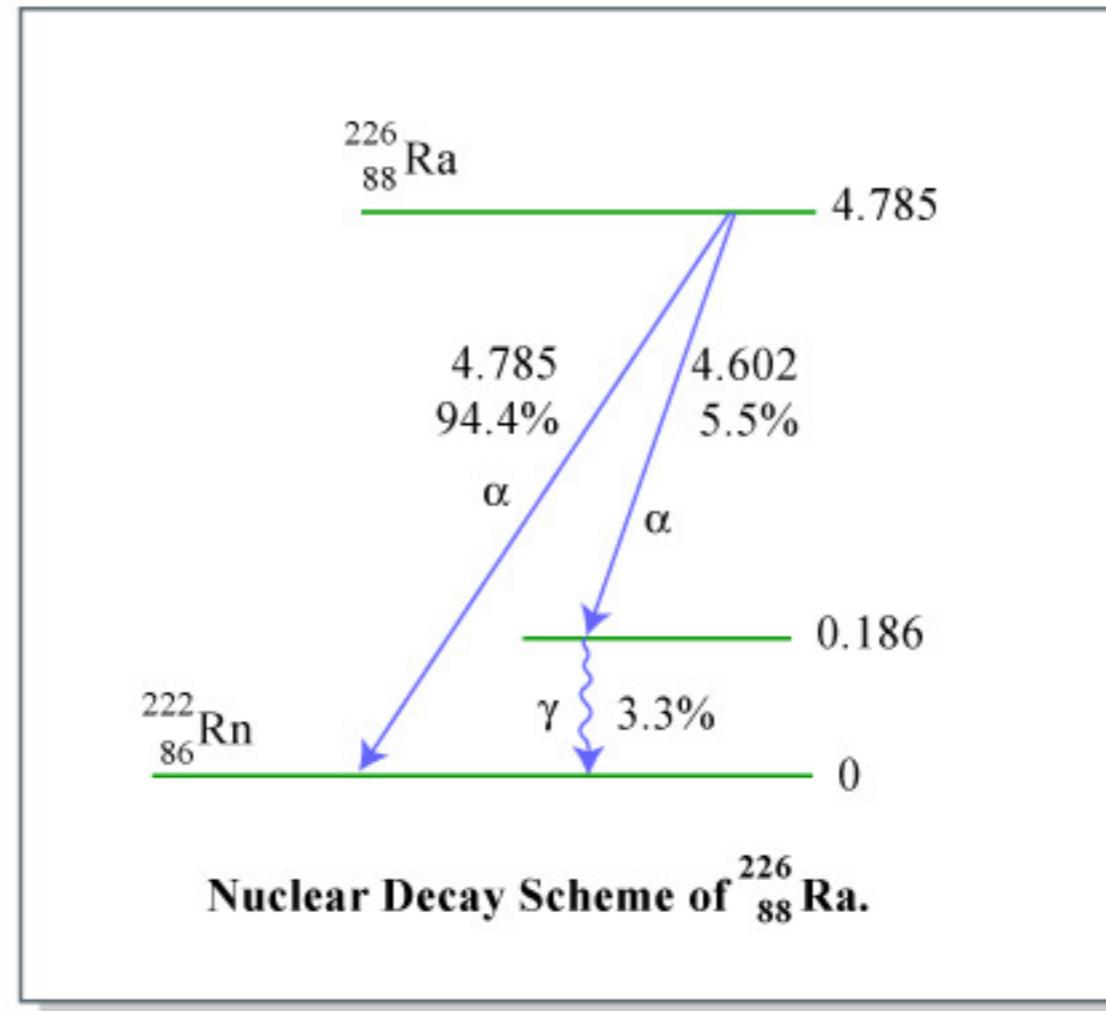
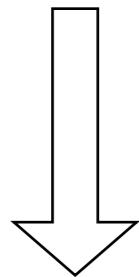


1000 decays/s

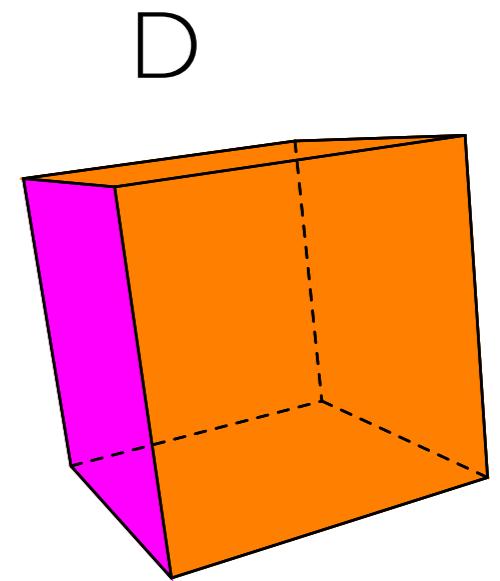


S

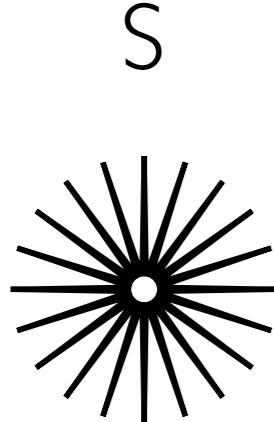
$$A = 1 \text{ kBq}$$



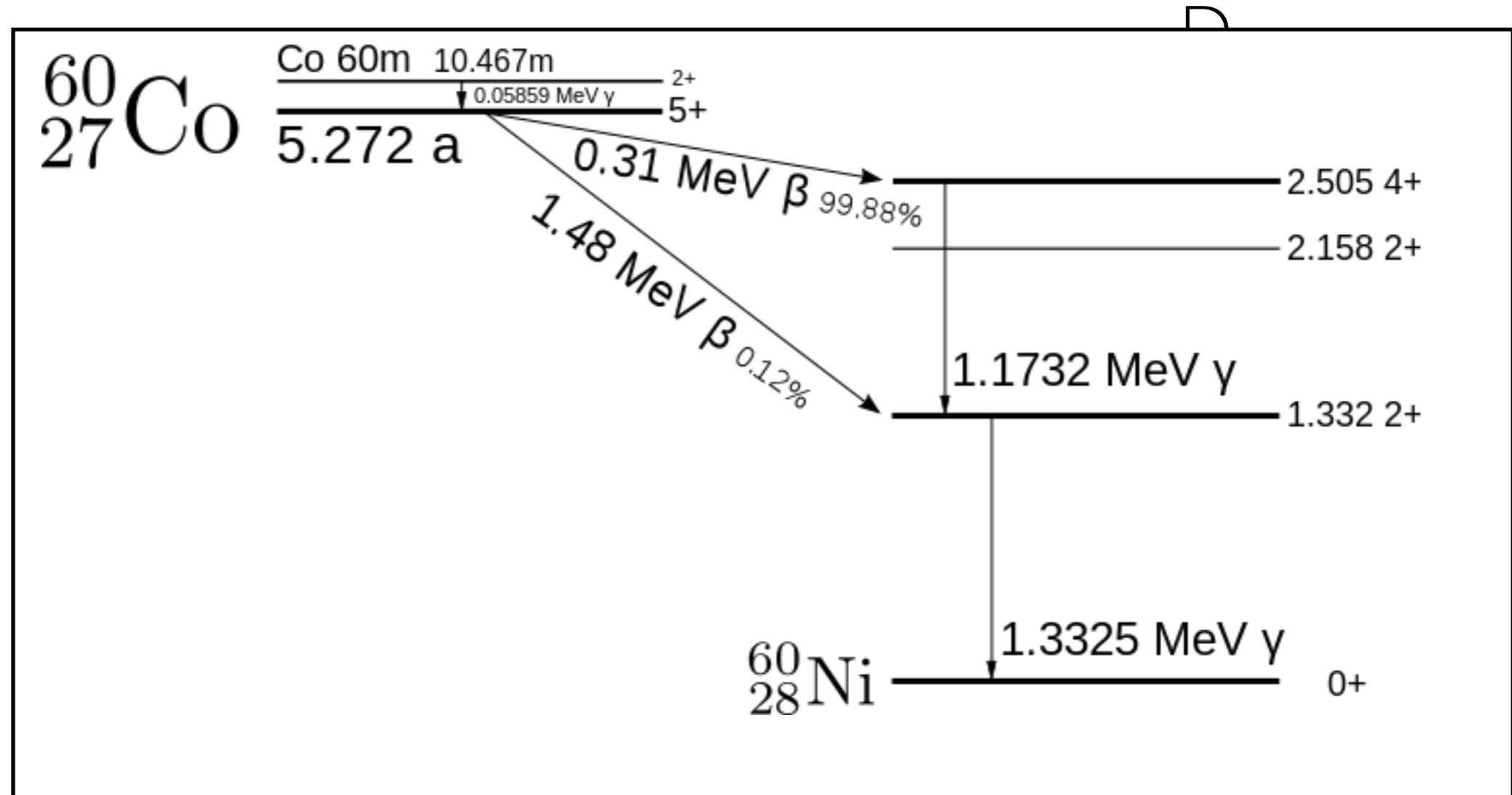
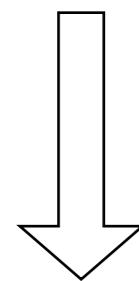
1000 decays/s



D

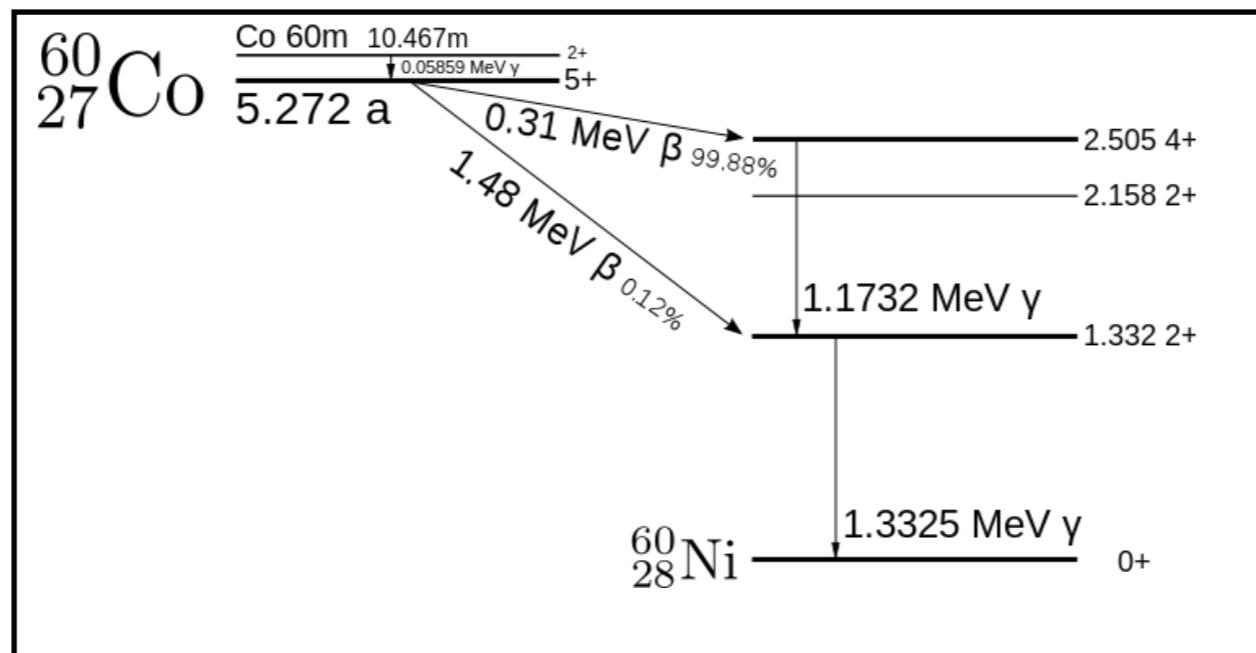


A = 1 kBq



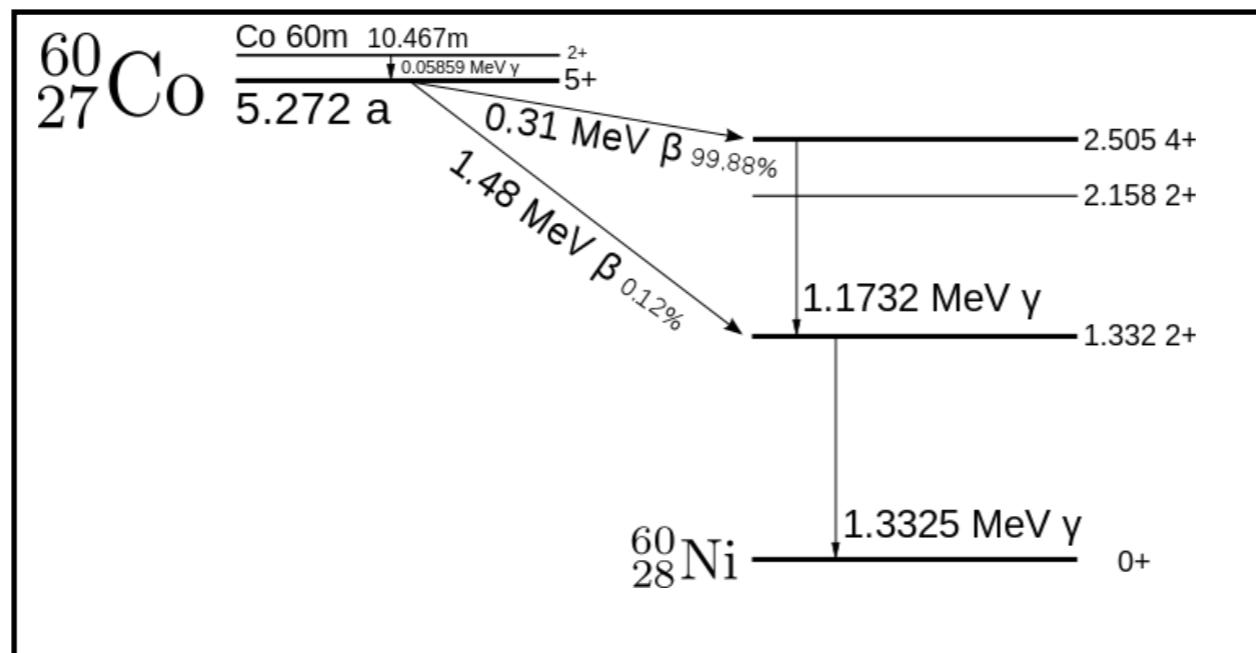
1000 decays/s

On average, how many photons are emitted in a ^{60}Co -decay?



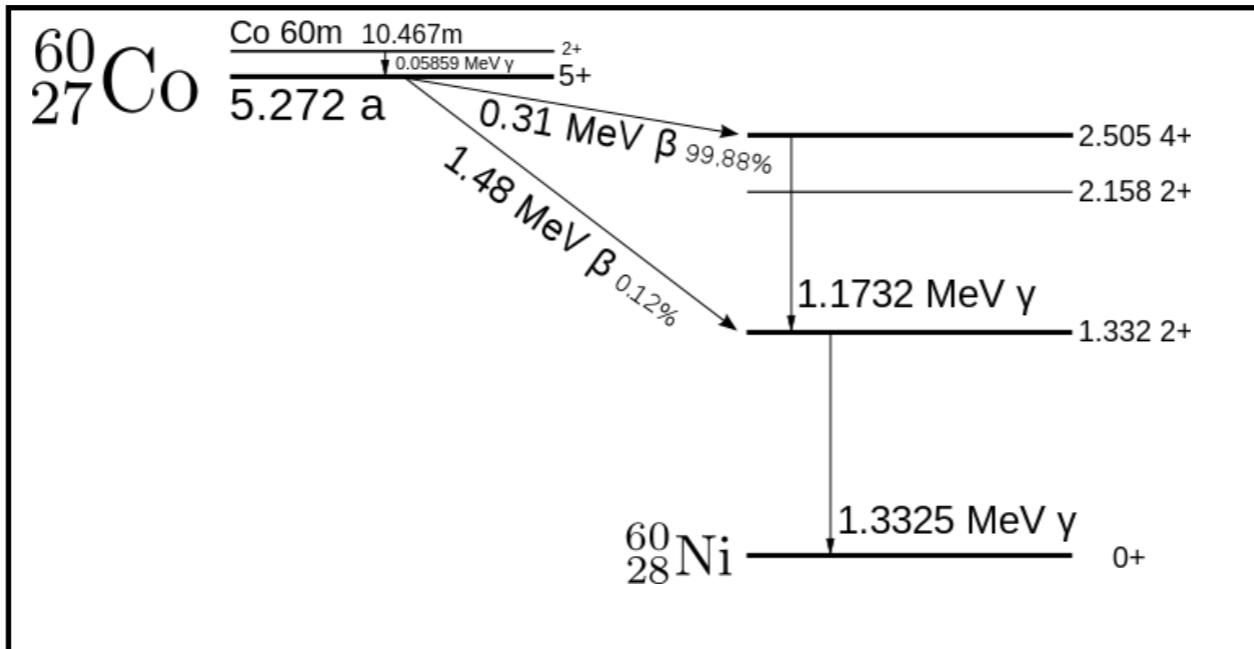
- 1. 1
- 2. 2
- 3. 0,9988
- 4. 1,9988
- 5. anything between 0 and 2 depending of what happens in the nucleus

On average, how many photons are emitted in a ^{60}Co -decay?



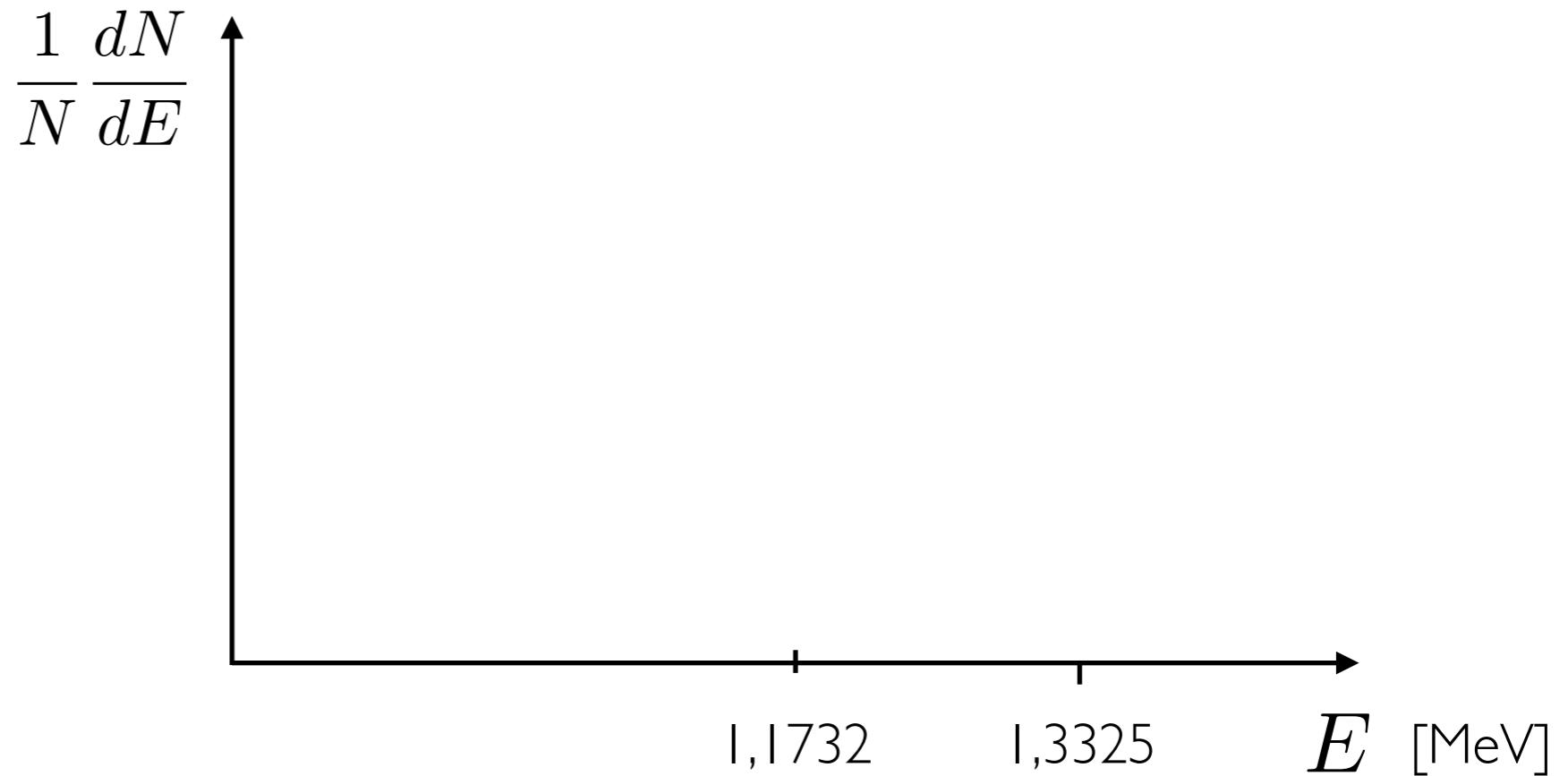
- 1. 1
- 2. 2
- 3. 0,9988
- 4. 1,9988
- 5. anything between 0 and 2 depending of what happens in the nucleus

