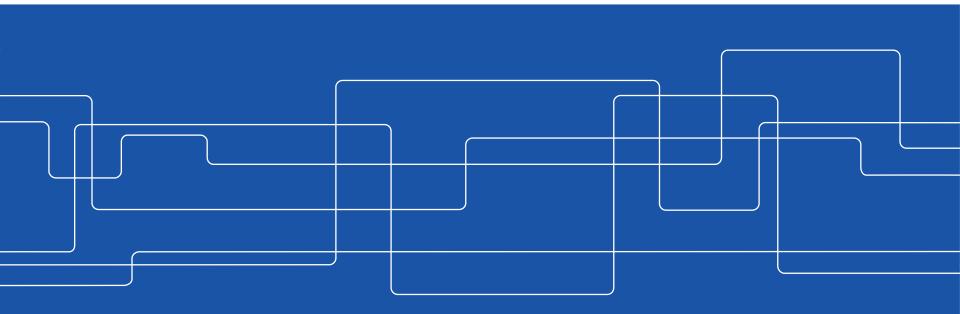


# Introduction to Robotics

## DD2410 - Introduction to Robotics

Lecture 4 - Differential Kinematics & Dynamics





#### Schedule - Lectures

- Sep 02 1. Intro, Course fundamentals, Topics, What is a Robot, History, Applications.
- Sep 03 2 ROS Introduction (Scheduled as lab, will be in zoom only)
- Sep 03 3 Manipulators, Kinematics
- Sep 06 4. Differential kinematics, dynamics
- Sep 08 5. Actuators, sensors I (force, torque, encoders, ...)
- Sep 13 6. Grasping, Motion, Control
- Sep 15 7. Planning (RRT, A\*, ...)
- Sep 20 8. Behavior Trees and Task Switching
- Sep 22 9. Mobility and sensing II (distance, vision, radio, GPS, ...)
- Sep 27 10. Localisation (where are we?)
- Sep 29 11. Mapping (how to build the map to localise/navigate w.r.t.?)
- Oct 04 12. Navigation (how do I get from A to B?)
- Oct 06 Q/A Open questions to your teachers.



#### Overview

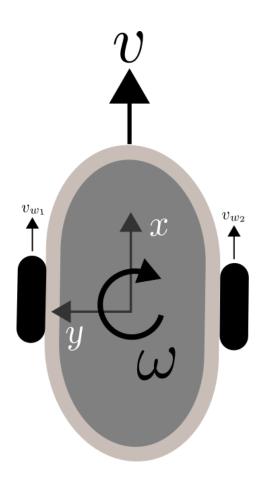
- Differential kinematics
  - Jacobians
  - Singularities
  - Manipulability
  - Calculations
- Dynamics
  - Forces and accelerations
  - algorithms for calculations



 For many operations, we are not interested in the stationary kinematics, but rather the differential kinematics, mainly for the mapping between velocities in configuration space and cartesian space



## Differential kinematics - Vacuum cleaner type



$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} \cos \theta & 0 \\ \sin \theta & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} v \\ \omega \end{bmatrix}$$
$$v = \frac{v_{w_1} + v_{w_2}}{2}$$
$$\omega = \frac{v_{w_2} - v_{w_1}}{2b}$$
$$v_{w_i} = \frac{2\pi r f \Delta_{\text{enc}}}{\text{ticks per rev}}$$



 The instantaneous transform between velocities in robot configuration space and cartesian space is given by the Jacobian:

 $\dot{X} = J(\Theta)\dot{\Theta}$ 

• Where each element  $j_{mn}$  in J is defined as  $\frac{\partial K(\Theta)_m}{\partial \Theta_n}$ 



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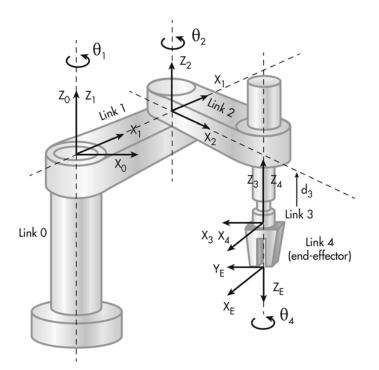


