

# DD2552 - Seminars on Theoretical Computer Science, Programming Languages and Formal Methods, Seminar 10

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2021-09-30

# Last Seminar and Today

Last seminar:

- priced timed automata
- PWCTL and statistical verification

Today:

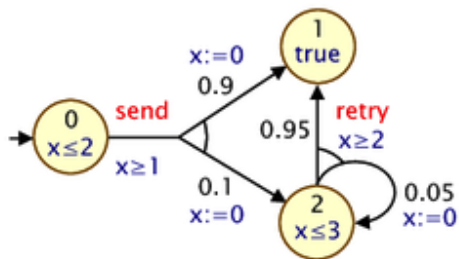
- note on tools for PTAs
- extension to more general hybrid systems

# UPPAAL and timed automata

- base UPPAAL used for model checking timed systems
- extension for statistical verification (UPPAAL-SMC)
- models are XML with code declarations
- specifications are *queries* as below

`Pr[time <= 200] (<> node1.s == 7 && node2.s == 8 )`

# PRISM and timed automata



# PRISM language

```
pta
module M
  s : [0..2] init 0;
  x : clock;

  invariant
    (s=0 => x<=2) &
    (s=2 => x<=3)
endinvariant

[send] s=0 & x>=1 -> 0.9:(s'=1)&(x'=0) +
  0.1:(s'=2)&(x'=0);
[retry] s=2 & x>=2 -> 0.95:(s'=1) +
  0.05:(s'=2)&(x'=0);
endmodule
```

# PRISM timed automata engines

- PTAs (mostly) treated as extension of MDPs with clocks
- three engines:
  - stochastic games engine (default, no global variables)
  - digital clocks engine (only single-clock constraints)
  - backwards reachability engine (no global variables)
- PTAs must be well-formed (not checked)
- some restrictions on guards/invariants

# Clock rates depending on other clocks

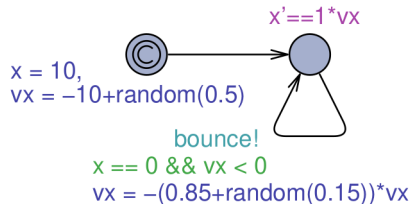
- with regular PTAs, we can express clocks that evolve at different rates
- but clock rates can only depend on state and variables, not on clocks
- when clock rates can depend on clocks, we get ordinary differential equations (ODEs)
- we get (networks of) *stochastic hybrid automata*, SHAs

# Statistical verification of SHAs

- with SMC, main problem is to generate **traces**
- for SHAs, need to solve ODEs (at least approximately)
- UPPAAL-SMC uses Euler integration method



# SHA example



- $x$ :  $x$  coordinate
- $vx$ : uncertain derivative of  $x$
- `bounce`: automaton output

- can introduce the usual probability operator on a HA logic
- example: Metric Temporal Logic (MTA)
- captures “quantitative timing properties”
- equip until operators with **intervals**, e.g.,  $\phi U_I \phi$
- define set of points  $R$  where we can evaluate formulas  $\phi$

$$R, t \models \phi U_I \phi' \text{ iff}$$

- there exists  $t' > t$  s.t.  $t' - t \in I$
- $R, t' \models \phi'$
- for all  $t''$  s.t.  $t < t'' < t'$ ,  $R, t'' \models \phi$

# Statistical checking for networks of HAs

- define “closed networks” of HAs (no dangling outputs)
- define paths on closed networks
- define and validate measures on paths
- generate random traces
- analyze traces and estimate/decide

# Bounding paths

can bound by:

- discrete system transitions
- clock value (Zeno issues)