Draw the emission spectrum of ^{60}Co

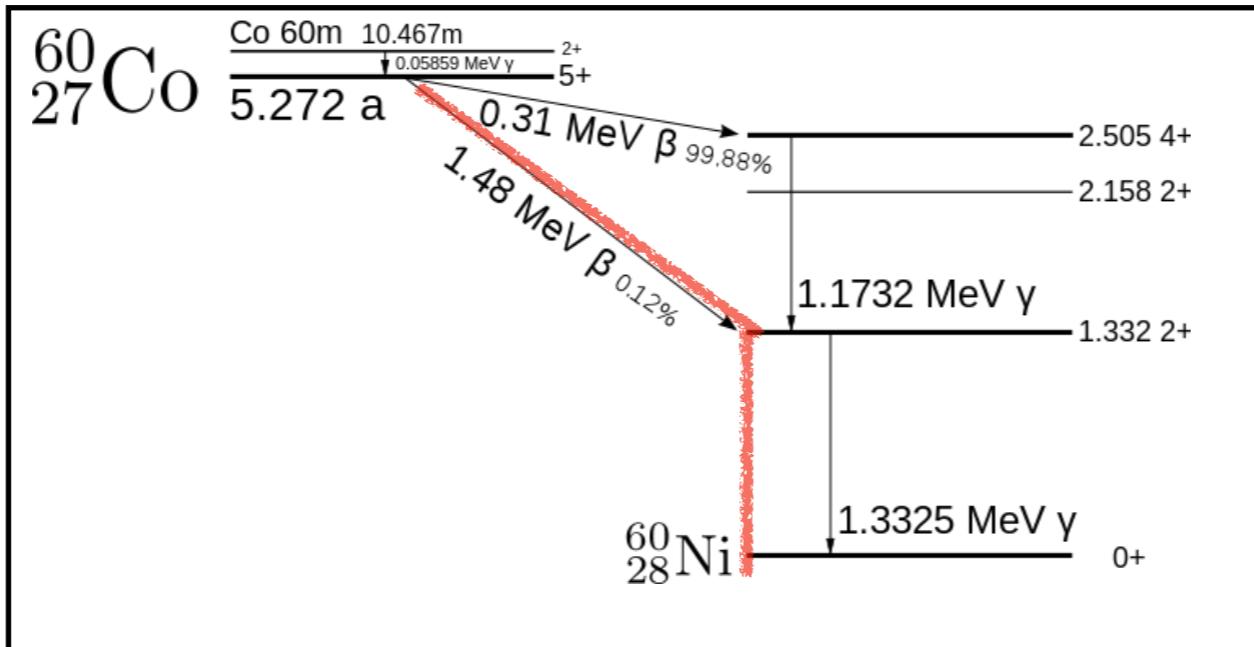


number of photons / energy bin

number of photons

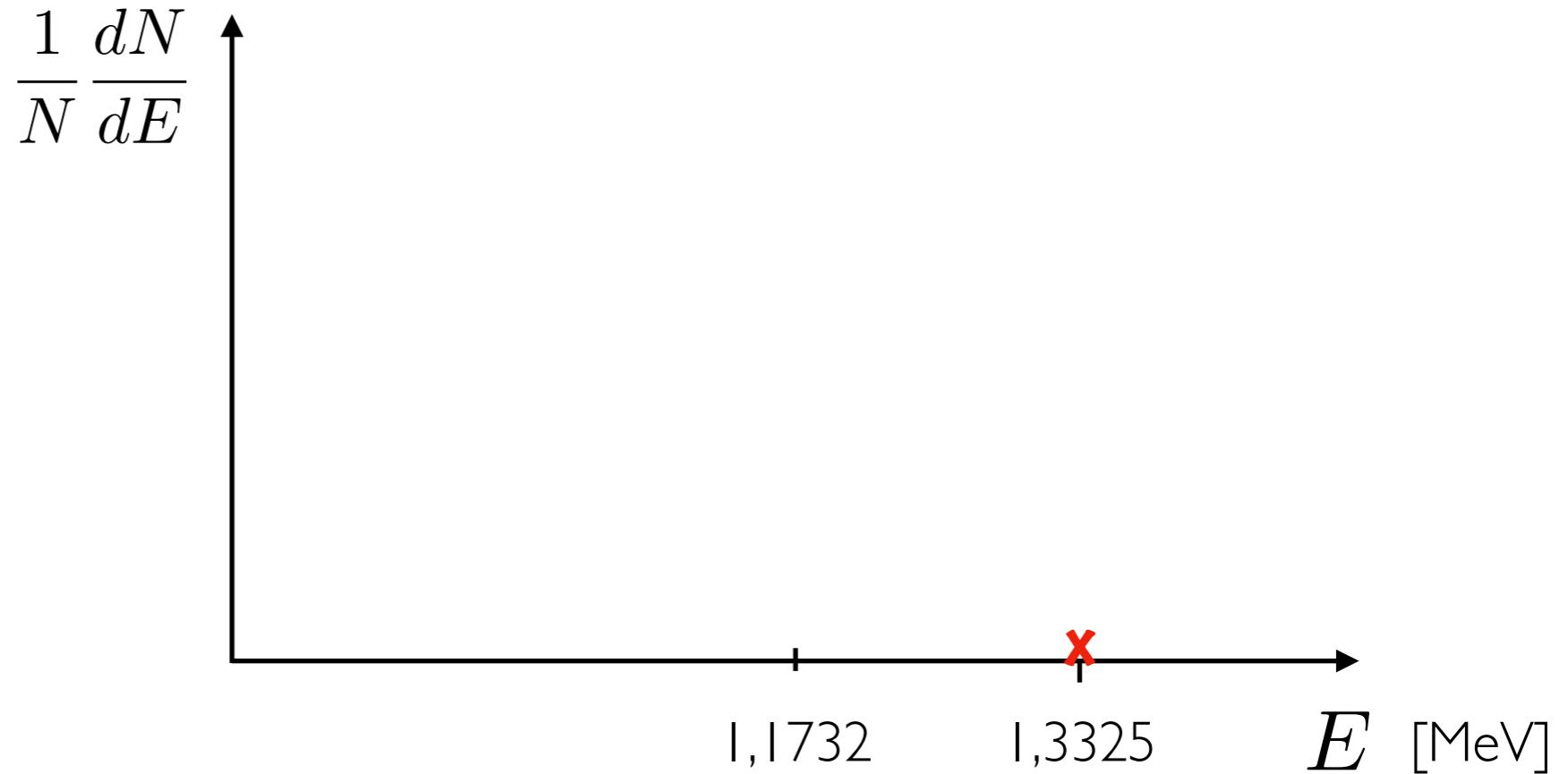


Draw the emission spectrum of ^{60}Co

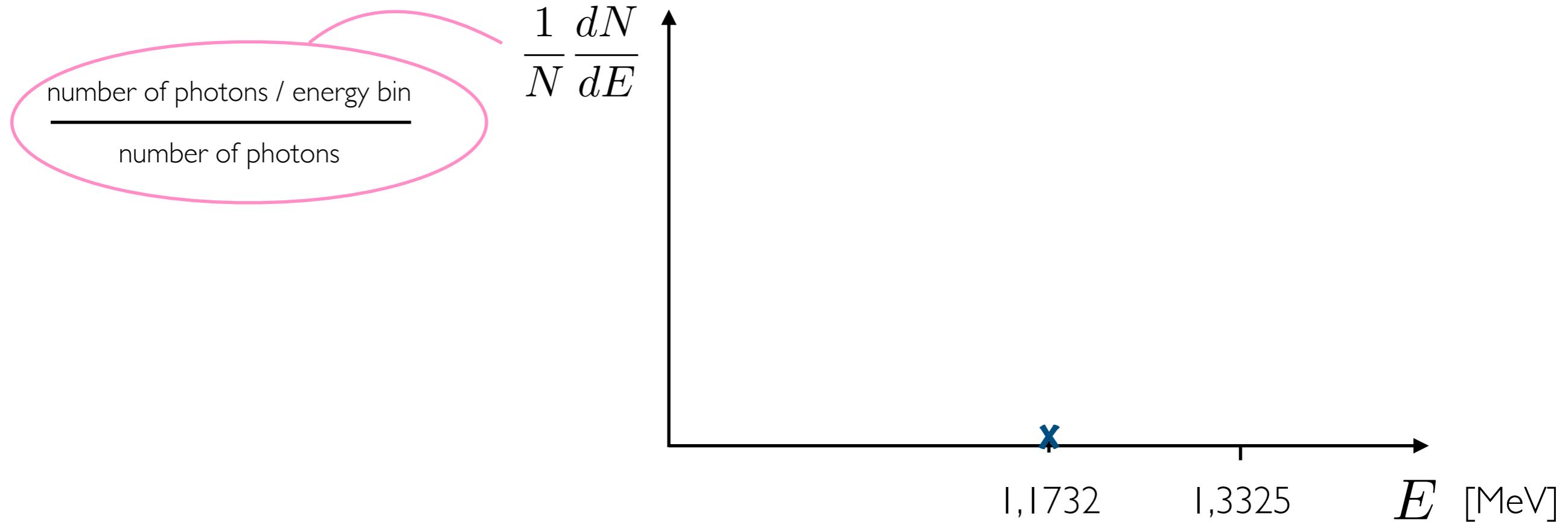
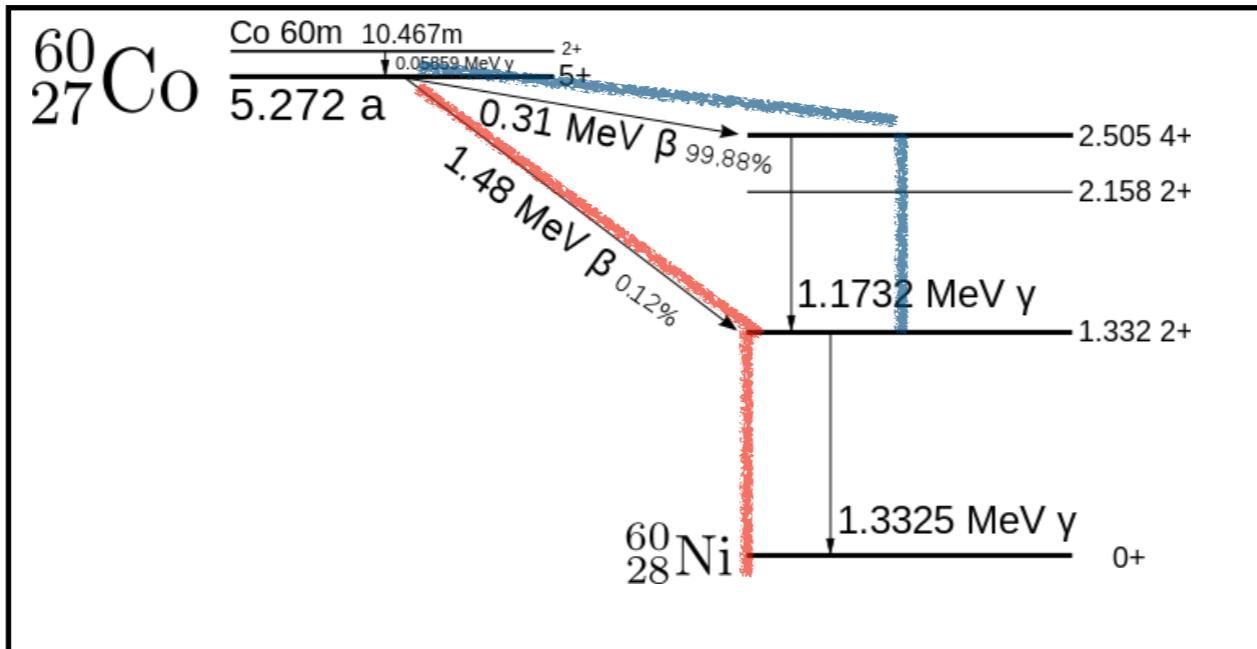