- Transform <sup>°</sup>T<sub>ε</sub> from end effector to base frame is dependent on configuration Θ
- The function that generates the end effector pose X given Θ, is called forward kinematics, K

$$\mathbf{X} = \mathbf{K}(\mathbf{\Theta}), \qquad \mathbf{r} = {}^{\circ}\mathbf{T}_{\mathbf{E}}\mathbf{p}_{\mathbf{E}}$$

where **p** is the position of the endpoint in the last frame

• Commonly, we define  $\mathbf{K}(\mathbf{\Theta})$  to output the pose vector  $\mathbf{X} = [\mathbf{x} \ \mathbf{y} \ \mathbf{z}]^{\mathsf{T}}$ , where  $\alpha \ \beta \ \gamma$  are the *Euler Angles* 



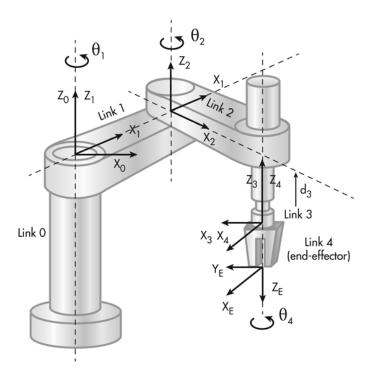


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See R-MPC 2.4

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 The instantaneous transform between velocities in robot configuration space and cartesian space is given by the Jacobian:

 $\dot{X} = J(\Theta)\dot{\Theta}$ 

• Where each element  $j_{mn}$  in J is defined as  $\frac{\partial K(\Theta)_m}{\partial \Theta_n}$ 

• Thus, each column in J can be seen as the vector  $\Delta X_{i}$ , or the motion in X caused by motion in the joint  $\theta_{i}$ .



• The closed form of a typical manipulator Jacobian is not printable



#### Differential kinematics

## The closed form of a typical manipulator Jacobian is not printable

The Puma 560 can be seen in Figures 1 and 2.

The forward kinematics  $K_f$  can be formulated as:

where

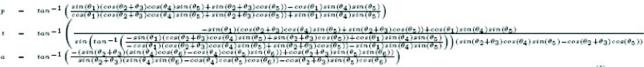
$$\mathbf{X} = \begin{bmatrix} x \\ y \\ z \\ p \\ t \\ a \end{bmatrix}, \qquad \boldsymbol{\Theta} = \begin{bmatrix} \theta_1 \\ \theta_2 \\ \theta_3 \\ \theta_4 \\ \theta_5 \\ \theta_6 \end{bmatrix}$$

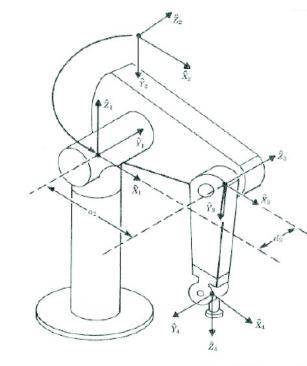
 $\mathbf{X} = K_f(\mathbf{\Theta})$ 

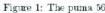
we have:

$$\begin{array}{rcl} x & = & \cos(\theta_1) * \left[a_2\cos(\theta_2) + a_3\cos(\theta_2 + \theta_3) - d_4\sin(\theta_2 + \theta_3)\right] - d_3\sin(\theta_1) \\ y & = & \sin(\theta_1) * \left[a_2\cos(\theta_2) + a_3\cos(\theta_2 + \theta_3) - d_4\sin(\theta_2 + \theta_3)\right] + d_3\cos(\theta_1) \\ z & = & -a_3\sin(\theta_2 + \theta_3) + a_2\sin(\theta_2) - d_4\cos(\theta_2 + \theta_3) \\ p & = & \tan^{-1}(\frac{s1(c23c4s5 + s23c5) - c1s4s5}{c1(c23c4s5 + s23c5) + s14s5}) \\ t & = & \tan^{-1}(\frac{-s1(c23c4s5 + s23c5) + c1s4s5}{sin(tan^{-1}(-s1(c23c4s5 + s23c5) + c1(s4s5) - c1(c23c4s5 + s23c5) - s1s4s5))(s23c4s5 - c23c5)}) \\ a & = & \tan^{-1}(\frac{-(s23(s4c6 - c4c5s6) + c23s5c6)}{s23(s4s6 - c4c5c6) - c23s5c6}) \end{array}$$