number of photons / energy bin

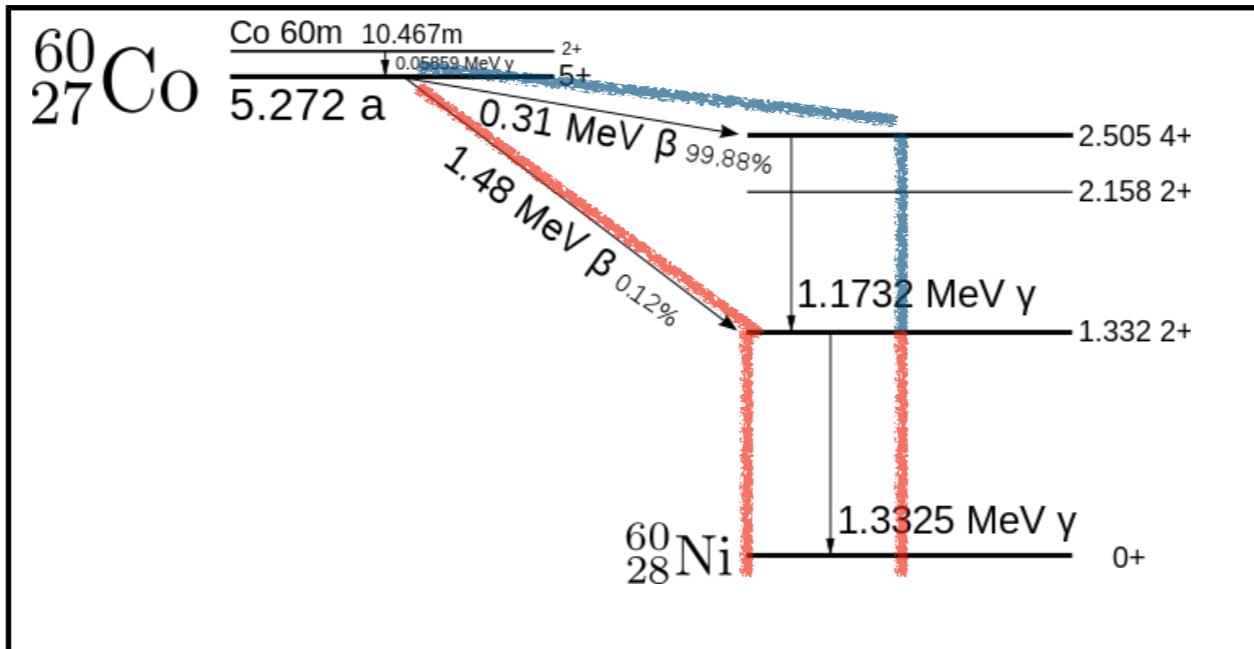
number of photons



Draw the emission spectrum of ^{60}Co

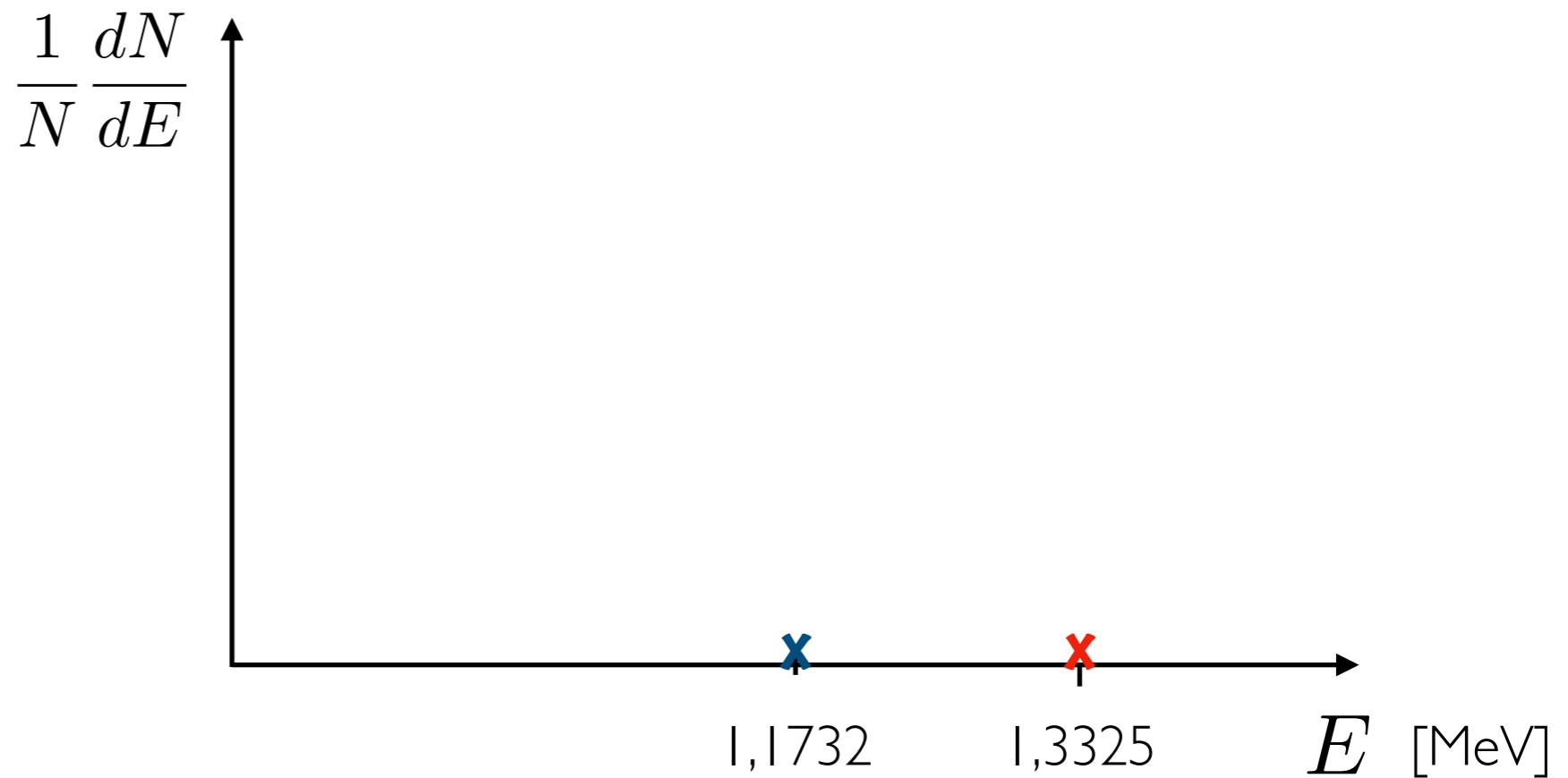


Draw the emission spectrum of ^{60}Co

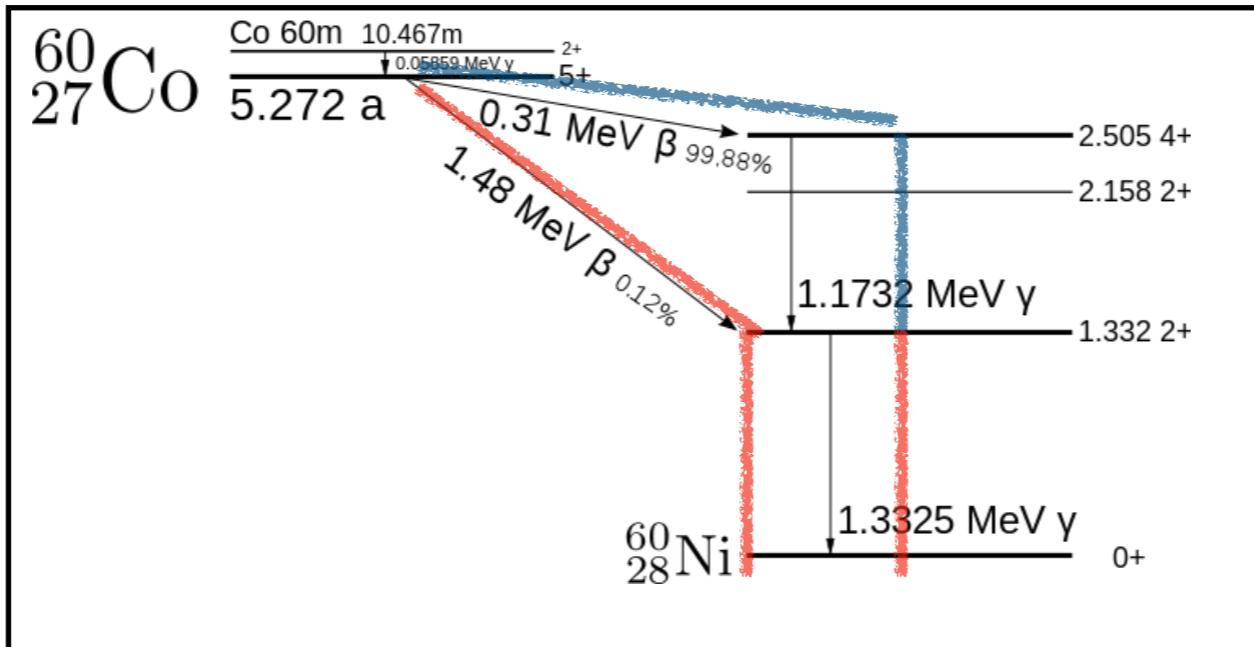


number of photons / energy bin

number of photons

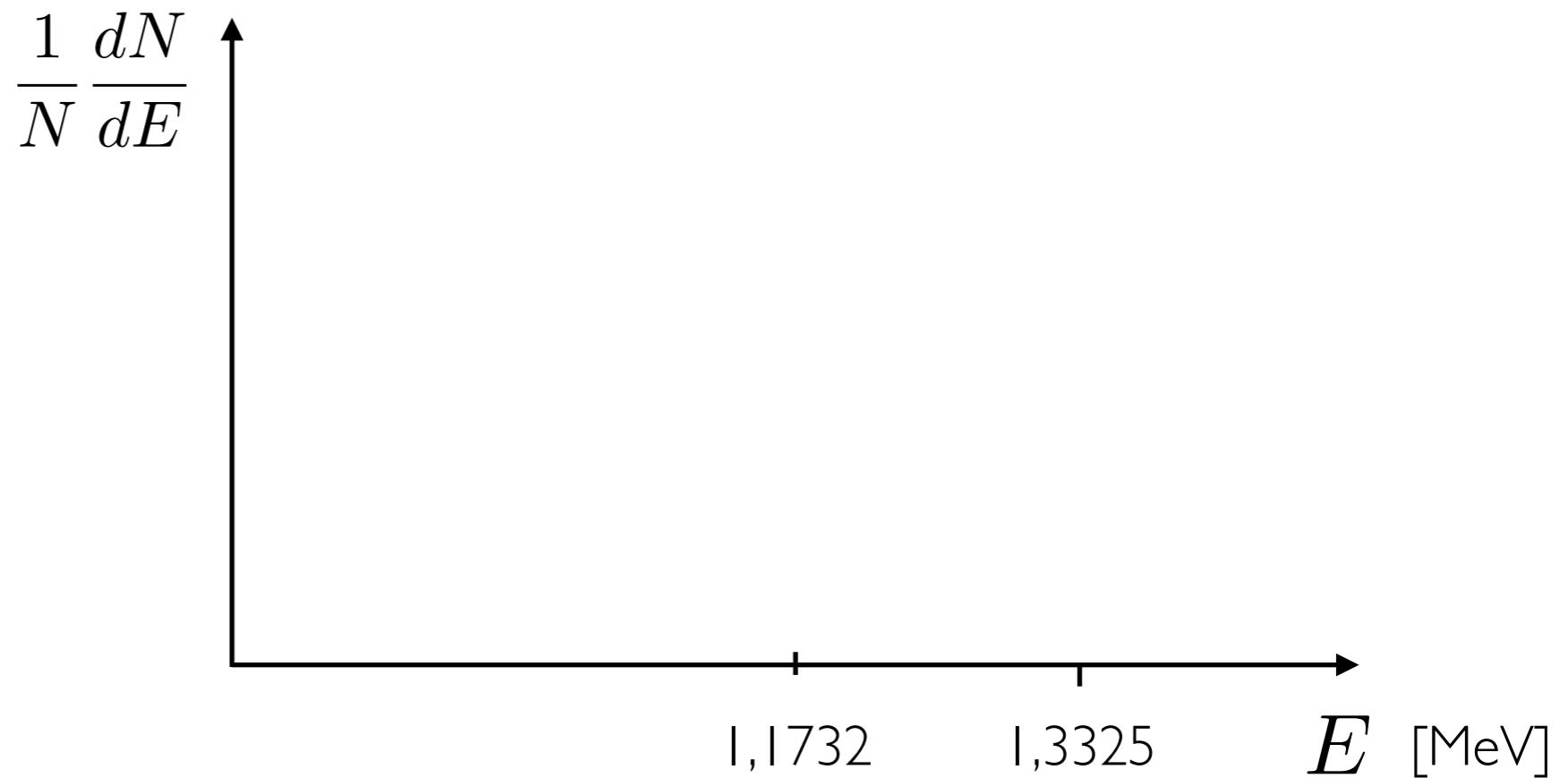


Draw the emission spectrum of ^{60}Co

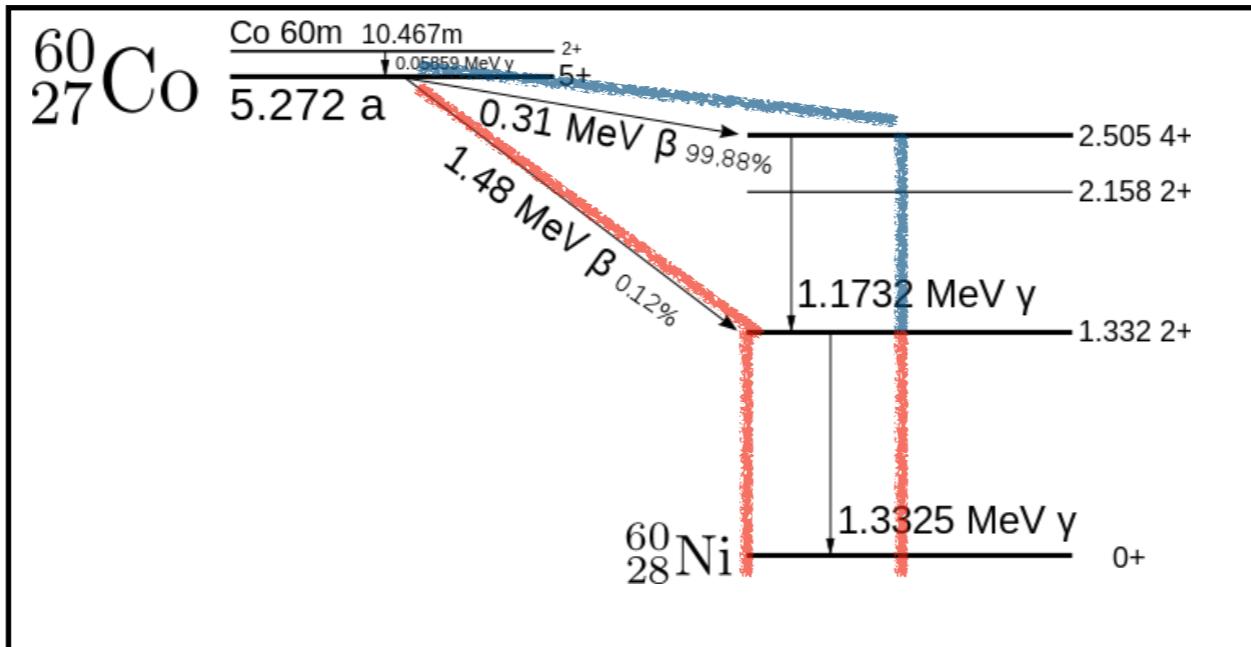


number of photons / energy bin

number of photons

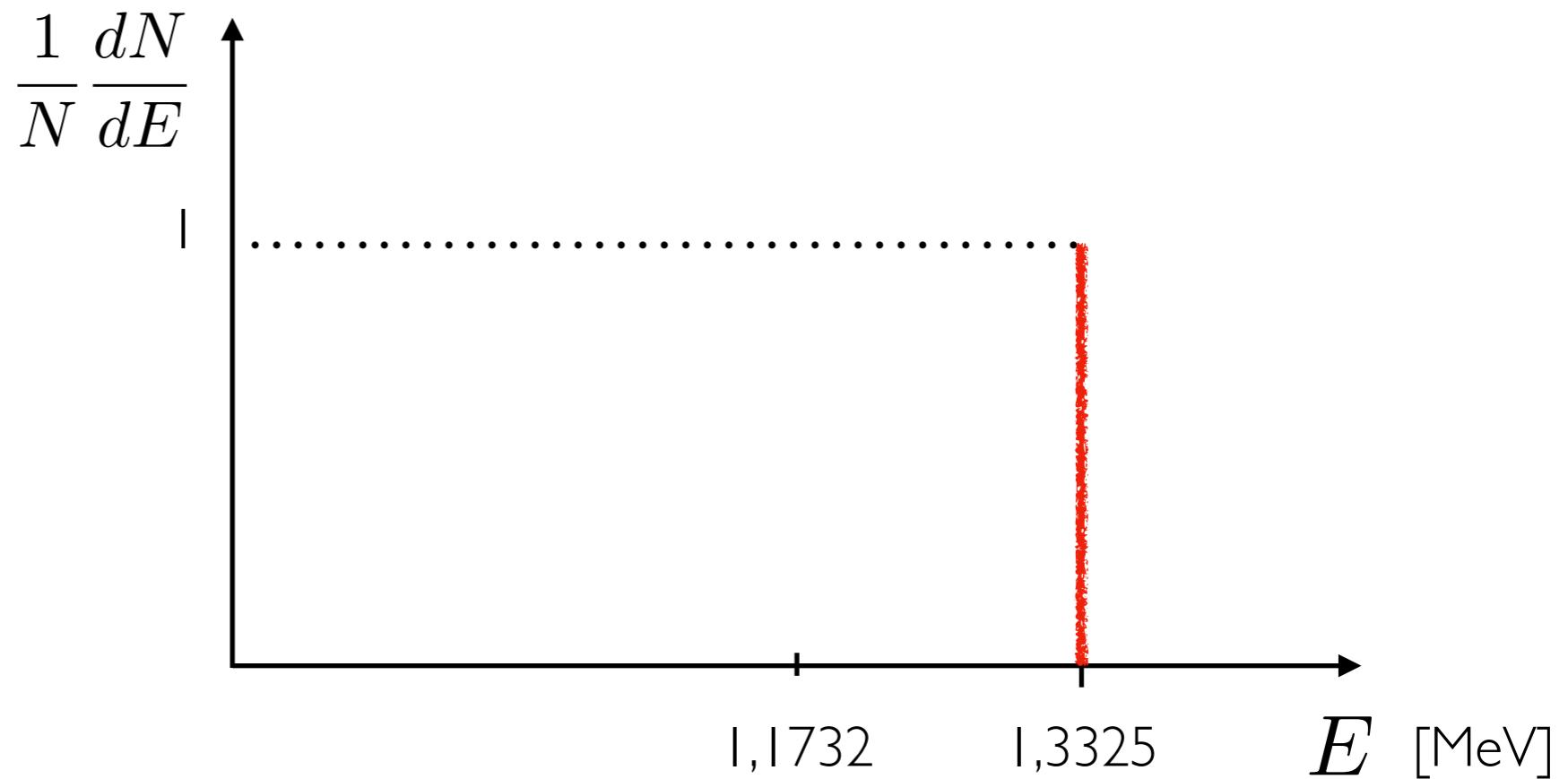


Draw the emission spectrum of ^{60}Co

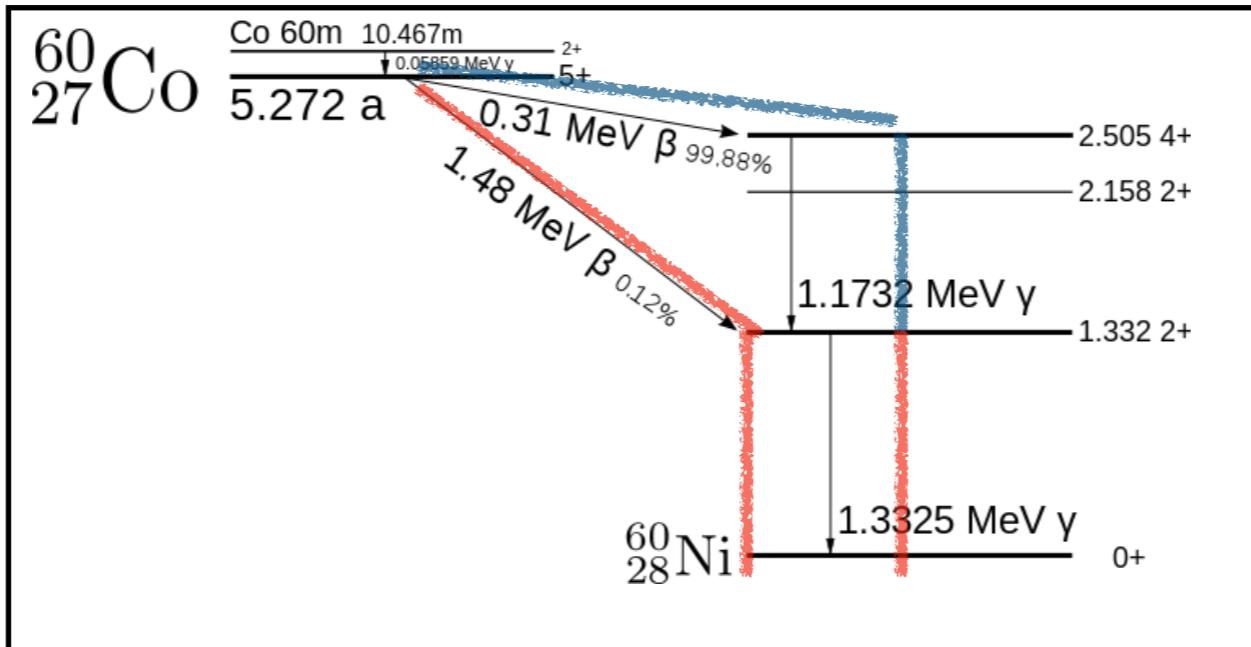


number of photons / energy bin

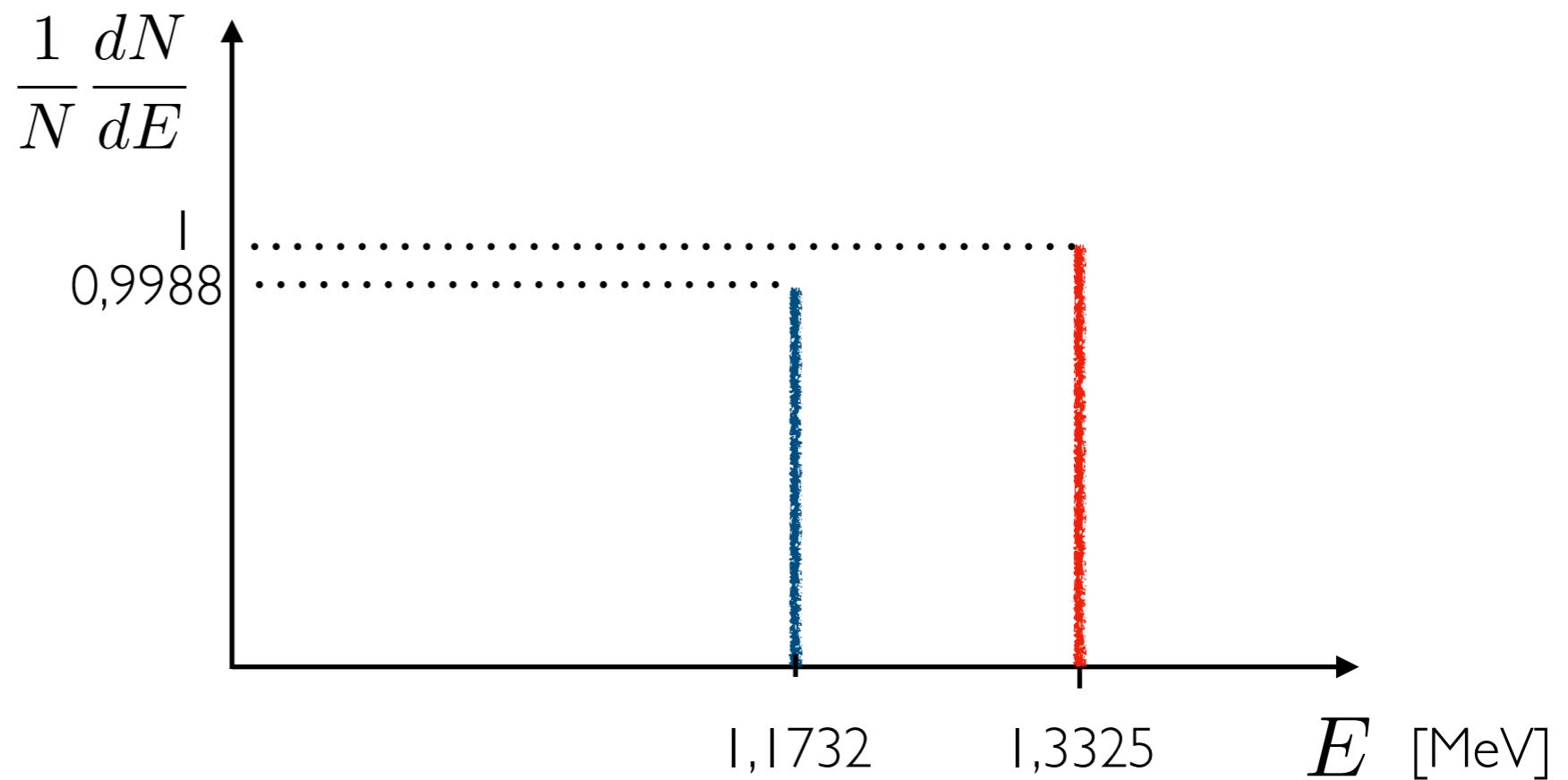
number of photons

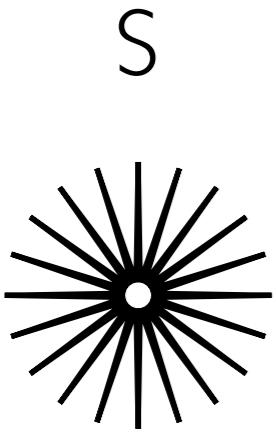


Draw the emission spectrum of ^{60}Co

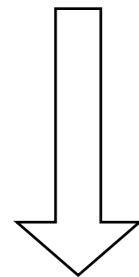


number of photons / energy bin
 $\frac{1}{N} \frac{dN}{dE}$
 number of photons



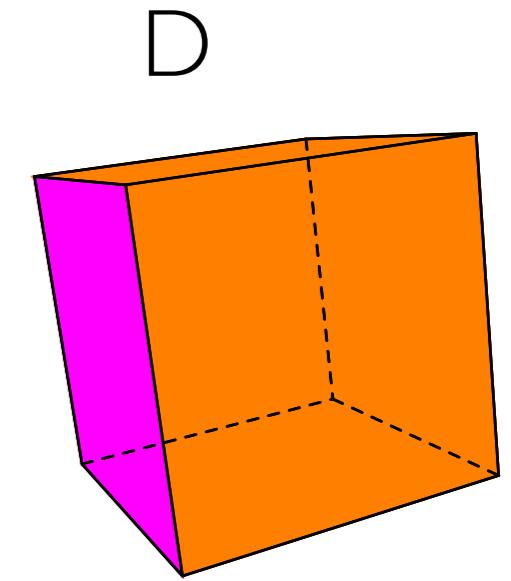


$A = 1 \text{ kBq}$



1000 decays/s

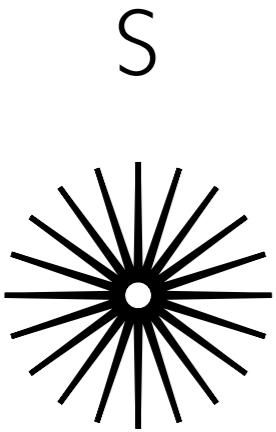
of emitted
photons depends
on decay
scheme!



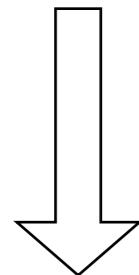
of detected
photons?

efficiency:

$$\frac{\text{\# detected photons}}{\text{\# emitted photons}}$$

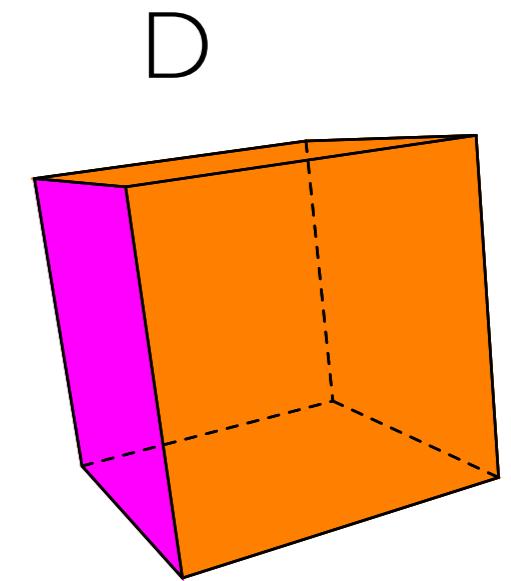


$A = 1 \text{ kBq}$



1000 decays/s

of emitted
photons depends
on decay
scheme!

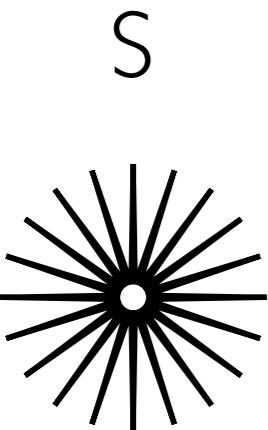


of detected
photons?

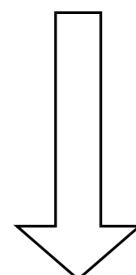
efficiency:

$$\frac{\text{\# detected photons}}{\text{\# emitted photons}}$$

count rate = detected photons?

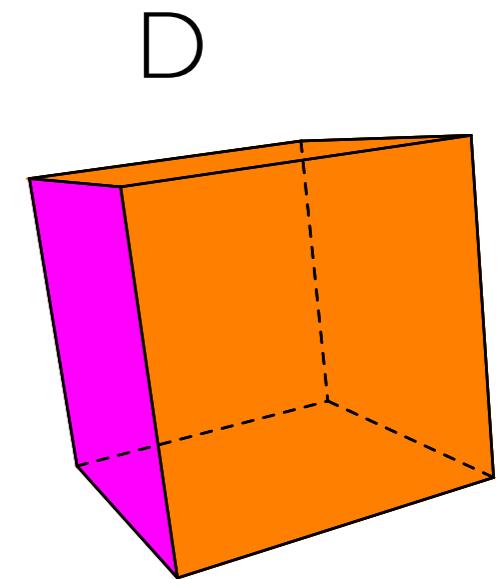


$$A = 1 \text{ kBq}$$



1000 decays/s

of emitted
photons depends
on decay
scheme!



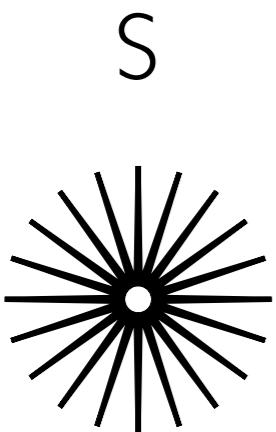
of detected
photons?

efficiency:

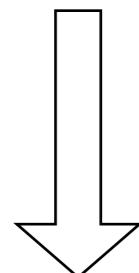
$$\frac{\text{\# detected photons}}{\text{\# emitted photons}}$$

count rate = detected photons?

NO!
(only for photon
counting detectors)

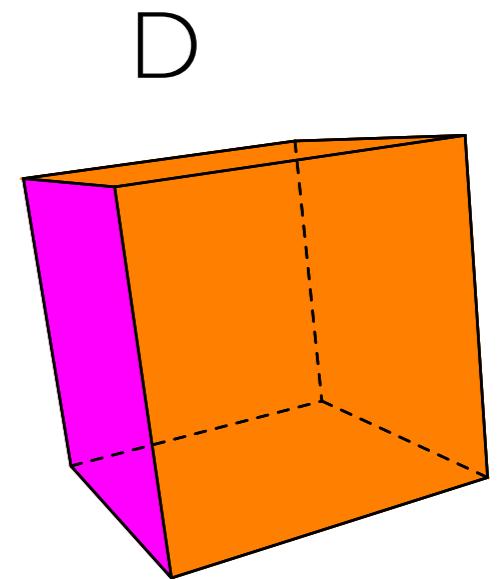


$A = 1 \text{ kBq}$



1000 decays/s

of emitted
photons depends
on decay
scheme!



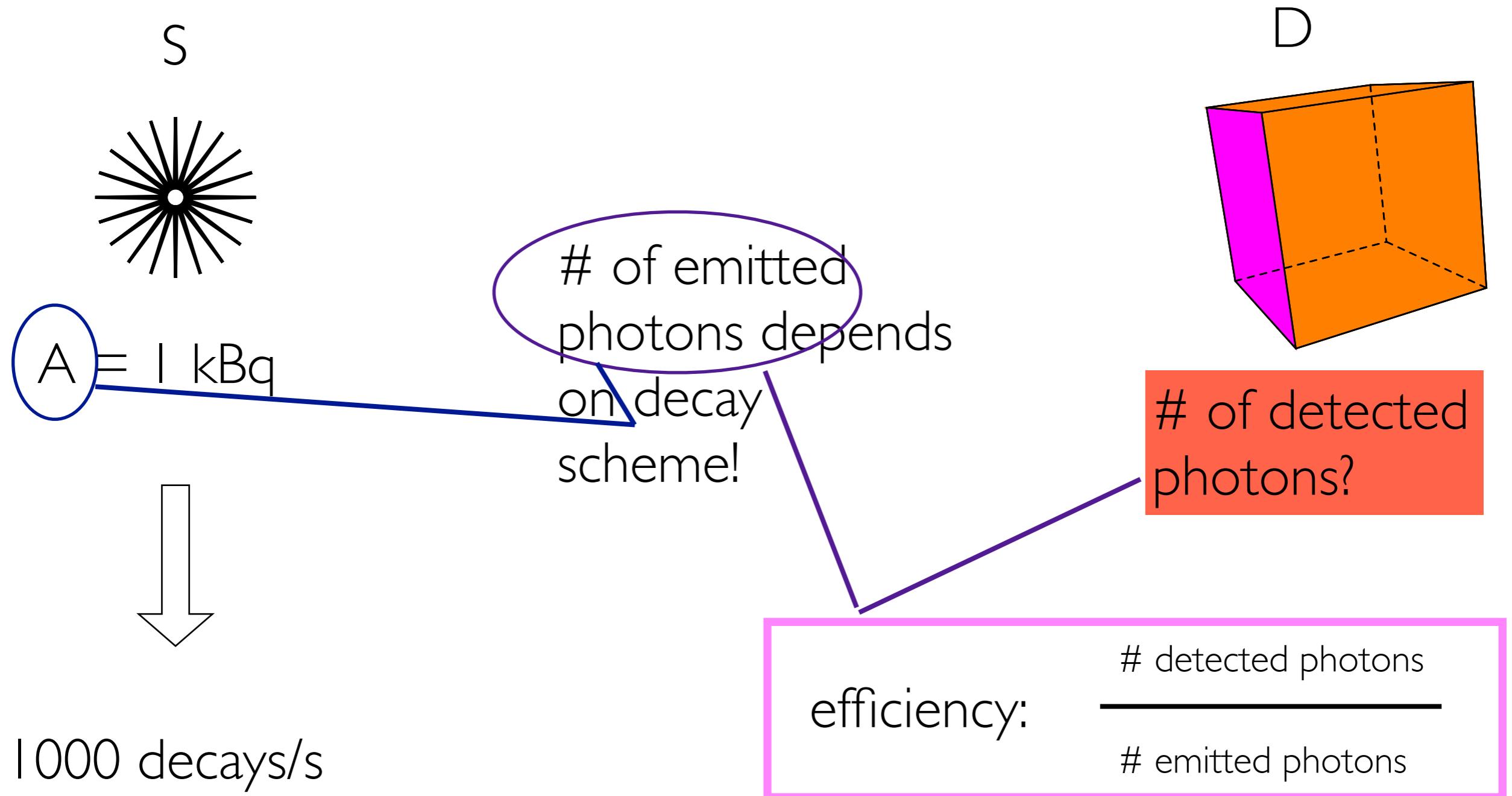
of detected
photons?

efficiency:

$$\frac{\text{# detected photons}}{\text{# emitted photons}}$$

count rate = detected photons?

NO!
(only for photon
counting detectors)



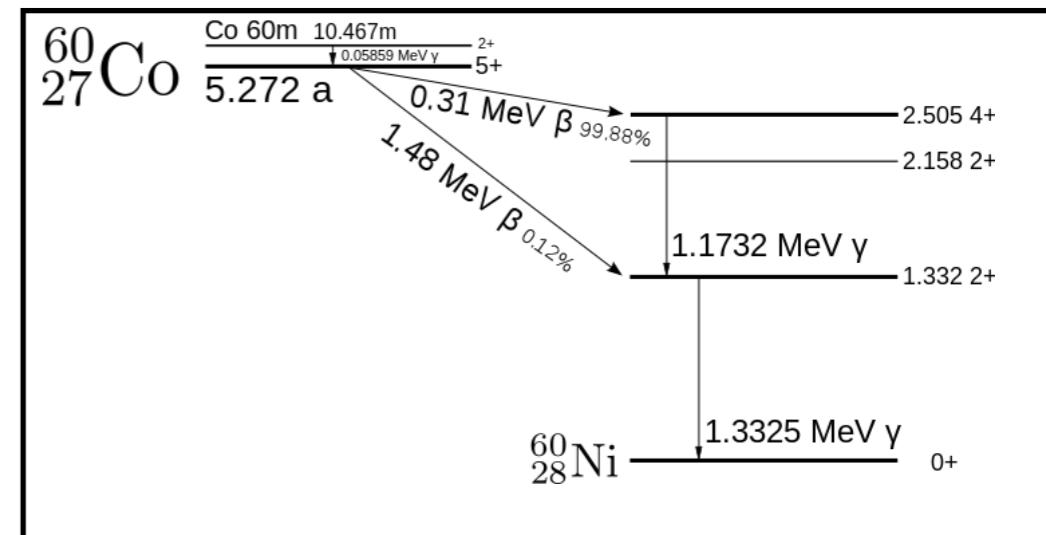
count rate = detected photons?

NO!
(only for photon counting detectors)

A detector with efficiency 2% detects 100 photons per second. The average number of emitted photons per second is then:

1. 2
2. impossible to say, but more than 100
3. 5000

A detector with efficiency 2% detects 100 photons per second from a ^{60}Co -source. The activity of the source can be estimated to be:



1. around 100 Bq
2. impossible to say, but more than 100 Bq
3. around 2500 Bq
4. around 5000 Bq

Source

Detector

What needs to happen for a photon emitted by the source to be detected?

I. The photon needs to hit the detector

$$\text{Def: geometric efficiency} = \frac{\text{fraction of emitted photons that hit the detector}}{\text{# of emitted photons}} = \frac{\text{# of photons hitting detector}}{\text{# of emitted photons}}$$

2. The photon needs to deposit energy (interact) in the detector

$$\text{Def: intrinsic efficiency} = \frac{\text{fraction of the photons hitting the detector that interact in the detector}}{\text{# of photons hitting detector}} = \frac{\text{# of photons interacting in detector}}{\text{# of photons hitting detector}}$$

Then the fraction of detected photons will be the product of the two above^[§]:

$$\text{Def: efficiency} = \frac{\text{fraction of the emitted photons that are detected}}{\text{# of emitted photons}} = \frac{\text{# of photons hitting detector}}{\text{# of emitted photons}} \cdot \frac{\text{# of photons interacting in detector}}{\text{# of photons hitting detector}}$$

(^[§]under the hypothesis that the two are independent of each other)

Warning to the audience!!!!!!| | | 2| 2| 2| 2| 2|

Now we have few definitions! The definitions are always true!

Do not confuse them with the calculation of the efficiency in a particular case, which might result in a number or a symbolic expression!

The latter are only valid in that particular case!

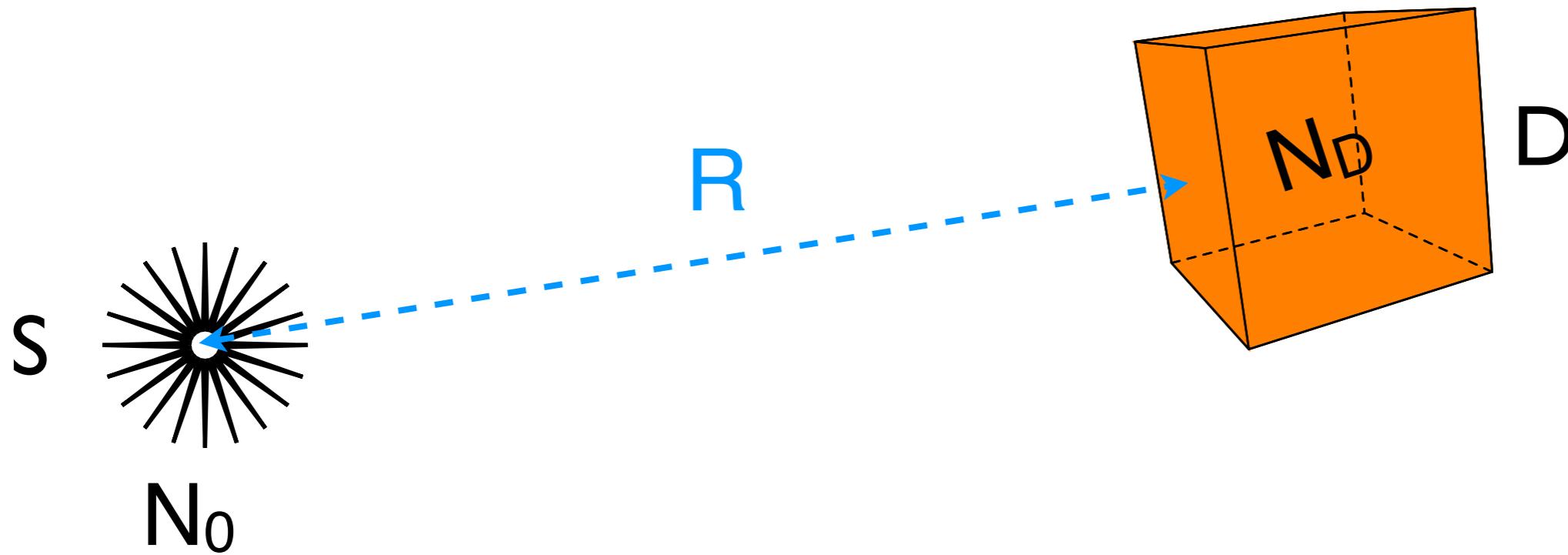
We are now going to find an expression for the efficiency, the geometric efficiency and the intrinsic efficiency ***in a particular case!***

It is an example, to help you:

- better understand the definitions
- understand how to calculate these quantities in various situation by using their definitions

effektivitet:

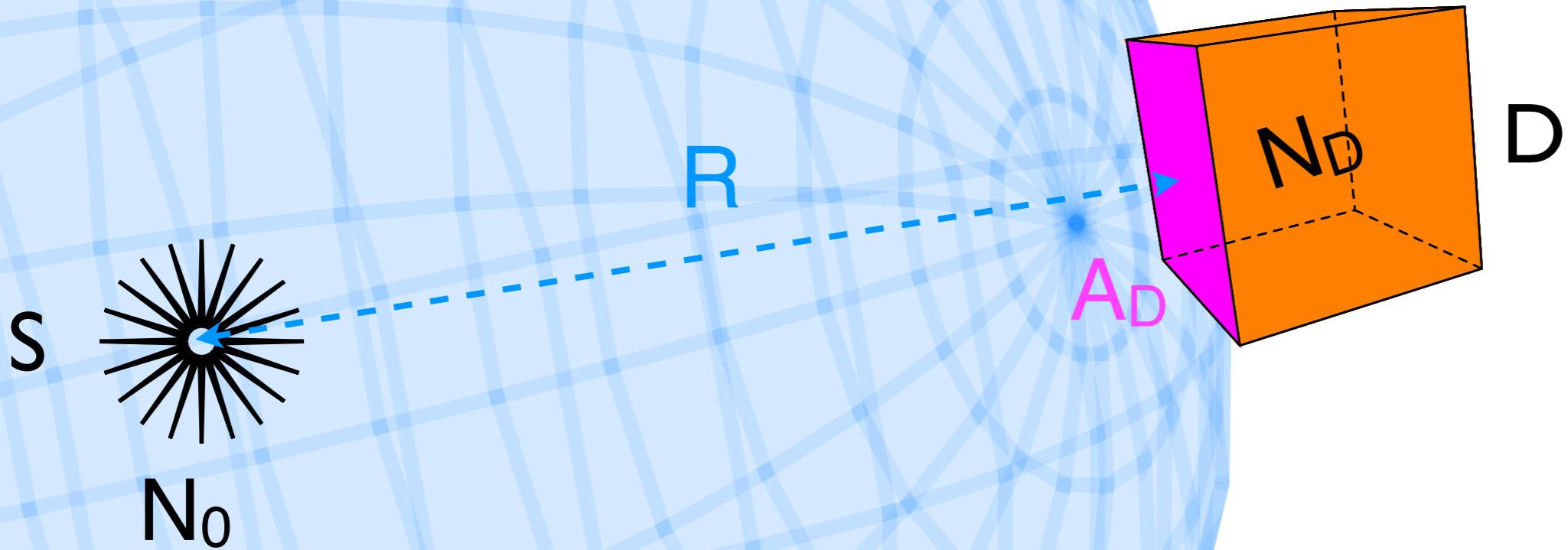
$$\frac{\# \text{ detekterade}}{\# \text{ emitterade}} = \frac{N_D}{N_0}$$



vad spelar roll?

effektivitet:

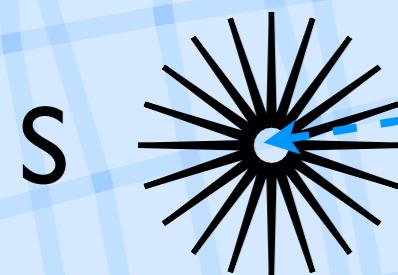
$$\frac{\# \text{ detekterade}}{\# \text{ emitterade}} = \frac{N_D}{N_0}$$



vad spelar roll?

effektivitet:

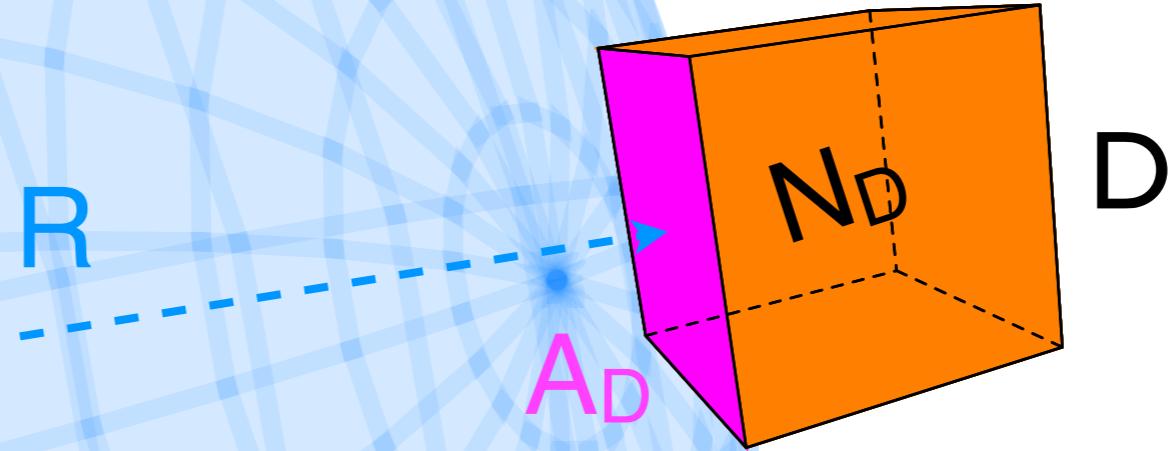
$$\frac{\# \text{ detekterade}}{\# \text{ emitterade}} = \frac{N_D}{N_0}$$



N_0

vad spelar roll?

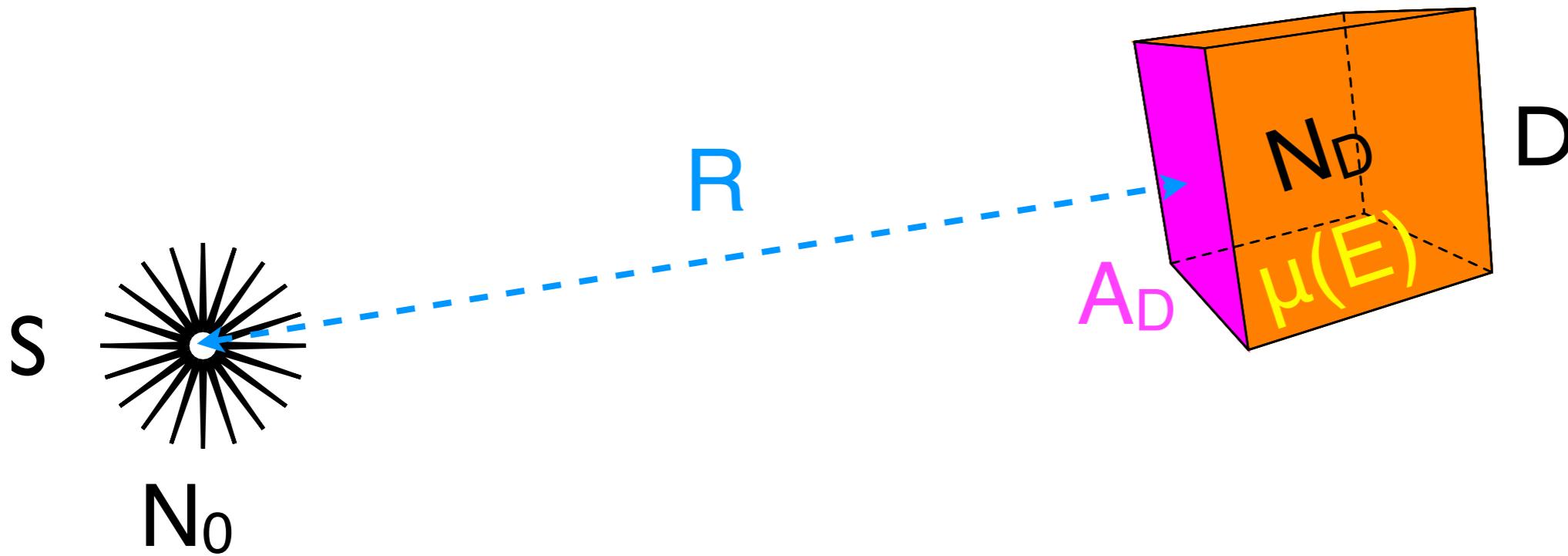
geometri:



$$\frac{\# \text{ träffar } D}{\# \text{ emitterade}} = \frac{A_D}{4\pi R^2}$$

effektivitet:

$$\frac{\# \text{ detekterade}}{\# \text{ emitterade}} = \frac{N_D}{N_0}$$



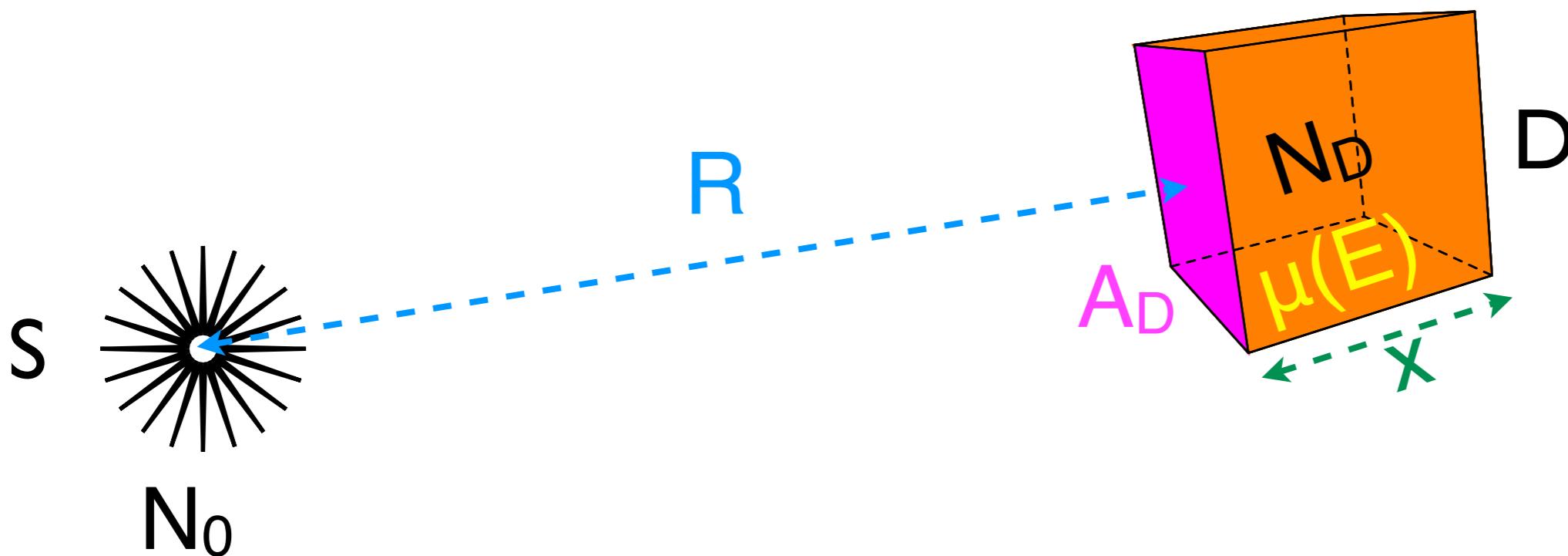
vad spelar roll?

geometri:

$$\frac{\# \text{ träffar } D}{\# \text{ emitterade}} = \frac{A_D}{4\pi R^2}$$

effektivitet:

$$\frac{\# \text{ detekterade}}{\# \text{ emitterade}} = \frac{N_D}{N_0}$$



vad spelar roll?