Where the latter uses shorthand. The full expression is:







(1)

(2)

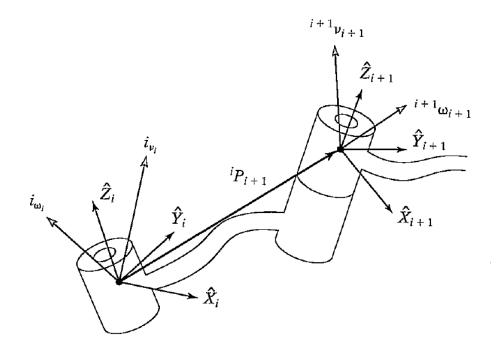
(3)



- The closed form of a typical manipulator Jacobian is often not printable, but can be derived by sequential application of frame transforms
- The motion of frame *i*+1, is a function of the motion of frame *i* and the motion of the joint between them.



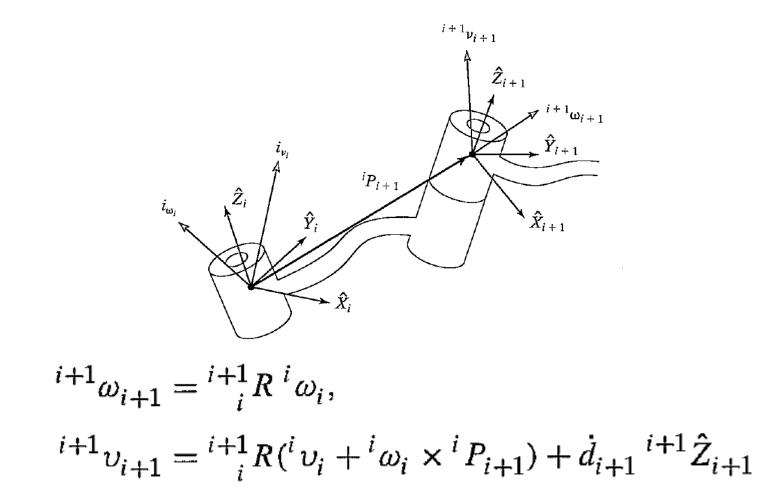
## Differential kinematics (R-MPC chapter 3): Rotational joints



$${}^{i+1}\omega_{i+1} = {}^{i+1}_{i}R {}^{i}\omega_{i} + \dot{\theta}_{i+1} {}^{i+1}\hat{Z}_{i+1}$$
$${}^{i+1}\upsilon_{i+1} = {}^{i+1}_{i}R ({}^{i}\upsilon_{i} + {}^{i}\omega_{i} \times {}^{i}P_{i+1})$$



### Differential kinematics (R-MPC chapter 3) - Prismatic joints

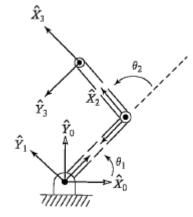




- Consequetive application of link transforms gives us velocities in end effector frame
- Note: resulting velocities are multilinear in joint velocities!
- Multiplying by rotation transform <sup>B</sup>R<sub>E</sub> gives us velocities in base frame
- Thus we can derive  $J(\Theta)$



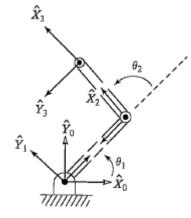
## Example: Planar robot



$$\begin{split} {}^{1}\omega_{1} &= \begin{bmatrix} 0\\ 0\\ \dot{\theta}_{1} \end{bmatrix}, \\ {}^{1}\upsilon_{1} &= \begin{bmatrix} 0\\ 0\\ 0\\ 0 \end{bmatrix}, \\ {}^{2}\omega_{2} &= \begin{bmatrix} 0\\ 0\\ \dot{\theta}_{1} + \dot{\theta}_{2} \end{bmatrix}, \\ {}^{2}\upsilon_{2} &= \begin{bmatrix} c_{2} & s_{2} & 0\\ -s_{2} & c_{2} & 0\\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0\\ l_{1}\dot{\theta}_{1} \\ 0 \end{bmatrix} = \begin{bmatrix} l_{1}s_{2}\dot{\theta}_{1} \\ l_{1}c_{2}\dot{\theta}_{1} \\ 0 \end{bmatrix}, \\ {}^{3}\omega_{3} &= {}^{2}\omega_{2}, \\ {}^{3}\upsilon_{3} &= \begin{bmatrix} l_{1}c_{2}\dot{\theta}_{1} + l_{2}(\dot{\theta}_{1} + \dot{\theta}_{2}) \\ 0 \end{bmatrix}, \\ {}^{3}\omega_{3} &= \sum_{1}^{0}R & \frac{1}{2}R & \frac{2}{3}R = \begin{bmatrix} c_{12} & -s_{12} & 0\\ s_{12} & c_{12} & 0\\ 0 & 0 & 1 \end{bmatrix}, \\ {}^{0}\upsilon_{3} &= \begin{bmatrix} -l_{1}s_{1}\dot{\theta}_{1} - l_{2}s_{12}(\dot{\theta}_{1} + \dot{\theta}_{2}) \\ l_{1}c_{1}\dot{\theta}_{1} + l_{2}c_{12}(\dot{\theta}_{1} + \dot{\theta}_{2}) \\ 0 \end{bmatrix}. \end{split}$$



## Example: Planar robot



$${}^{1}\omega_{1} = \begin{bmatrix} 0\\0\\\dot{\theta}_{1} \end{bmatrix},$$

$${}^{1}\upsilon_{1} = \begin{bmatrix} 0\\0\\0 \end{bmatrix},$$

$${}^{2}\omega_{2} = \begin{bmatrix} 0\\0\\\dot{\theta}_{1} + \dot{\theta}_{2} \end{bmatrix},$$

$${}^{2}\upsilon_{2} = \begin{bmatrix} c_{2} s_{2} & 0\\-s_{2} & c_{2} & 0\\0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0\\l_{1}\dot{\theta}_{1} \\0 \end{bmatrix} = \begin{bmatrix} l_{1}s_{2}\dot{\theta}_{1}\\l_{1}c_{2}\dot{\theta}_{1} \end{bmatrix},$$

$${}^{3}\omega_{3} = {}^{2}\omega_{2},$$

$${}^{3}\upsilon_{3} = \begin{bmatrix} l_{1}c_{2}\dot{\theta}_{1} + l_{2}(\dot{\theta}_{1} + \dot{\theta}_{2})\\0 \end{bmatrix},$$

$${}^{0}_{3}R = {}^{0}_{1}R \quad {}^{1}_{2}R \quad {}^{2}_{3}R = \begin{bmatrix} c_{12} & -s_{12} & 0\\s_{12} & c_{12} & 0\\0 & 0 & 1 \end{bmatrix},$$

$${}^{0}\upsilon_{3} = \begin{bmatrix} -l_{1}s_{1}\dot{\theta}_{1} - l_{2}s_{12}(\dot{\theta}_{1} + \dot{\theta}_{2})\\l_{1}c_{1}\dot{\theta}_{1} + l_{2}c_{12}(\dot{\theta}_{1} + \dot{\theta}_{2})\\0 \end{bmatrix},$$

$${}^{0}J(\Theta) = \begin{bmatrix} -l_{1}s_{1} - l_{2}s_{12} & -l_{2}s_{12}\\l_{1}c_{1} + l_{2}c_{12} & l_{2}c_{12} \end{bmatrix},$$



 $\dot{\mathbf{X}} = \mathbf{J}(\Theta) \dot{\Theta}$ 

- Column j<sub>i</sub> in J is the contribution of the i:th joint to the velocity of the end effector.
- Each column in **J** can be computed individually.