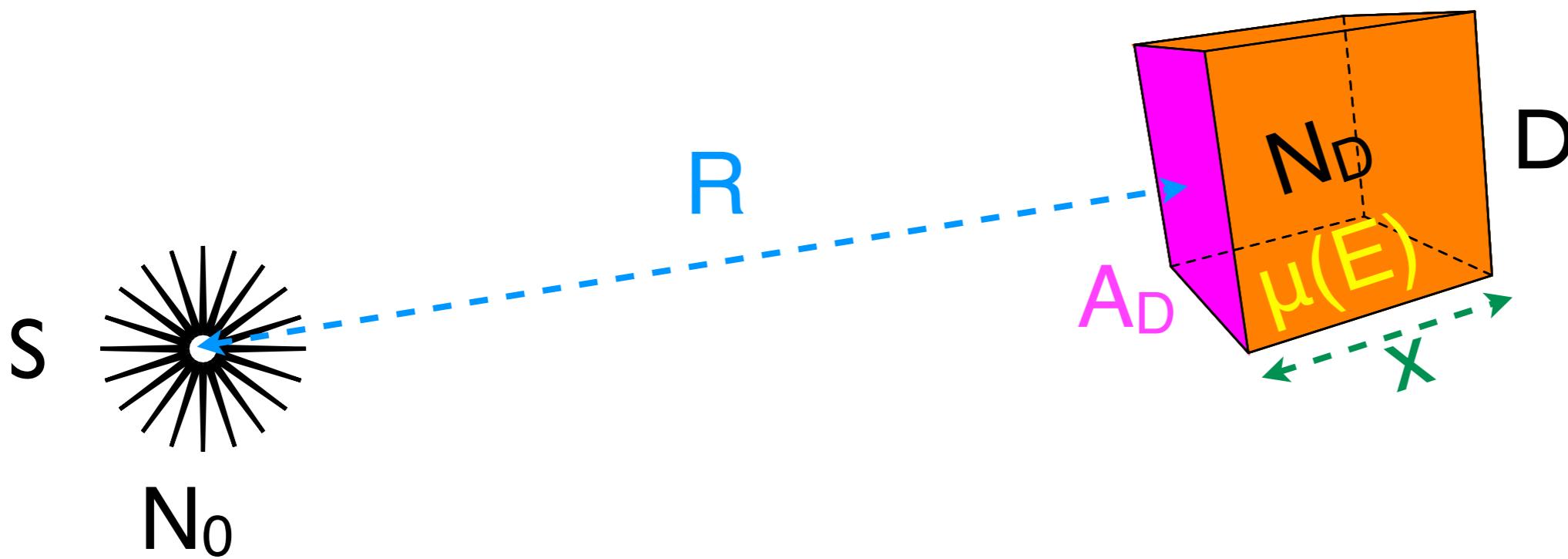
geometri: $\frac{\# \text{ träffar } D}{\# \text{ emitterade}} = \frac{A_D}{4\pi R^2}$

“intrinsic efficiency”:

$$\frac{\# \text{ attenuerade}}{\# \text{ träffar } D} = 1 - e^{-\mu(E)x}$$

effektivitet:

$$\frac{\# \text{ detekterade}}{\# \text{ emitterade}} = \frac{N_D}{N_0} = \frac{A_D (1 - e^{-\mu(E)x})}{4\pi R^2}$$



vad spelar roll?

geometri: $\frac{\# \text{ träffar } D}{\# \text{ emitterade}} = \frac{A_D}{4\pi R^2}$

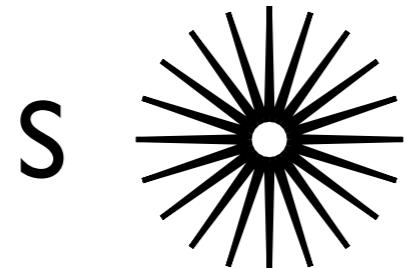
“intrinsic efficiency”:

$$\frac{\# \text{ attenuerade}}{\# \text{ träffar } D} = 1 - e^{-\mu(E)x}$$

Detection efficiency can also be experimentally determined (measured):

Def: efficiency = fraction of the emitted photons that are detected

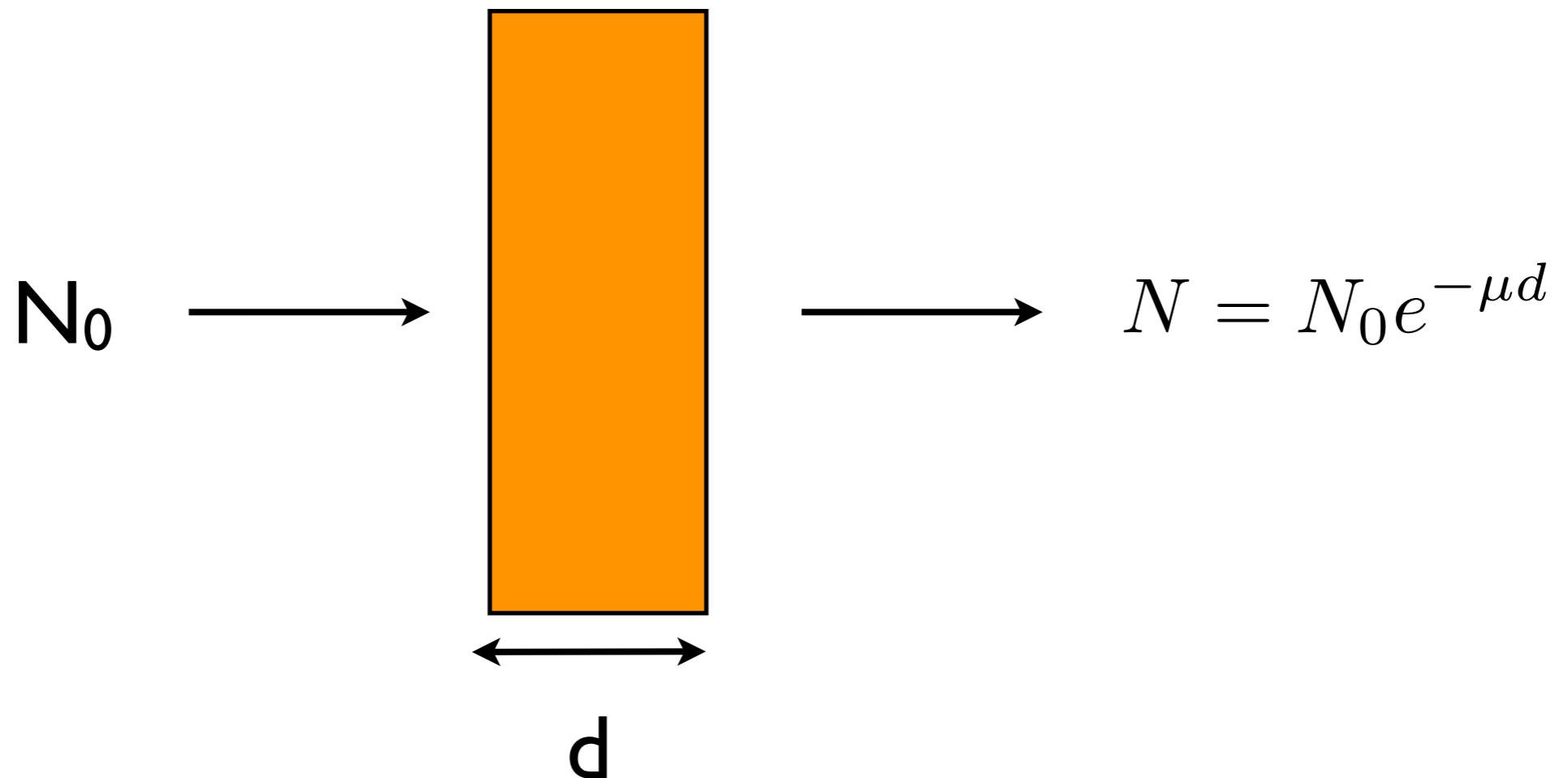
known source
(A and decay scheme)



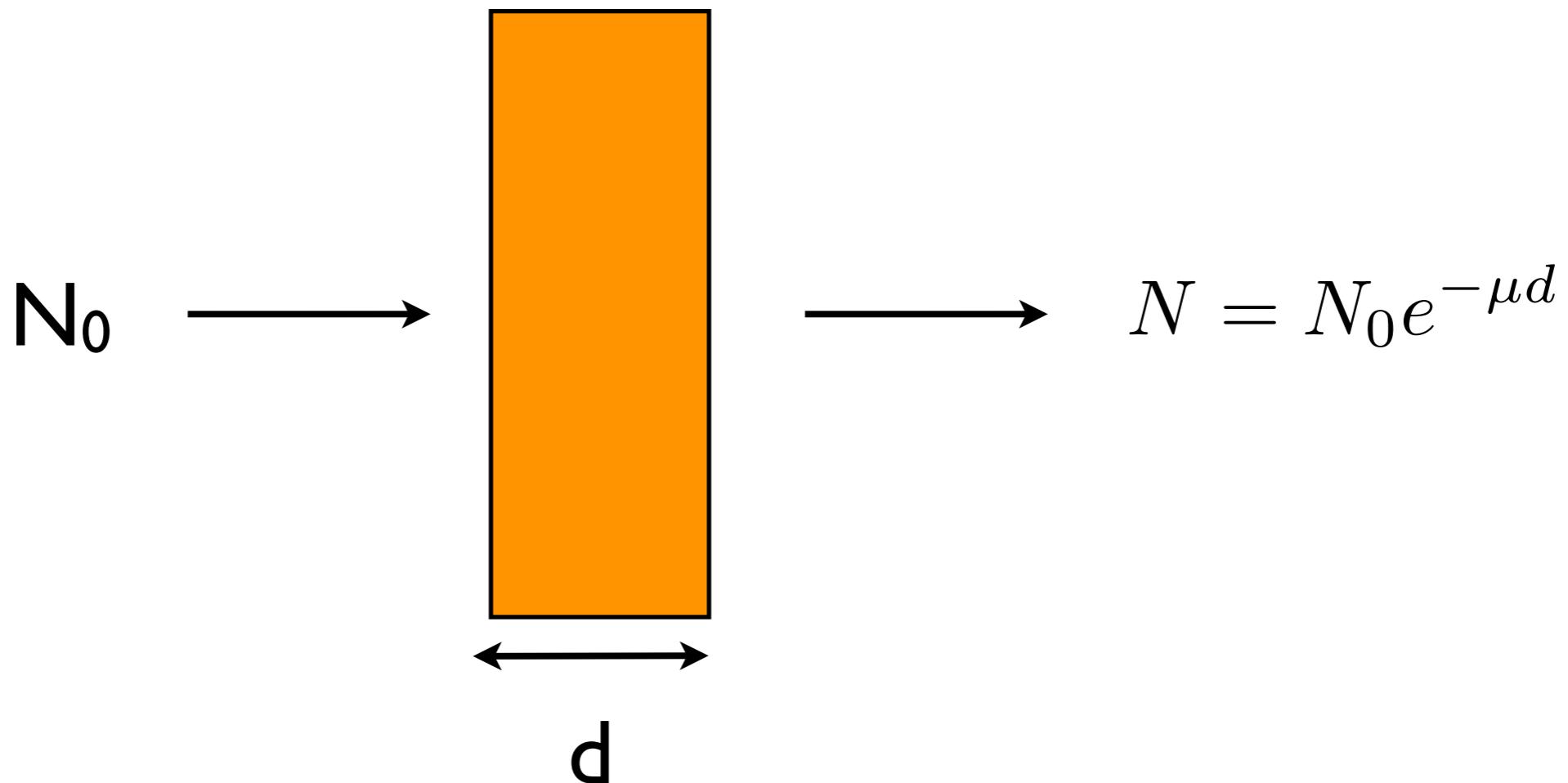
detector



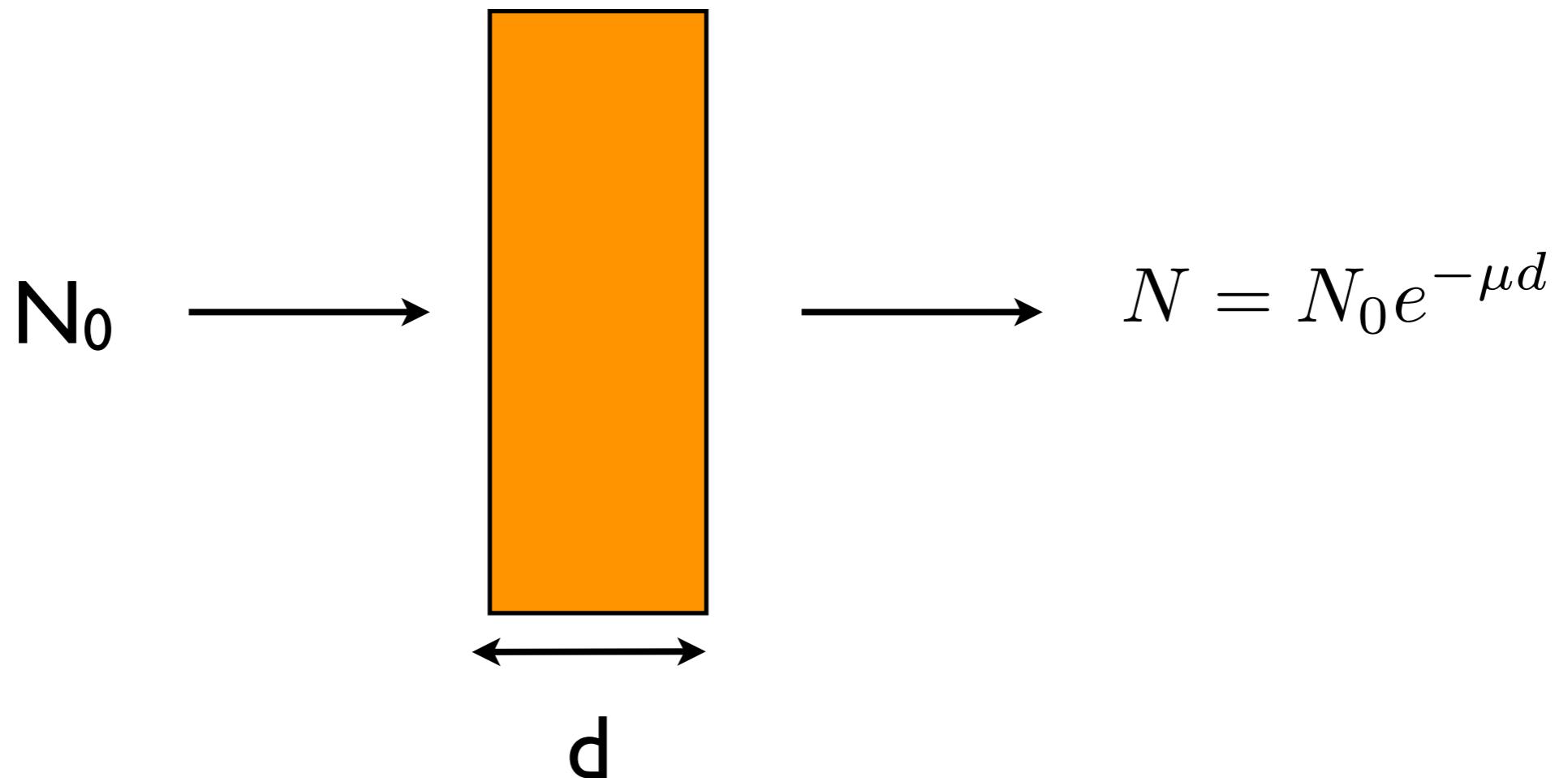
$$\text{efficiency} = \frac{\text{number of counts from detector under acquisition time}}{\text{number of estimated photons emitted under acquisition time}}$$



1. N är antal som har gått genom
2. N är antal som har attenuerats
3. N är antal som har absorberats



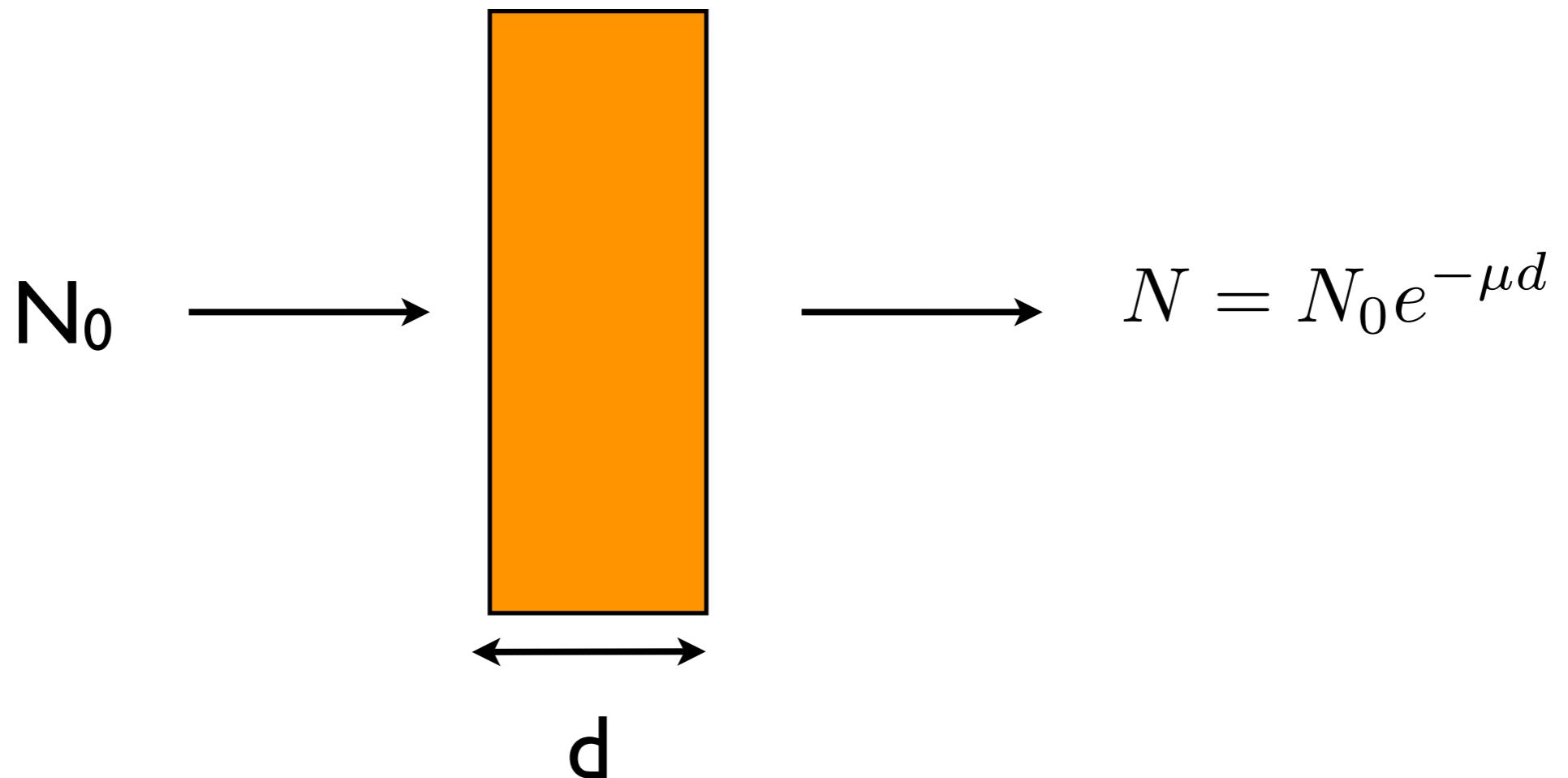
1. N är antal som har gått genom
2. N är antal som har attenuerats
3. N är antal som har absorberats



Antag att:

$$\frac{N}{N_0} = 0,9$$

1. 90% har stoppats
2. 90% har attenuerats
3. 10% har stoppats
4. 10% har attenuerats



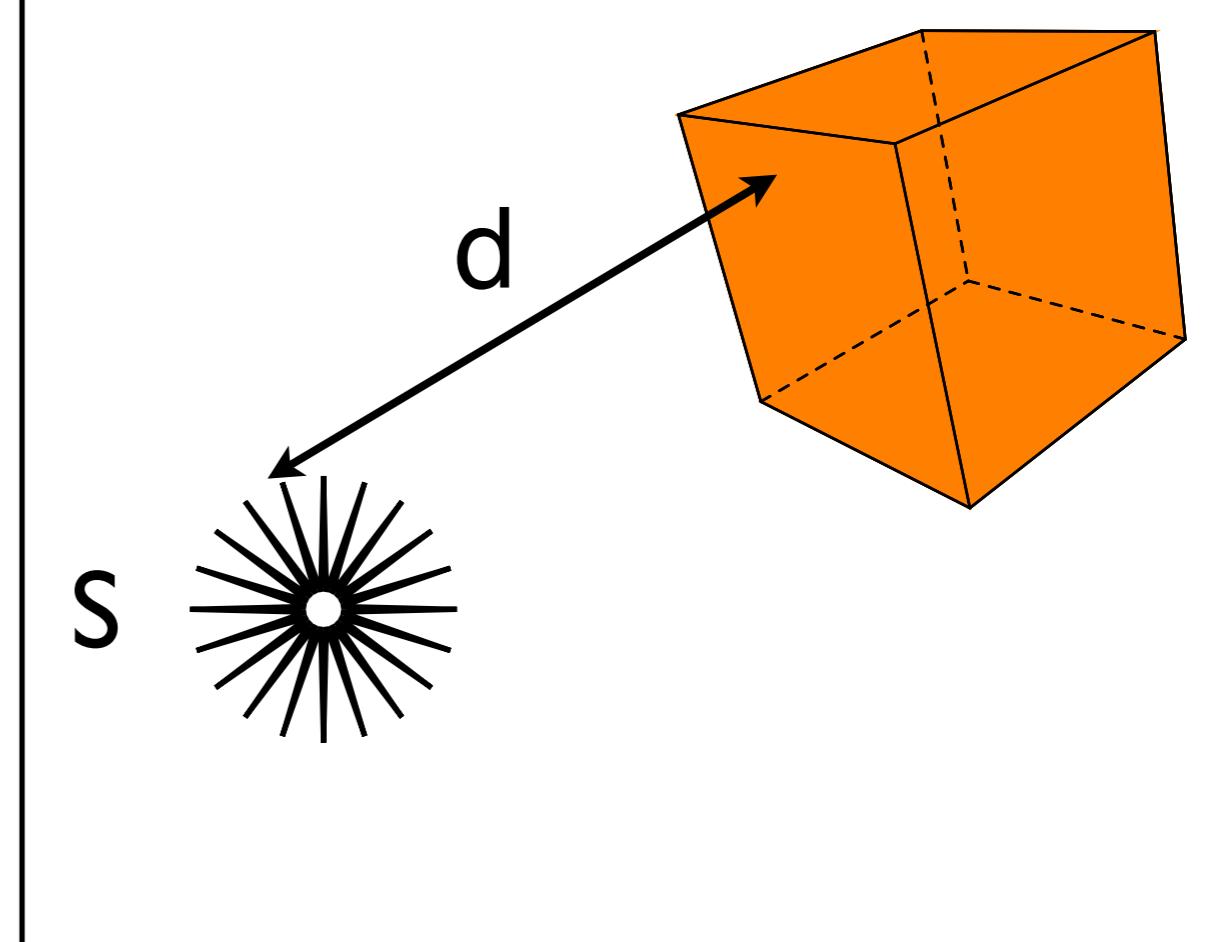
Antag att:

$$\frac{N}{N_0} = 0,9$$

1. 90% har stoppats
2. 90% har attenuerats
3. 10% har stoppats
4. 10% har attenuerats

När källan S ställs på avståndet d från detektorn så är räknehastigheten hos detektorn N counts/s.

Om källan flyttas till avståndet $2d$ så blir räknehastigheten:



- 1. $4N$
- 2. $2N$
- 3. N
- 4. $N/2$
- 5. $N/4$

Detector technology

Detektorer för planröntgen:

önskvärda egenskaper?

absorptionsförmåga: effektivitet

- 100% absorption, helst PE
- position sensitive
- ~~förkasta Comptonspridda~~
- snabb?

kontrast

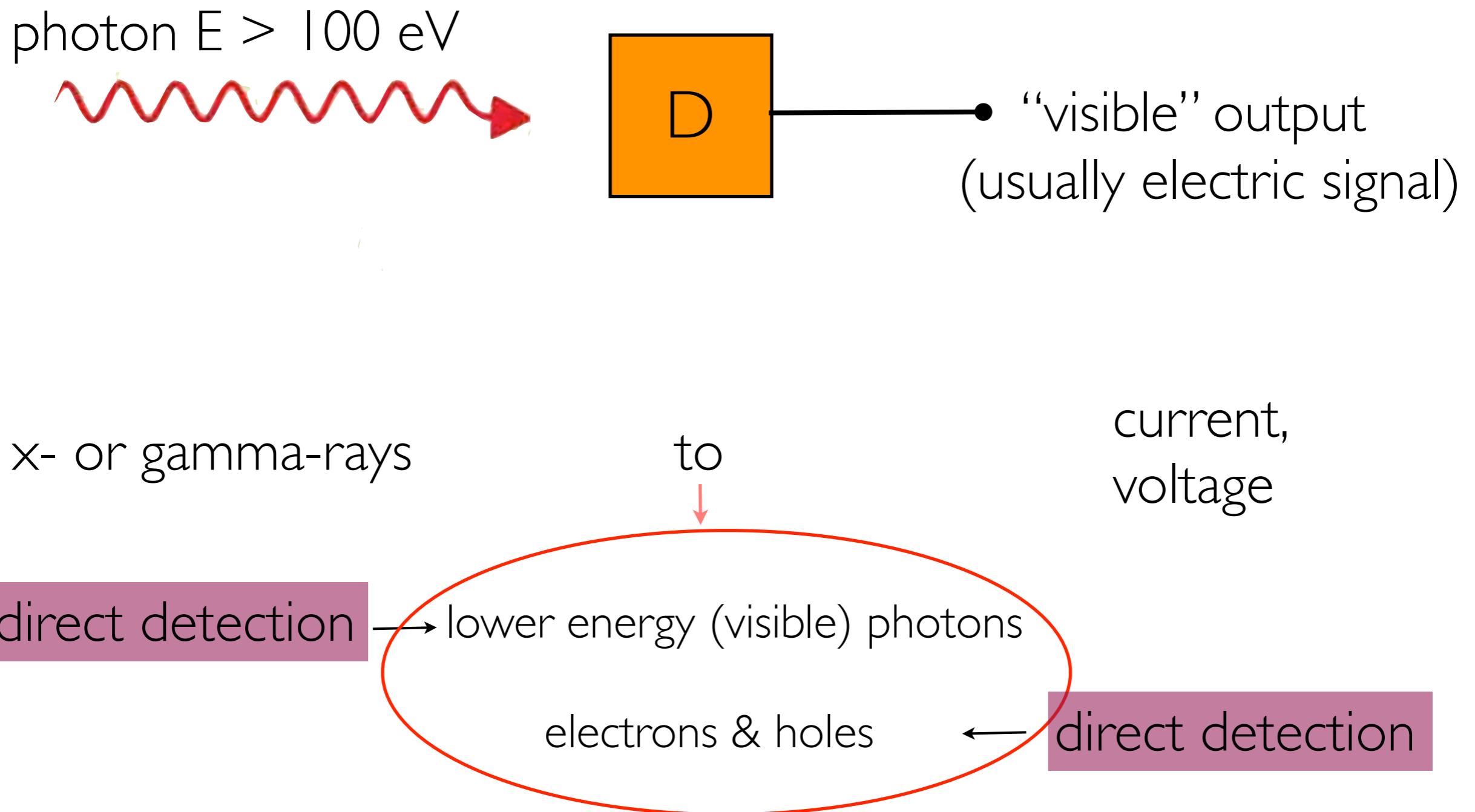
rumsupplösning

ej möjligt i transm

ibland

BILLIGT!!!

Detector for ionising radiation: basic principles

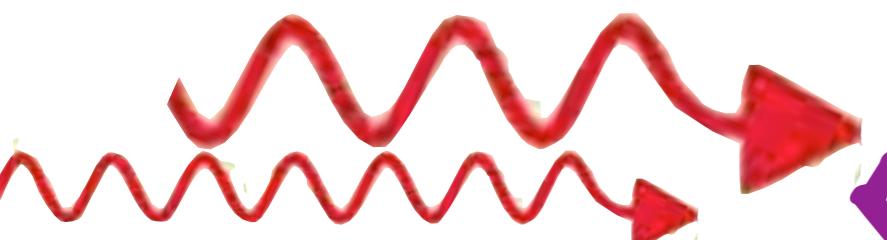


What characterises indirect detection:

1. ionising radiation is not directly visible, so x-rays and gamma rays are converted to electrical signal and therefore detected indirectly
2. high energetic photons are first converted to lower energy photons and then converted to electrical signal

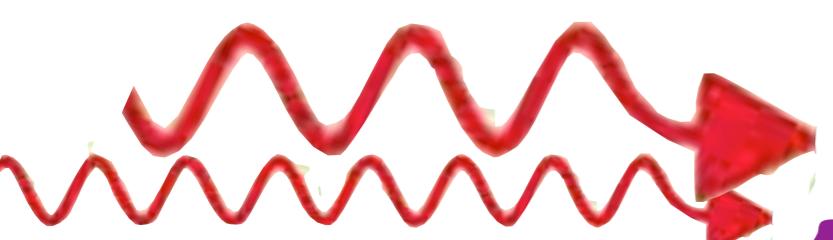
Detector for ionising radiation: basic principles

pulse mode



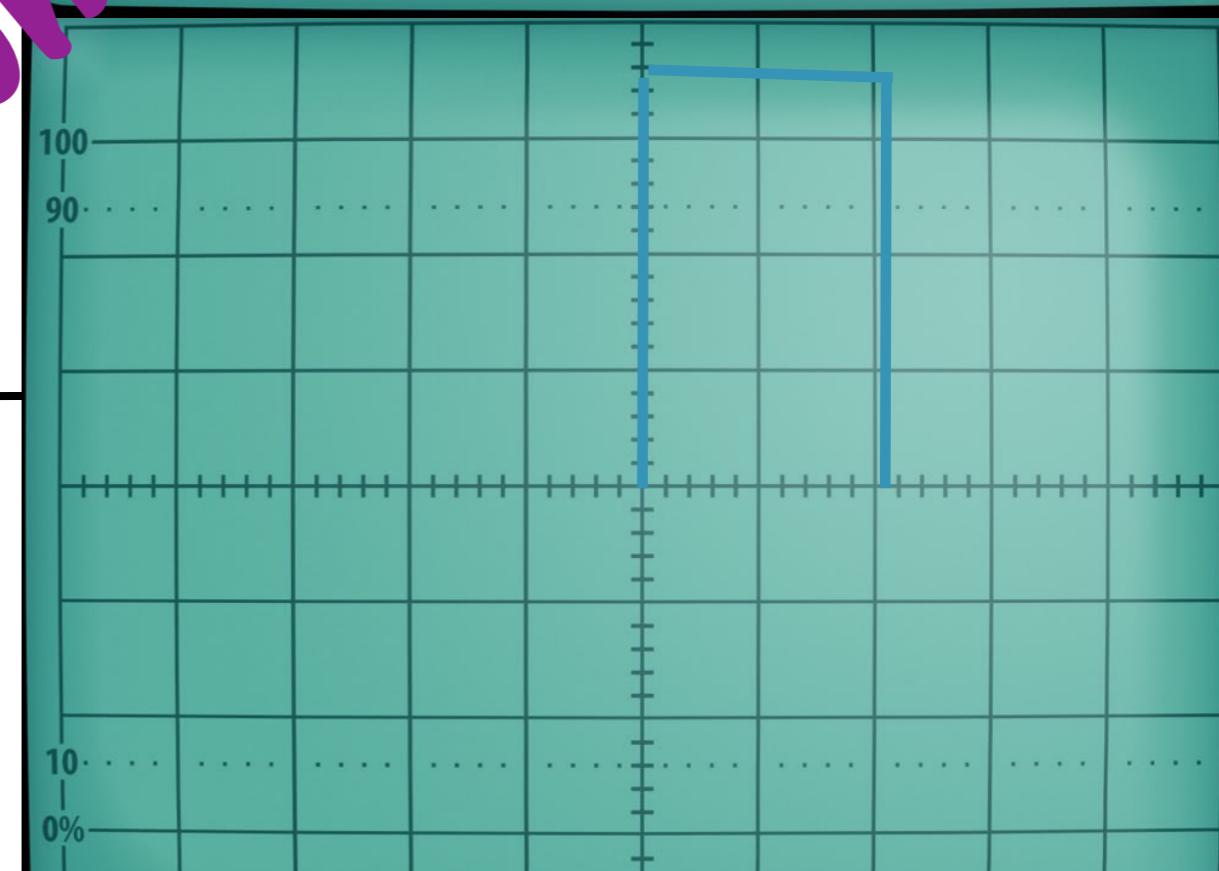
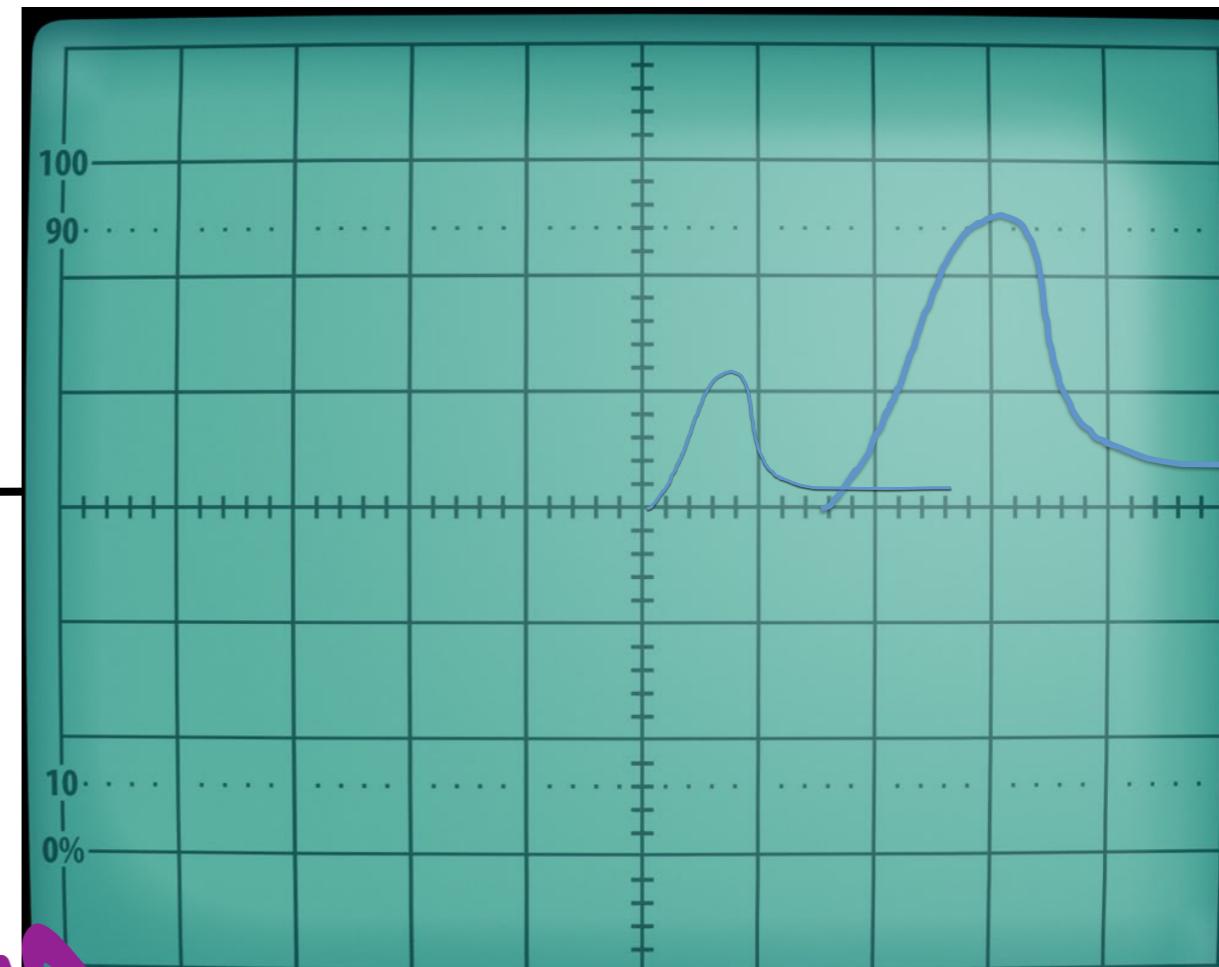
photon counting, energy resolving

current mode



energy integrating

Emission
Transmission



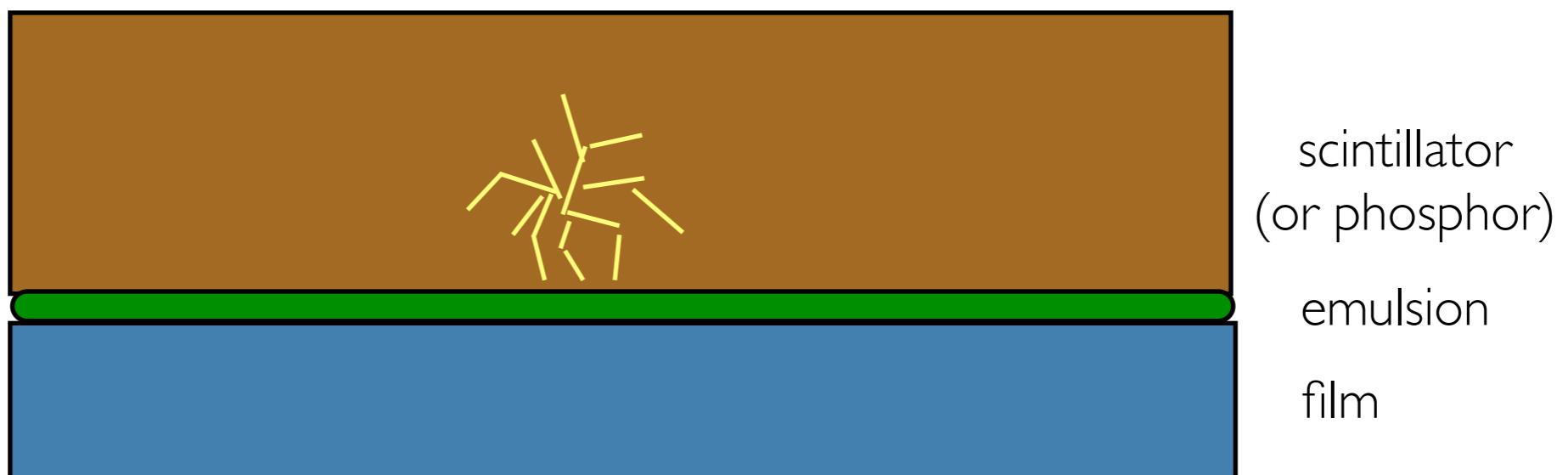
Common “indirect detection”
detectors in radiography:

Filmcassette:



Filmcassette:

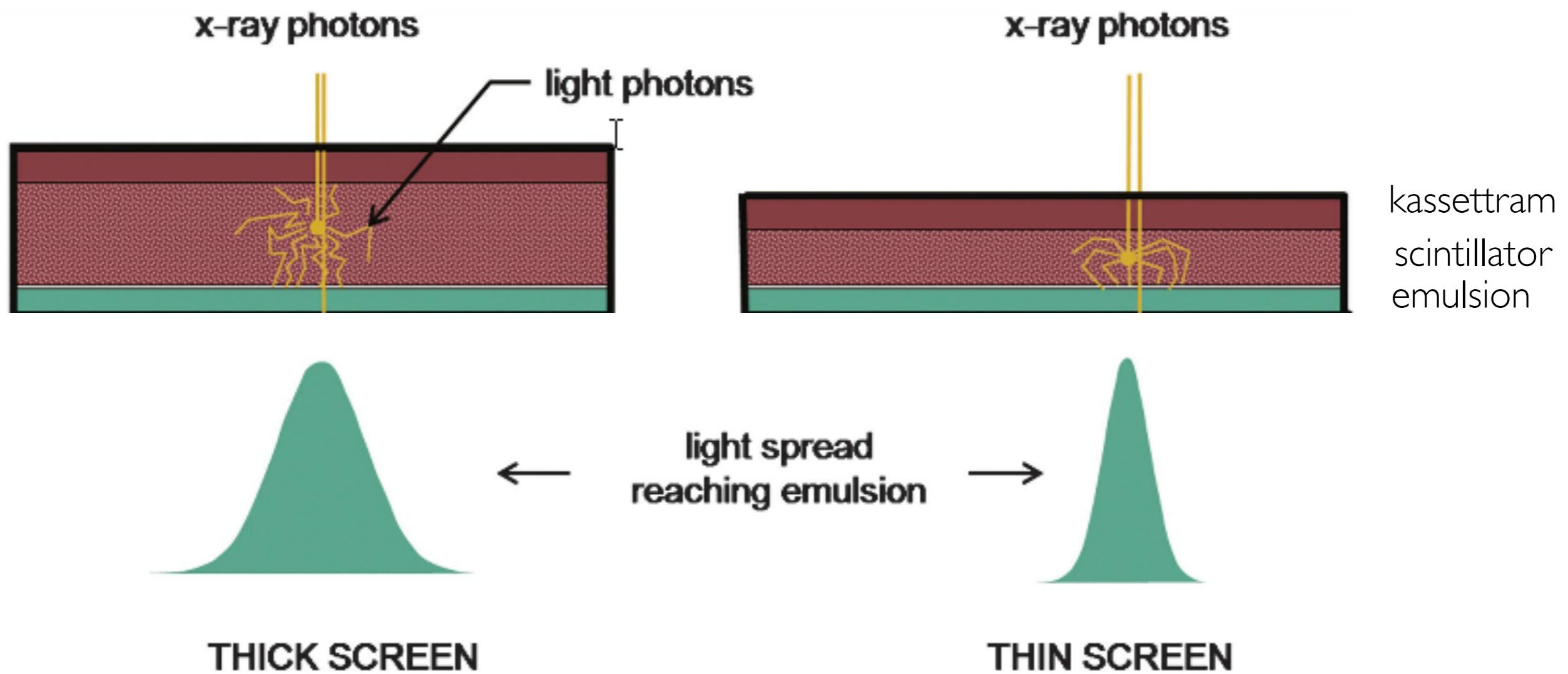
Filmcassette:

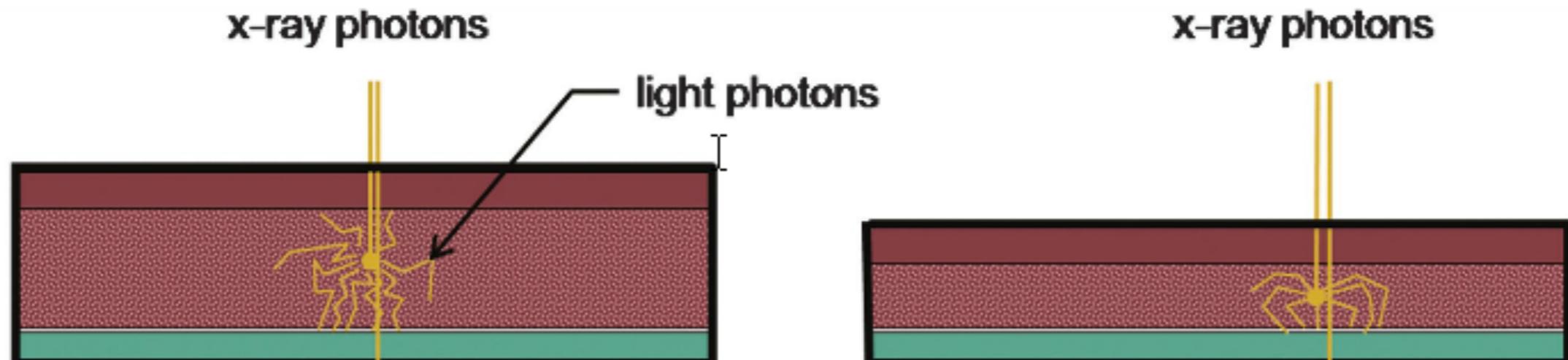


The role of the scintillator is:

1. increase detection efficiency
2. protect film from radiation exposure
3. “translate” x-rays to visible light
4. increase uniformity
5. increase spatial resolution

Filmcassette: effect of the scintillator

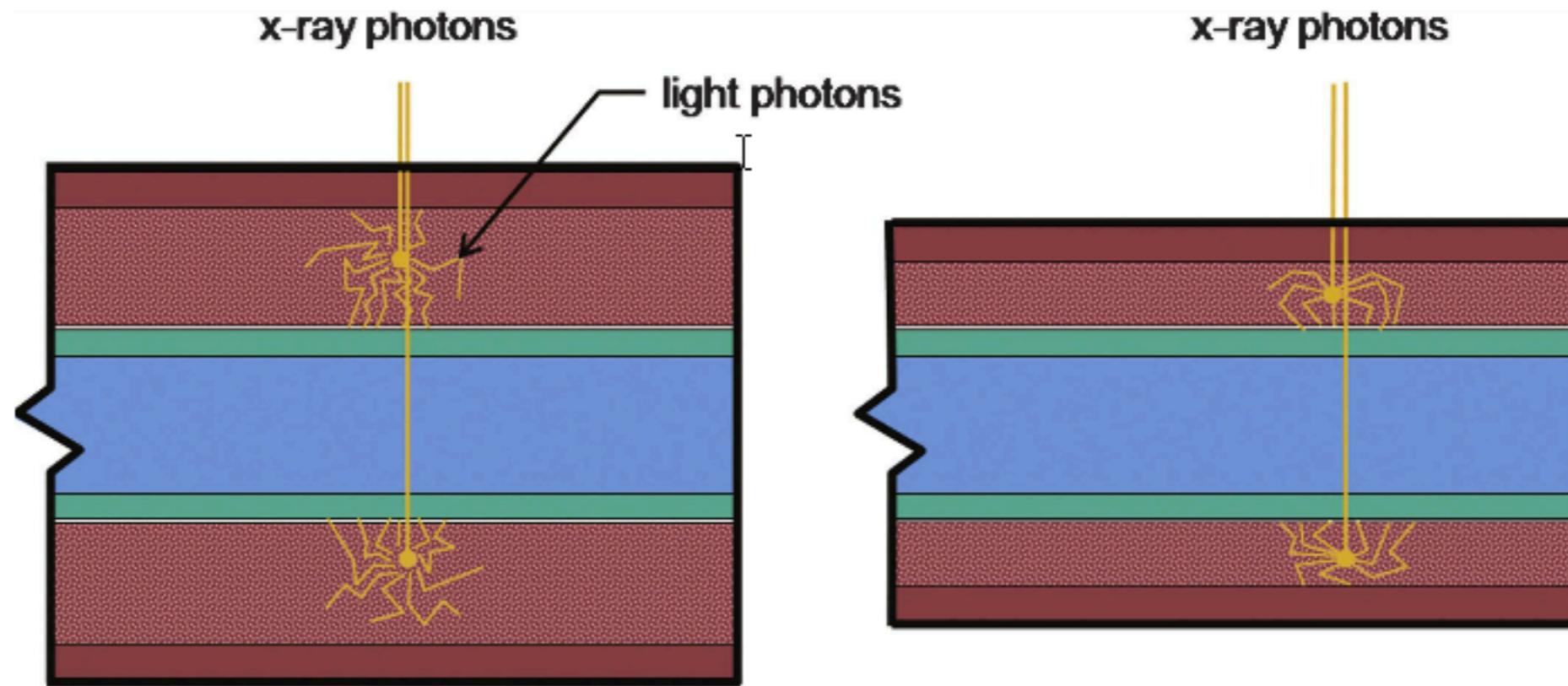




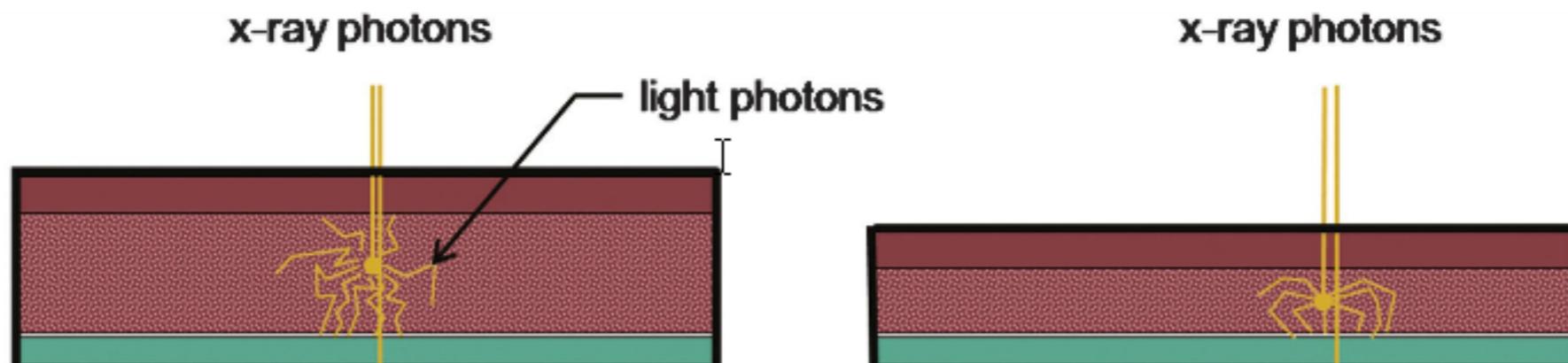
I x-ray 40keV -> hur många optiska fotoner?