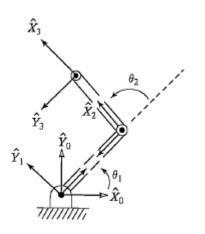
 $\dot{\mathbf{X}} = \mathbf{J}(\Theta)\dot{\Theta}$ 

Column j in J is the contribution of the inth joint to the velocity of the end effector. Each column in J can be computed individually. •

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## Example: Planar robot

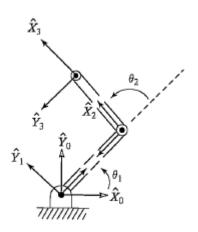


$${}^{0}J(\Theta) = \begin{bmatrix} -l_{1}s_{1} - l_{2}s_{12} & -l_{2}s_{12} \\ l_{1}c_{1} + l_{2}c_{12} & l_{2}c_{12} \end{bmatrix}$$

What happens if both angles are 0?



#### Example: Planar robot



$$\dot{\mathsf{X}} = \begin{bmatrix} -l_1 s_1 - l_2 s_{12} & -l_2 s_{12} \\ l_1 c_1 + l_2 c_{12} & l_2 c_{12} \end{bmatrix} \begin{bmatrix} \dot{\theta}_1 \\ \dot{\theta}_2 \end{bmatrix}$$

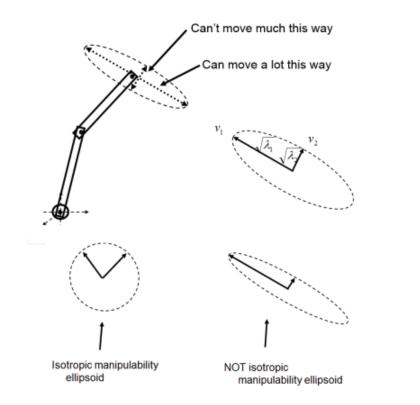
What happens if both angles are 0?

When the Jacobian loses rank, we get a kinematic singularity - we lose the ability to generate motion in some direction!



#### Manipulability

We can generalize this into a concept of manipulability w ۲



 $w = \sqrt{det(JJ^T)}$ 

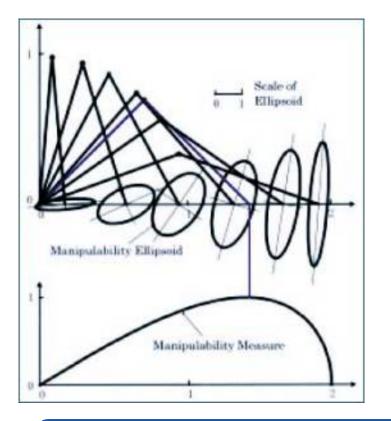
w is proportional to the volume of the *manipulability* ellipsoid.

Tsuneo Yoshikawa, "Manipulability of Robotic Mechanisms" The International Journal of Robotics Research Vol 4, Issue 2, pp. 3 - 9, June 1, 1985



### Manipulability

• We can generalize this into a concept of manipulability w



 $w = \sqrt{det(JJ^T)}$ 

w is proportional to the volume of the *manipulability ellipsoid*.



## Manipulability example



Image: Trossen Robotics



#### Jacobians

- The inverse Jacobian is trivial to calculate, as long as the Jacobian matrix is invertible.
- If J is not invertible, we can often use pseudo-inverse instead.



• We want to find the inverse kinematics

$$\Theta = K^{-1}(X)$$



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- We start with an approximation  $\widehat{\Theta} \!=\! \Theta \!+\! \varepsilon_{\Theta}$ 



• We want to find the inverse kinematics

$$\Theta = K^{-1}(X)$$

• We start with an approximation  

$$\widehat{\Theta} = \Theta + \epsilon_{\Theta}$$

$$X + \epsilon_X = K(\Theta + \epsilon_{\Theta})$$



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$$K(\Theta) + \epsilon_{X} = K(\Theta + \epsilon_{\Theta})$$



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• With linear approximation, we get  $\epsilon_{X} \approx J(\Theta) \epsilon_{\Theta}$ 