- 1. 10 - 40
- 2. 10-40 thousand
- 3. 100-400 thousand
- 4. 10 - 40 millions

Filmcassette:

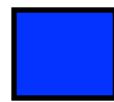


dubbelt så stor effektivitet med samma rumupplösning

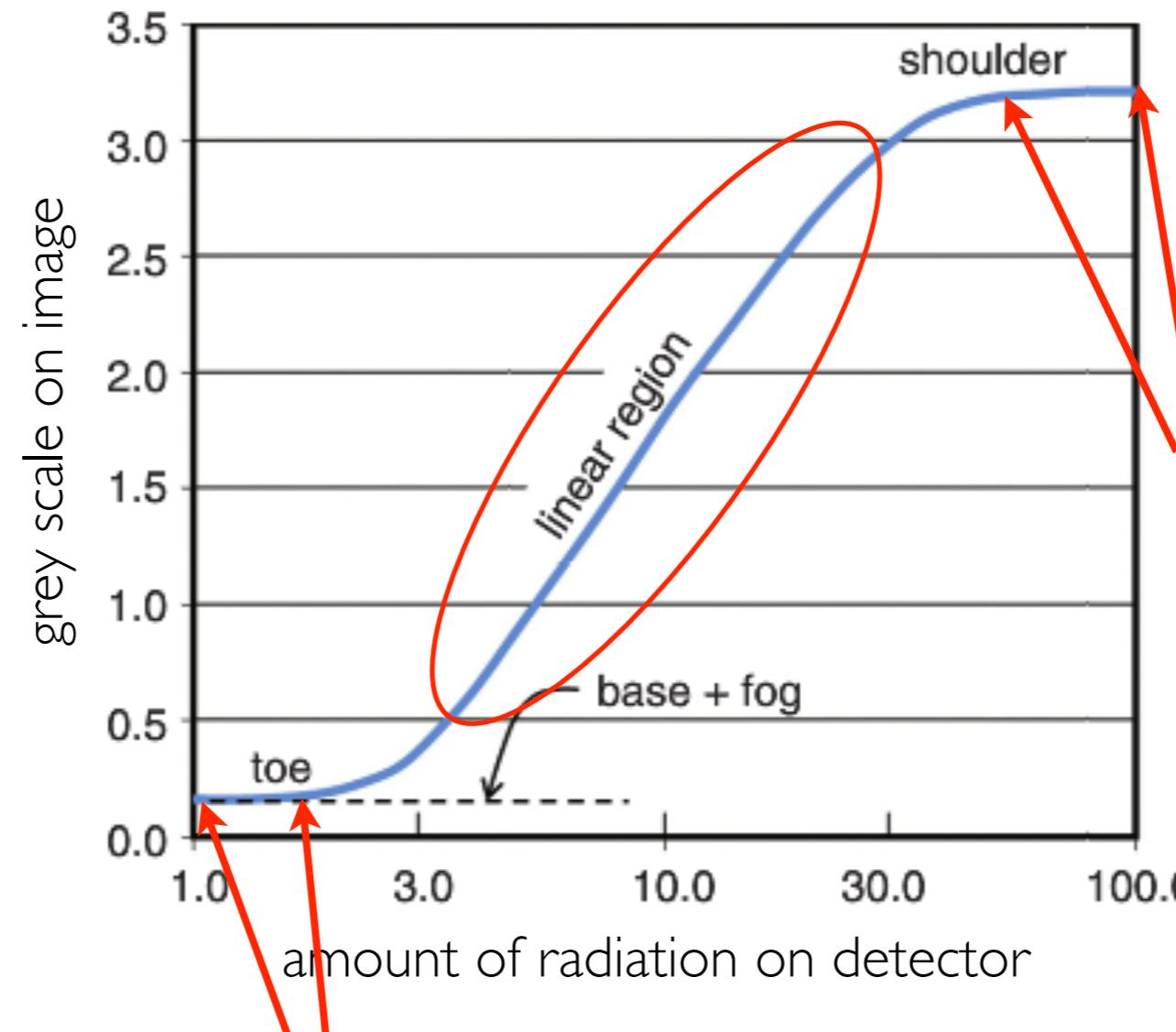
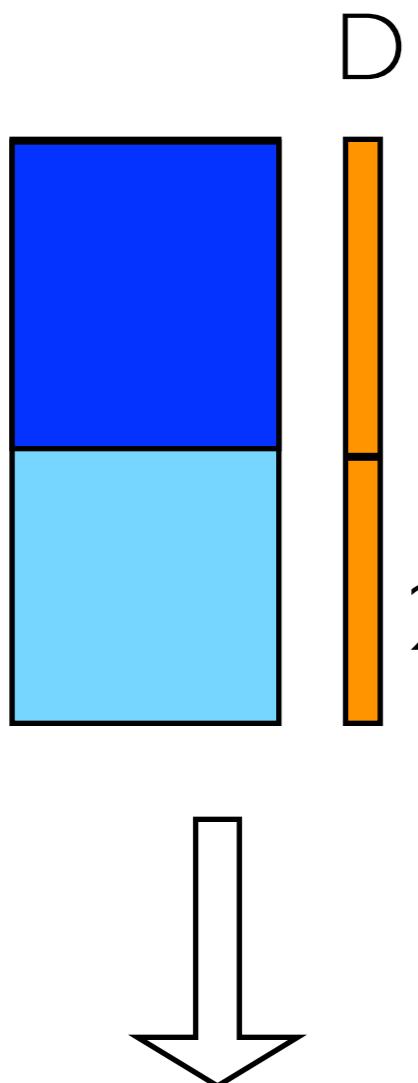
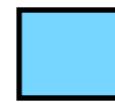


jfr med

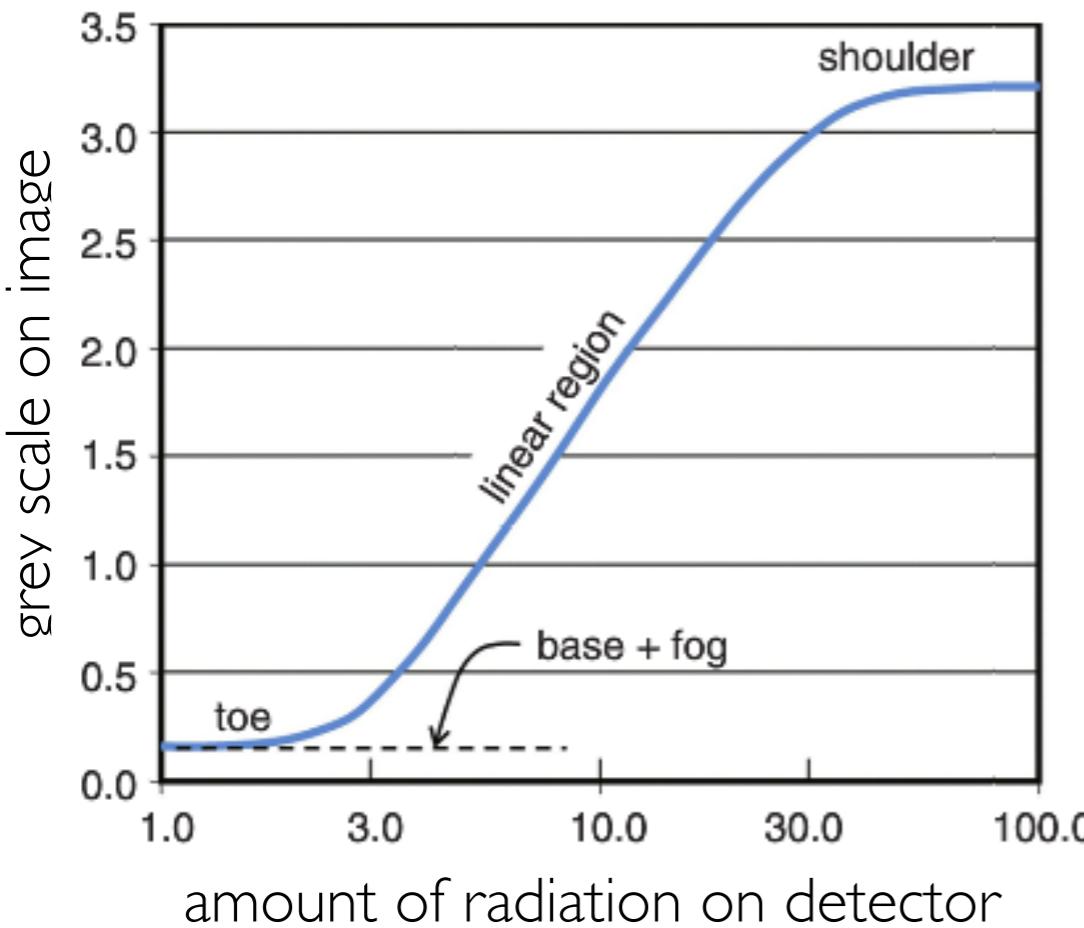
bild på film:



attenuates twice as much as



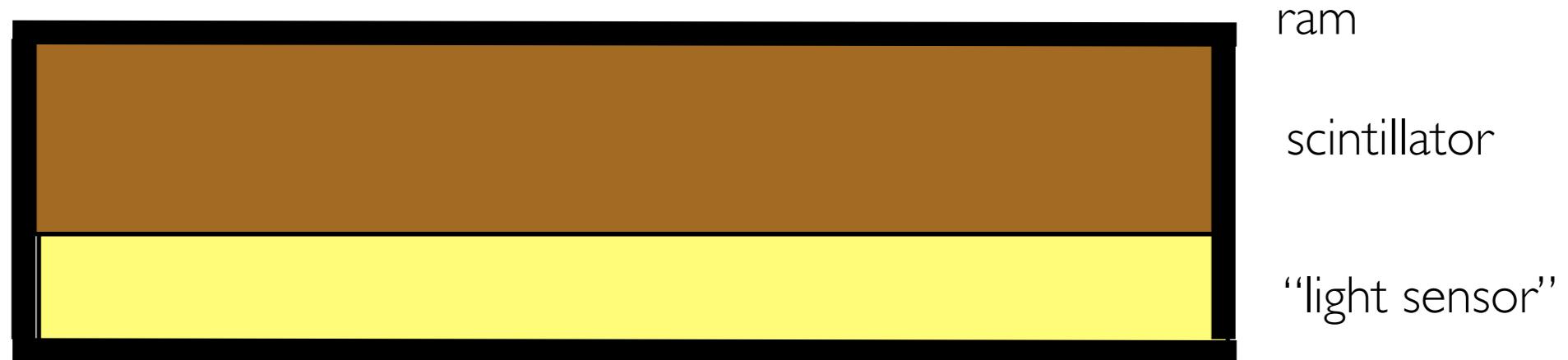
2 twice as much radiation as I



Which of the following claims are correct?

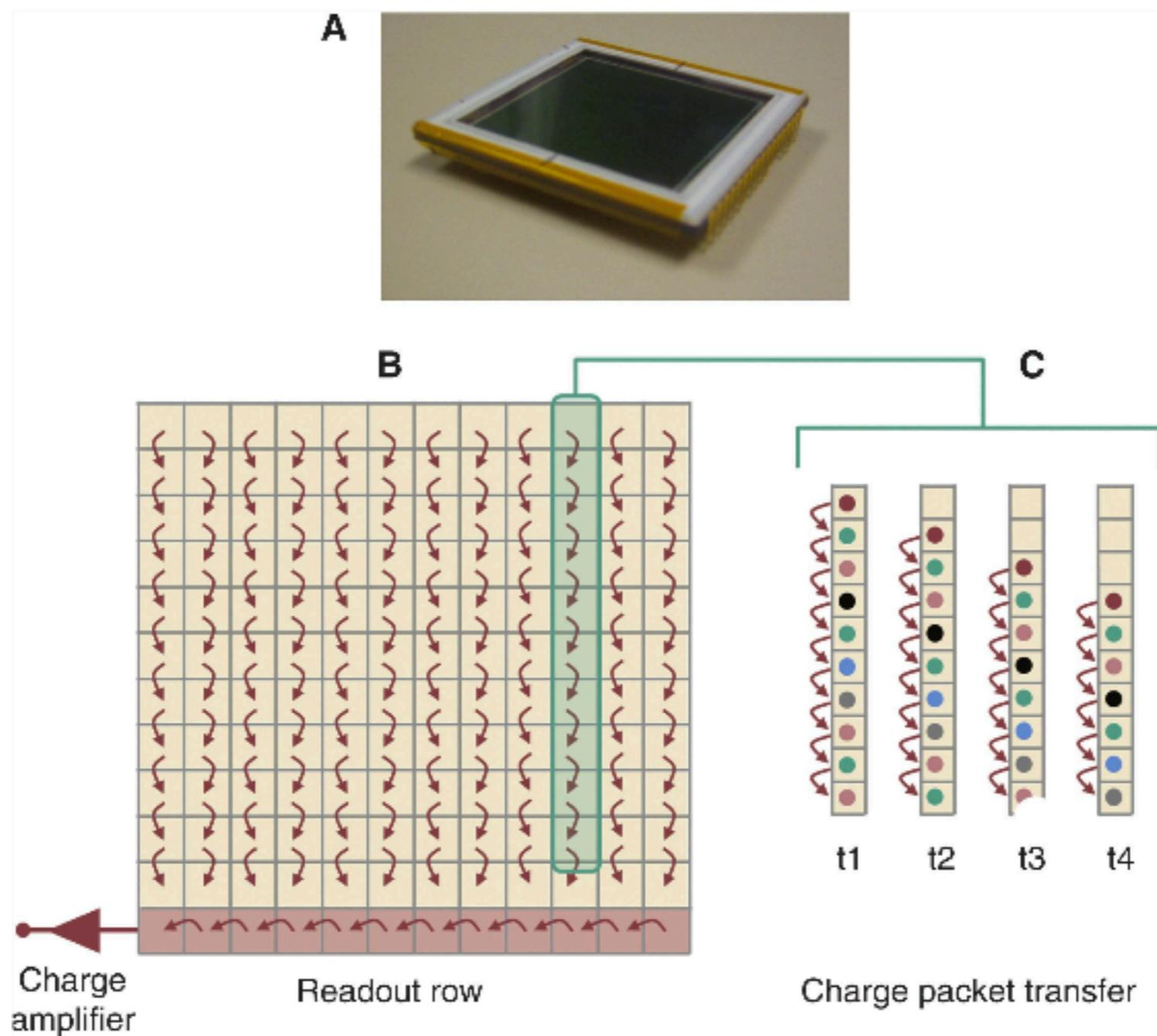
1. in the “toe” region the amount of light reaching the film is too low to be detected
2. in the “toe” region the image is saturated and increasing radiation does not change the grey scale
3. in the “shoulder” region the amount of light reaching the film is too low to be detected
4. in the “shoulder” region the image is saturated and increasing radiation does not change the grey scale
5. at any point in the linear region you can double exposure without reaching saturation

Better than film!

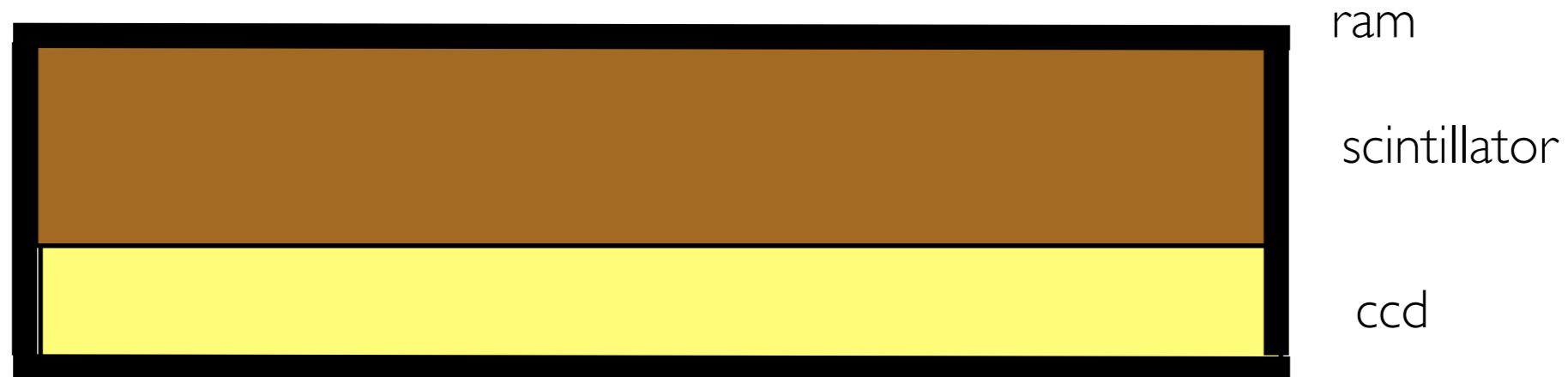


DR: CCD & CMOS

Charge-Coupled Device:

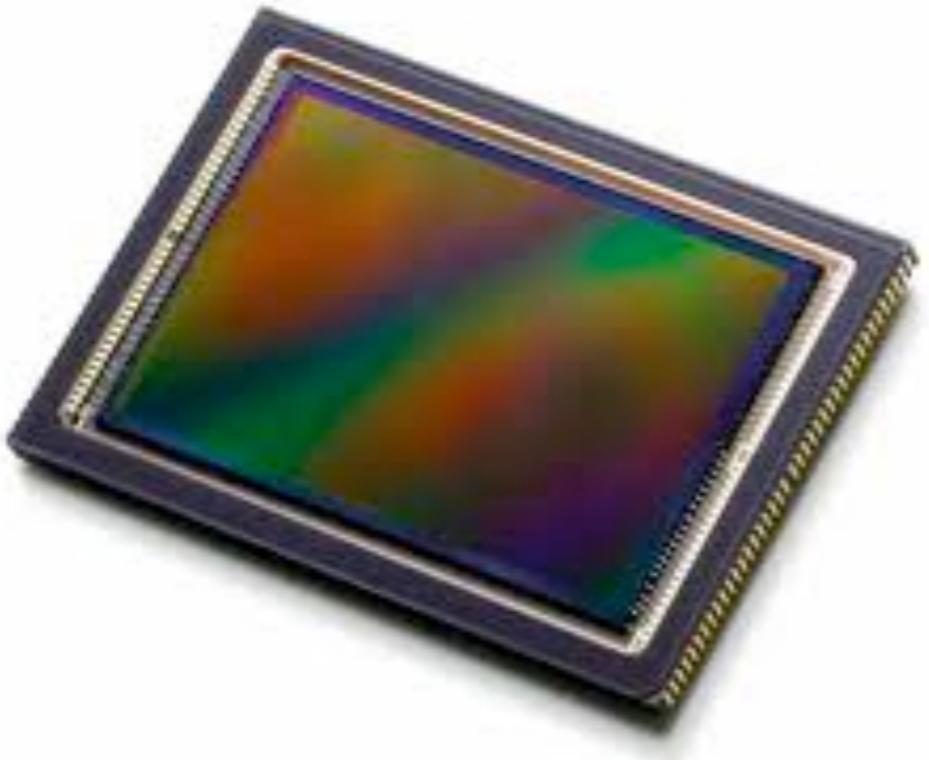


CCD kan användas i stället för film:



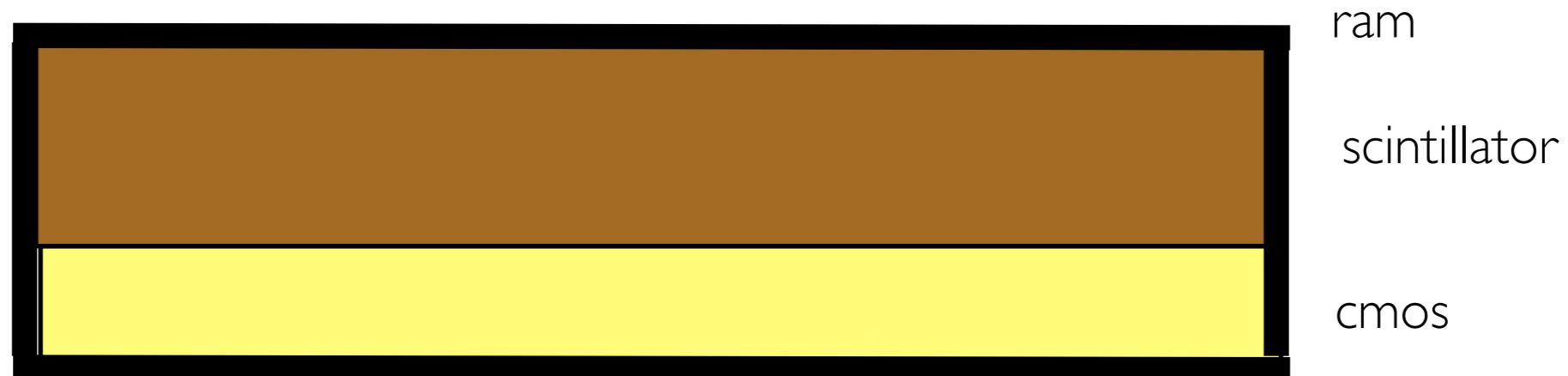
Complementary Metal-Oxide Semiconductor:

same as CCD, fotons -> electrons

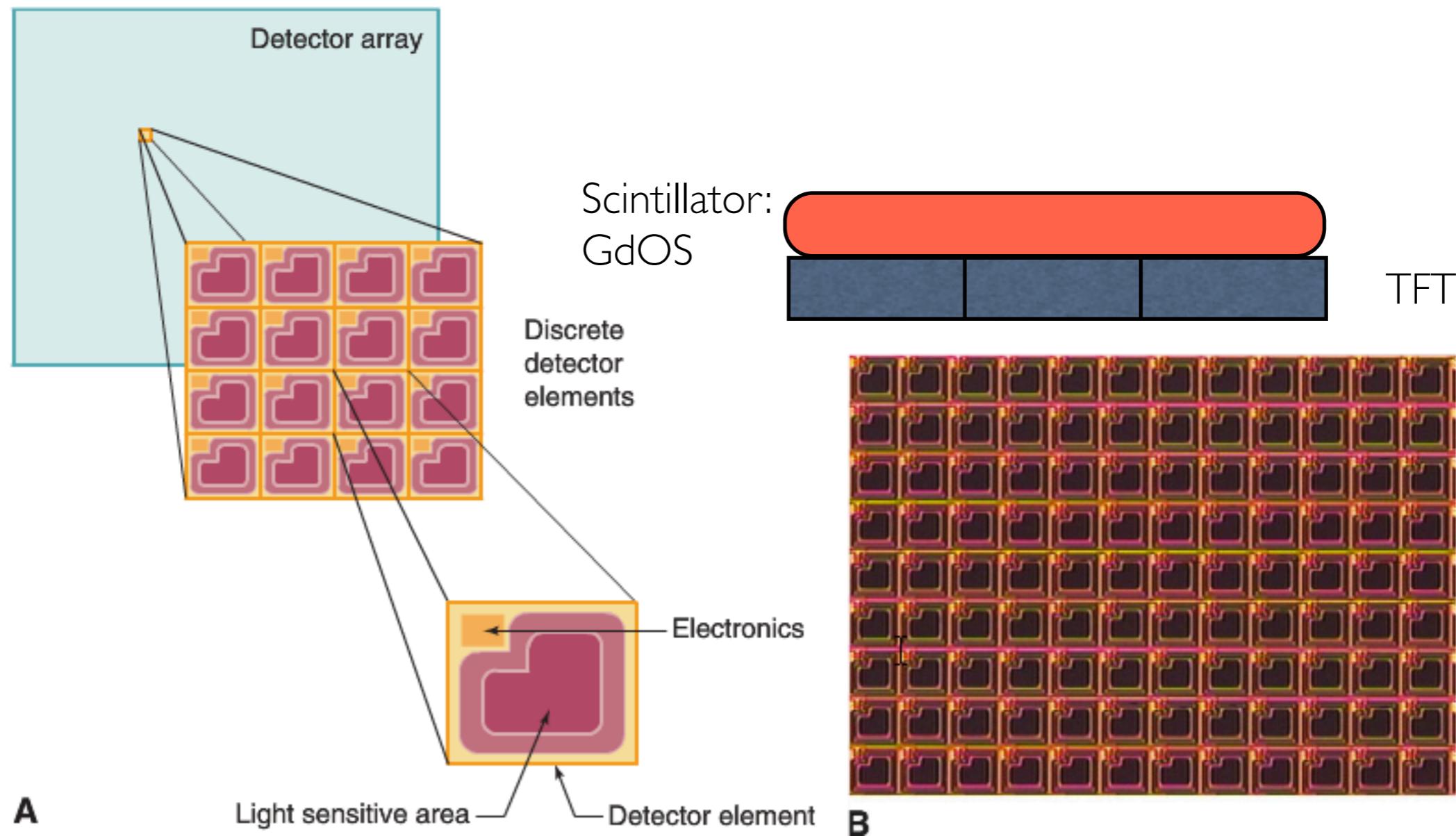


- + each pixel can be accessed random!
- noise
- size (small FOV 10×15 cm)

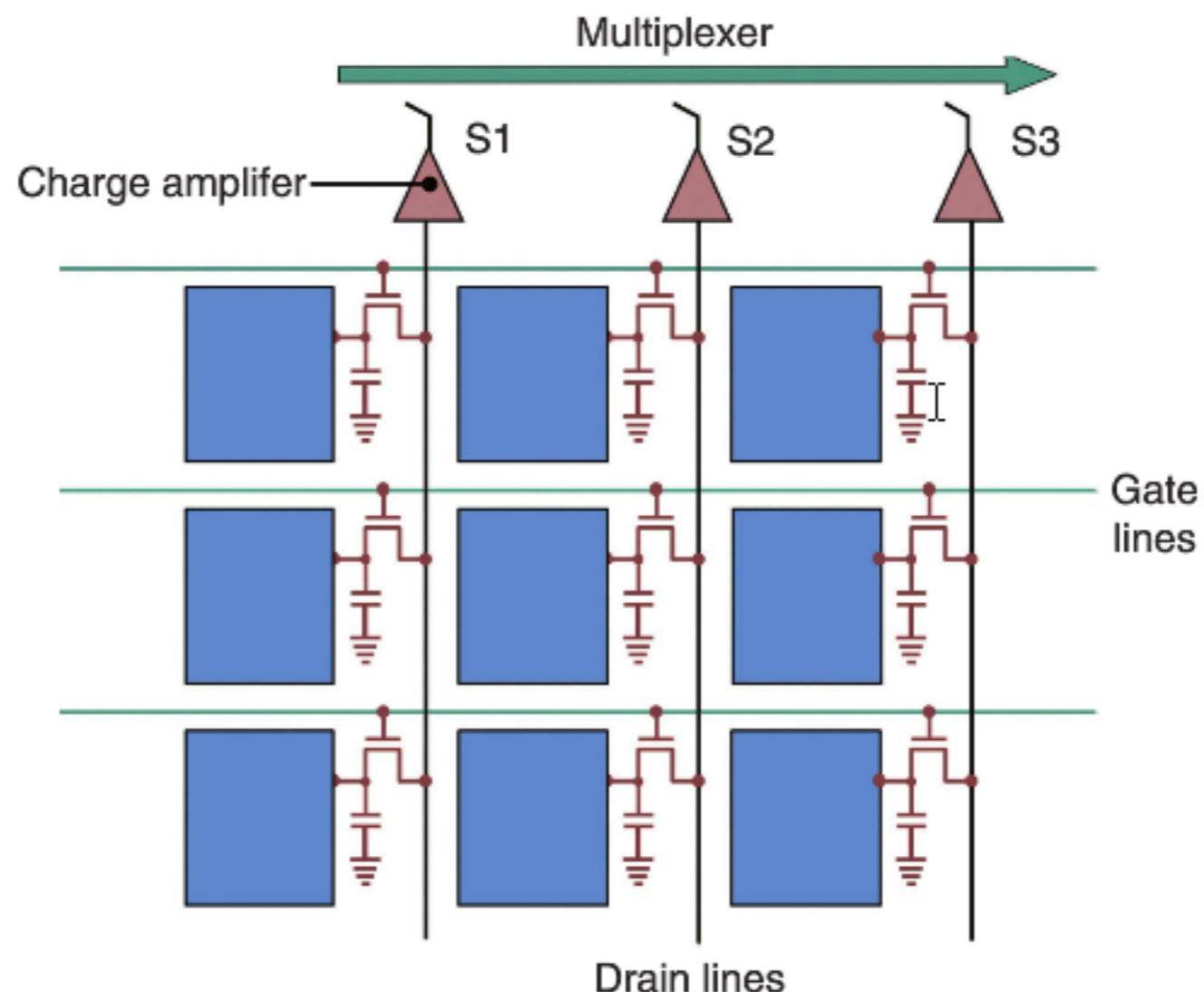
CMOS kan användas i stället för film:



Flat Panel Thin-Film-Transistor Array Detectors



Flat Panel TFT Array Detectors: read out

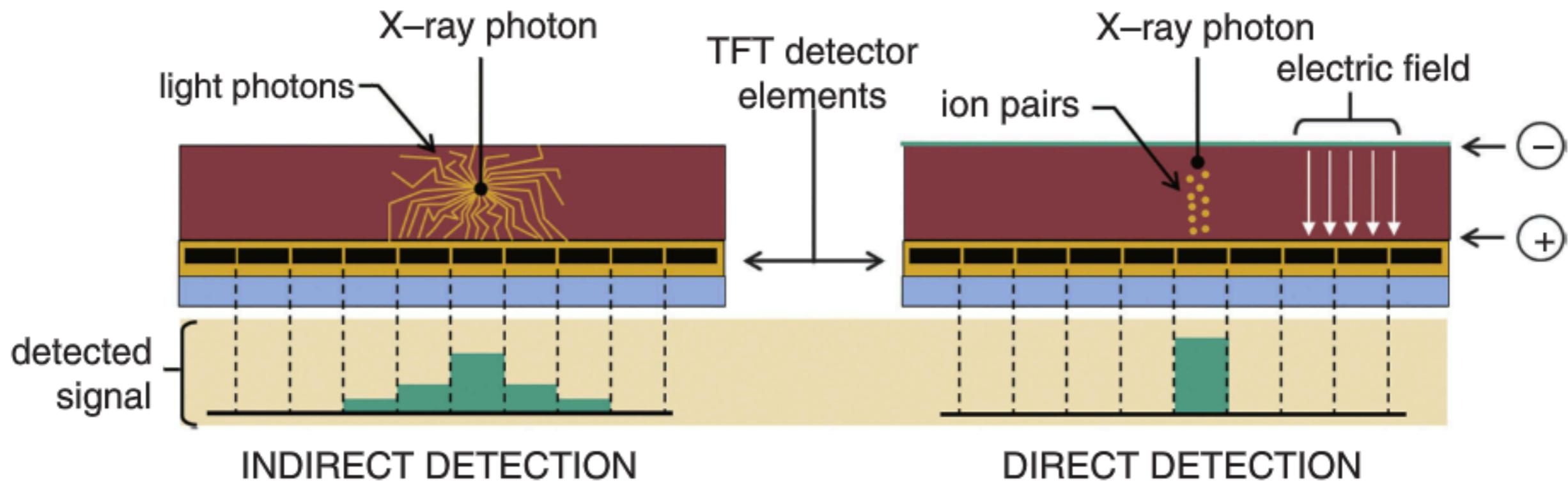


Flat Panel Thin-Film-Transistor Arrays have the same function as:

1. film
2. scintillator
3. phosphor
4. CCD
5. CMOS

direct detection detectors in
radiography:

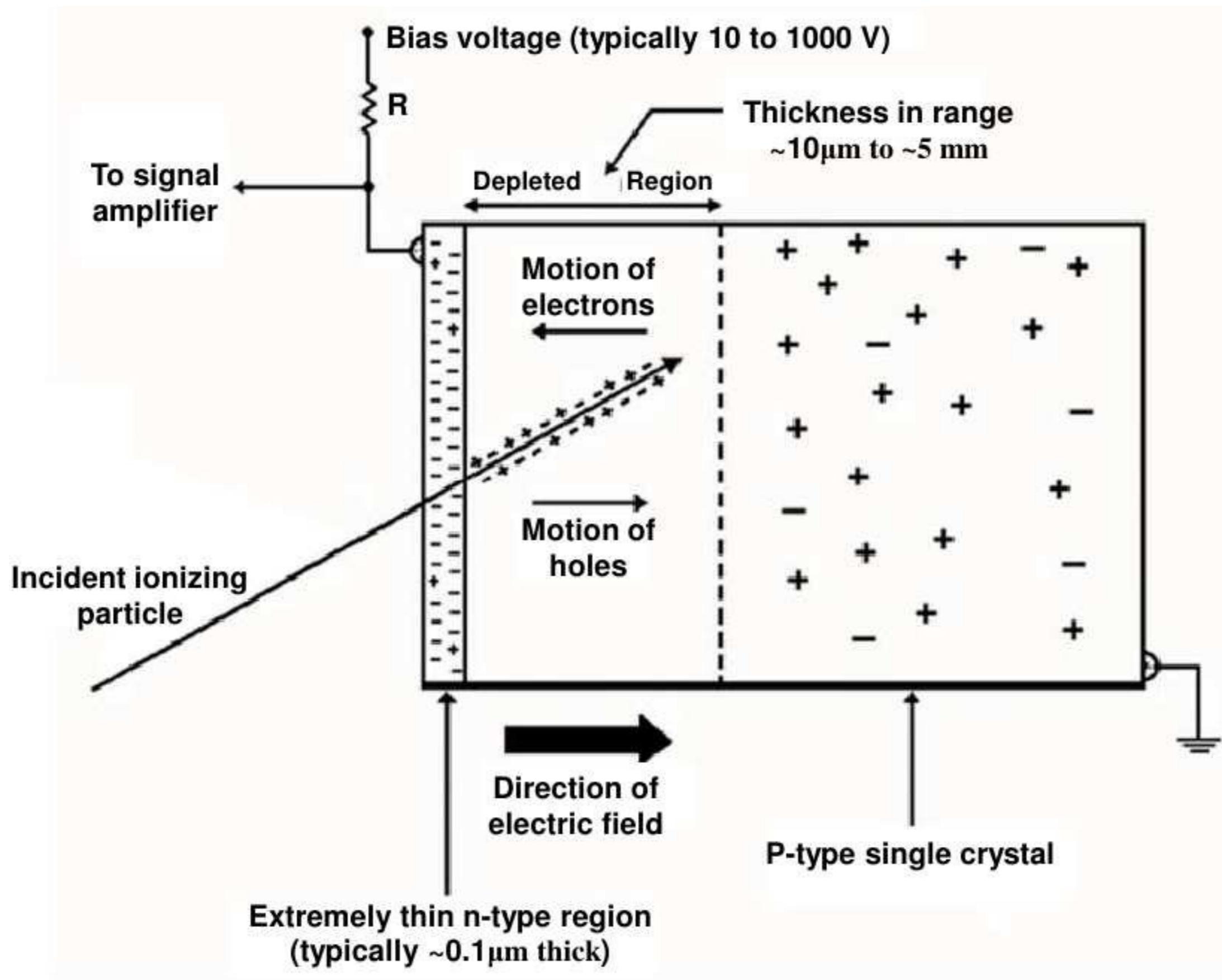
Direct vs Indirect detection

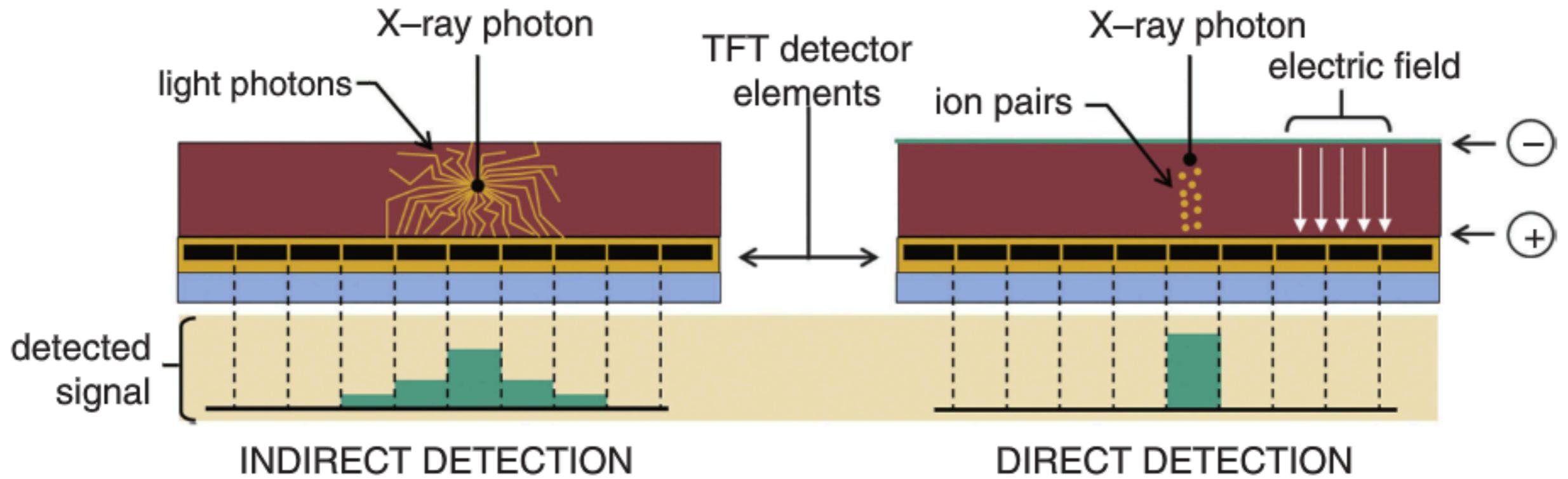


Name	Formula	Density (g/mm ³)	Z _{eff}	Light yield (ph/MeV)	Primary Decay time (ns)	Emissio n (nm)
LSO:Ce	Lu ₂ SiO ₅ :Ce	7.40	66	35,000	32	420
GSO:Ce	Gd ₂ SiO ₅ :Ce	6.71	59	20,000	60	440
LPS:Ce	Lu ₂ Si ₂ O ₇ :Ce	6.2	64	23,000	30	380
GPS:Ce	Gd ₂ Si ₂ O ₇ :Ce	5.5	58	30,000	46	380
BGO	Bi ₄ Ge ₃ O ₁₂	7.13	74	8,000	300	480
YAP:Ce	YAlO ₃ :Ce	5.35	34	20,000	24	365
LuYAG:Pr	Lu _{2.26} Y _{.79} Al ₅ O ₁₂ :Ce	6.20	60	33,000	20	310
GGAG:Ce	Gd ₃ Ga ₅ Al ₂ O ₁₂ :Ce	6.5	54	47,000	51	540

semi-conductor	density [g/cm ³]	Z	E _{gap} [eV]	ε [eV]	X ₀ [cm]
Si	2.33	14	1.12	3.6	9.37
Ge	5.33	32	0.67	2.9	2.30
CdTe	5.85	48,52	1.44	4.43	1.52
CdZnTe	5.81		1.6	4.6	
HgI ₂	6.40	80,53	2.13	4.2	1.16
GaAs	5.32	31, 33	1.42	4.3	2.29

E_{gap} : band gap energy
 ϵ : an ionization potential
 X_0 : radiation length



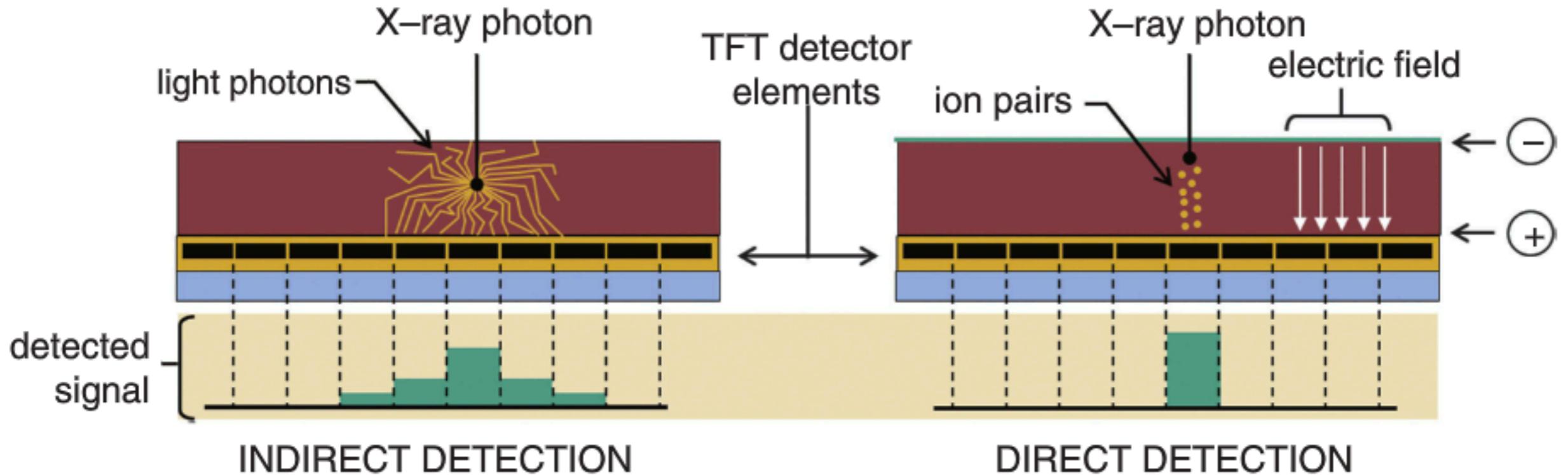


1. 0,15 mm

2. 1,5 mm

3. 1,5 cm

4. 15 cm



Consider 40keV x-ray and Si, how thick (approximately) has Si to be to detect 90%?

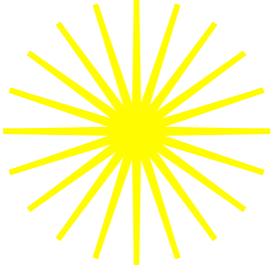
(please, calculate on your own before choosing an answer)

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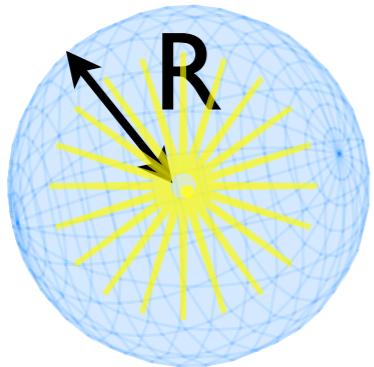
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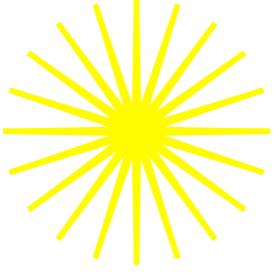
$t = 0$, N fotoner emitteras



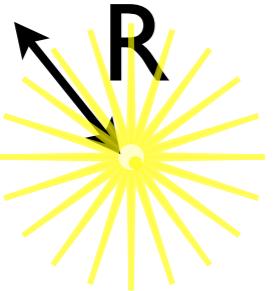
en liten stund senare N fotoner har alla
nått randen av den blåaktiga sfären

Antal fotoner per areaenhett är nu:

1. proportionell mot N/R
2. proportionell mot N/R^2
3. har inget att göra med varken N eller R



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Vilket stämmer?

1. det är jätteviktigt att komma i håg att mantelyta av en sfär är $4\pi R^2$
2. det är faktiskt omöjligt att komma i håg att mantelyta av en sfär är $4\pi R^2$
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4 “pie” är i kvadrat

$$4\pi R^2$$

En källa placeras i närheten av en detektor och räknehastighet då är 36000 cps. Källan flyttas till ett avstånd som är tre gånger det ursprungliga, räknehastighet blir då:

1. ~36000 cps
2. ~18000 cps
3. ~12000 cps
4. ~9000 cps
5. ~4000 cps
6. man bör aldrig flytta en källa medan en detektor räknar

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