• We want to find the inverse kinematics

$$\Theta = K^{-1}(X)$$

• We start with an approximation  

$$\widehat{\Theta} = \Theta + \epsilon_{\Theta}$$

$$X + \epsilon_{X} = K(\Theta + \epsilon_{\Theta})$$

$$K(\Theta) + \epsilon_{X} = K(\Theta + \epsilon_{\Theta})$$

• With linear approximation, we get (assuming invertible J)  $\epsilon_X \approx J(\Theta) \epsilon_\Theta$  $\epsilon_\Theta \approx J^{-1}(\Theta) \epsilon_X$ 



Algorithm for finding inverse kinematics

Given target **X** and initial approximation  $\widehat{\Theta}$ 



• Algorithm for finding inverse kinematics Given target **X** and initial approximation  $\widehat{\Theta}$ 

repeat

 $\widehat{X} = K(\widehat{\Theta})$ 

until  $\epsilon_{X} \leq tolerance$ 



• Algorithm for finding inverse kinematics Given target **X** and initial approximation  $\widehat{\Theta}$ 

repeat

 $\widehat{X} = K(\widehat{\Theta}) \\ \epsilon_{X} = \widehat{X} - X$ 

until  $\epsilon_{X} \leq tolerance$ 



• Algorithm for finding inverse kinematics Given target **X** and initial approximation  $\widehat{\Theta}$ 

repeat

$$\widehat{X} = K(\widehat{\Theta}) \\ \epsilon_{X} = \widehat{X} - X \\ \epsilon_{\Theta} = J^{-1}(\widehat{\Theta}) \epsilon_{x}$$

until  $\epsilon_x \leq tolerance$ 



Jacobians for numerical inverse kinematics

• Algorithm for finding inverse kinematics Given target **X** and initial approximation  $\widehat{\Theta}$ 

repeat

$$\begin{aligned} \widehat{X} &= K(\widehat{\Theta}) \\ \widehat{\epsilon}_{X} &= \widehat{X} - X \\ \widehat{\epsilon}_{\Theta} &= J^{-1}(\widehat{\Theta}) \widehat{\epsilon}_{x} \\ \widehat{\Theta} &= \widehat{\Theta} - \widehat{\epsilon}_{\Theta} \end{aligned}$$

until  $\epsilon_x \leq tolerance$ 



• Virtual work must be same independent of coordinates

$$\mathcal{F}^T \delta \chi = \tau^T \delta \Theta$$

• We remember that:

$$\delta \chi = J \delta \Theta$$

• Which gives us:

$$\mathcal{F}^T J = \tau^T$$
$$\tau = J^T \mathcal{F}$$



$$\tau = J^T \mathcal{F}$$

 We can now see that for singular configurations, there will be directions where the required torque for a given force goes to zero, or inversely, the forces generated by a given torque tend to infinity. This may cause damage to the robot or the environment.



$$\tau = J^T \mathcal{F}$$

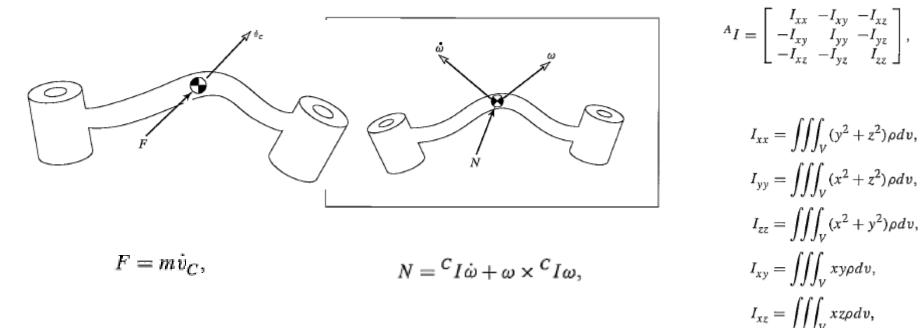
 We can also calculate inverse kinematics by virtual forces and torques. We apply a "force" correcting the end effector position, calculate the torques this would generate, and move the robot accordingly. This gives us the update step:

$$\boldsymbol{\epsilon}_{\Theta} = J^{T}(\widehat{\boldsymbol{\Theta}})\boldsymbol{\epsilon}_{x}$$

• This is useful when inverse of J does not exist, but typically converges slower.



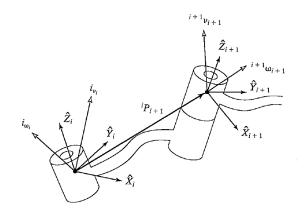
### Dynamics (R-MPC Chapter 7)



 $I_{yz} = \iiint_{v} yz \rho dv,$ 



## Dynamics (R- MPC chapter 7) - Rotational joints



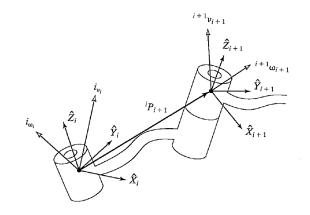
$${}^{i+1}\omega_{i+1} = {}^{i+1}_{i}R {}^{i}\omega_{i} + \dot{\theta}_{i+1} {}^{i+1}\hat{Z}_{i+1}$$
$${}^{i+1}\upsilon_{i+1} = {}^{i+1}_{i}R({}^{i}\upsilon_{i} + {}^{i}\omega_{i} \times {}^{i}P_{i+1})$$

$${}^{i+1}\dot{\omega}_{i+1} = {}^{i+1}_{i}R^{i}\dot{\omega}_{i} + {}^{i+1}_{i}R^{i}\omega_{i} \times \dot{\theta}_{i+1} {}^{i+1}\hat{Z}_{i+1} + \ddot{\theta}_{i+1} {}^{i+1}\hat{Z}_{i+1}$$

 ${}^{i+1}\dot{v}_{i+1} = {}^{i+1}_i R[{}^i\omega_i \times {}^iP_{i+1} + {}^i\omega_i \times ({}^i\omega_i \times {}^iP_{i+1}) + {}^i\dot{v}_i]$ 



### Dynamics (R-MPC chapter 7) - Prismatic joints



$$\begin{split} {}^{i+1}\omega_{i+1} &= {}^{i+1}_{i}R {}^{i}\omega_{i}, \\ {}^{i+1}\upsilon_{i+1} &= {}^{i+1}_{i}R ({}^{i}\upsilon_{i} + {}^{i}\omega_{i} \times {}^{i}P_{i+1}) + \dot{d}_{i+1} {}^{i+1}\hat{Z}_{i+1} \\ {}^{i+1}\dot{\omega}_{i+1} &= {}^{i+1}_{i}R {}^{i}\omega_{i}, \\ {}^{i+1}\dot{v}_{i+1} &= {}^{i+1}_{i}R ({}^{i}\dot{\omega}_{i} \times {}^{i}P_{i+1} + {}^{i}\omega_{i} \times ({}^{i}\omega_{i} \times {}^{i}P_{i+1}) + {}^{i}\dot{v}_{i}) \\ &+ 2{}^{i+1}\omega_{i+1} \times \dot{d}_{i+1} {}^{i+1}\hat{Z}_{i+1} + \ddot{d}_{i+1} {}^{i+1}\hat{Z}_{i+1} \end{split}$$

$${}^{i}\dot{v}_{C_{i}} = {}^{i}\dot{\omega}_{i} \times {}^{i}P_{C_{i}} + {}^{i}\omega_{i} \times ({}^{i}\omega_{i} + {}^{i}P_{C_{i}}) + {}^{i}\dot{v}_{i}$$

### Dynamics



Newton - Euler approach:

- Find the acceleration and velocity of each joint, working outwards
- Find the necessary torque/force to generate that acceleration, adding the external forces and torques, working inwards

### Dynamics



Outward iterations:  $i: 0 \rightarrow 5$ 

$$\begin{split} ^{i+1}\omega_{i+1} &= {}_{i}^{i+1}R\ {}^{i}\omega_{i} + \dot{\theta}_{i+1}\ {}^{i+1}\hat{Z}_{i+1}, \\ ^{i+1}\dot{\omega}_{i+1} &= {}_{i}^{i+1}R\ {}^{i}\dot{\omega}_{i} + {}_{i}^{i+1}R\ {}^{i}\omega_{i} \times \dot{\theta}_{i+1}\ {}^{i+1}\hat{Z}_{i+1} + \ddot{\theta}_{i+1}\ {}^{i+1}\hat{Z}_{i+1}, \\ ^{i+1}\dot{v}_{i+1} &= {}_{i}^{i+1}R({}^{i}\dot{\omega}_{i} \times {}^{i}P_{i+1} + {}^{i}\omega_{i} \times ({}^{i}\omega_{i} \times {}^{i}P_{i+1}) + {}^{i}\dot{v}_{i}), \\ ^{i+1}\dot{v}_{C_{i+1}} &= {}^{i+1}\dot{\omega}_{i+1} \times {}^{i+1}P_{C_{i+1}} \\ &+ {}^{i+1}\omega_{i+1} \times ({}^{i+1}\omega_{i+1} \times {}^{i+1}P_{C_{i+1}}) + {}^{i+1}\dot{v}_{i+1}, \\ ^{i+1}F_{i+1} &= m_{i+1}\ {}^{i+1}\dot{v}_{C_{i+1}}, \\ ^{i+1}N_{i+1} &= {}^{C_{i+1}}I_{i+1}\ {}^{i+1}\dot{\omega}_{i+1} + {}^{i+1}\omega_{i+1} \times {}^{C_{i+1}}I_{i+1}\ {}^{i+1}\omega_{i+1}. \end{split}$$

Inward iterations:  $i: 6 \rightarrow 1$ 

$$\begin{split} {}^{i}f_{i} &= {}^{i}_{i+1}R^{i+1}f_{i+1} + {}^{i}F_{i}, \\ {}^{i}n_{i} &= {}^{i}N_{i} + {}^{i}_{i+1}R^{i+1}n_{i+1} + {}^{i}P_{C_{i}} \times {}^{i}F_{i} \\ &+ {}^{i}P_{i+1} \times {}^{i}_{i+1}R^{i+1}f_{i+1}, \\ \tau_{i} &= {}^{i}n_{i}^{T}{}^{i}\hat{Z}_{i}. \end{split}$$



The resulting dynamic equations can be written on the form (state-space equation):

$$\tau = M(\Theta)\ddot{\Theta} + V(\Theta,\dot{\Theta}) + G(\Theta) + J^{T}f$$

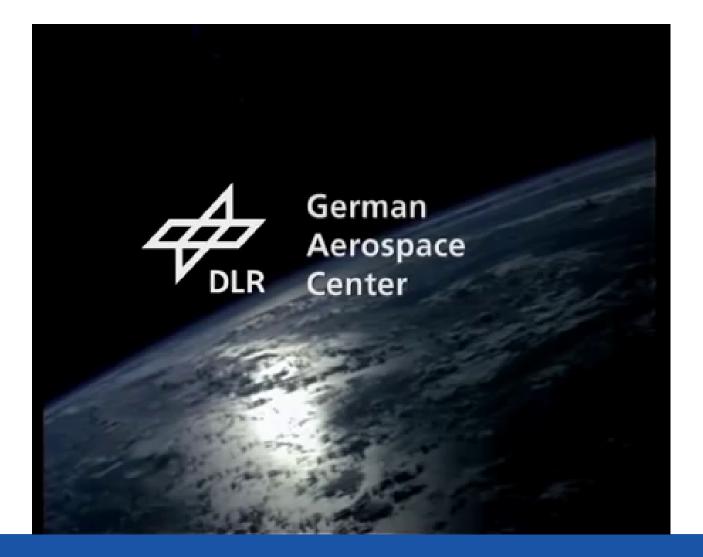


# $\tau = M(\Theta)\ddot{\Theta} + V(\Theta,\dot{\Theta}) + G(\Theta) + J^{T}f$











### State of the art - industrial manipulation







## End-Effector Airbags for Accelerating Human-Robot Collaboration